

# A Comprehensive Tutorial on over 100 years of Diagrammatic Representations of Logical Statements and Relational Queries

Wolfgang Gatterbauer  
([w.gatterbauer@northeastern.edu](mailto:w.gatterbauer@northeastern.edu))

May 17, 2024  
(ICDE'24)

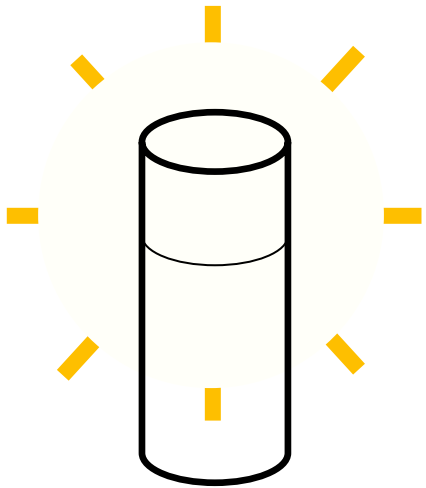
PLEASE ask questions and let me  
know if you spot any errors (we  
cover a lot of material and I  
must have made some errors...)  
Thank you ☺

An anonymous feedback form is linked from the tutorial web page:

<https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

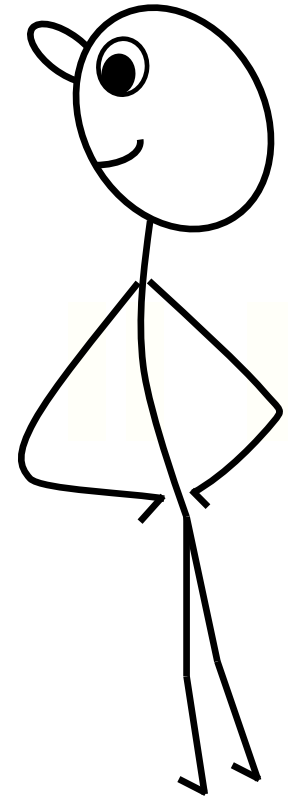


# 1. How do you know your voice assistant understood you correctly?



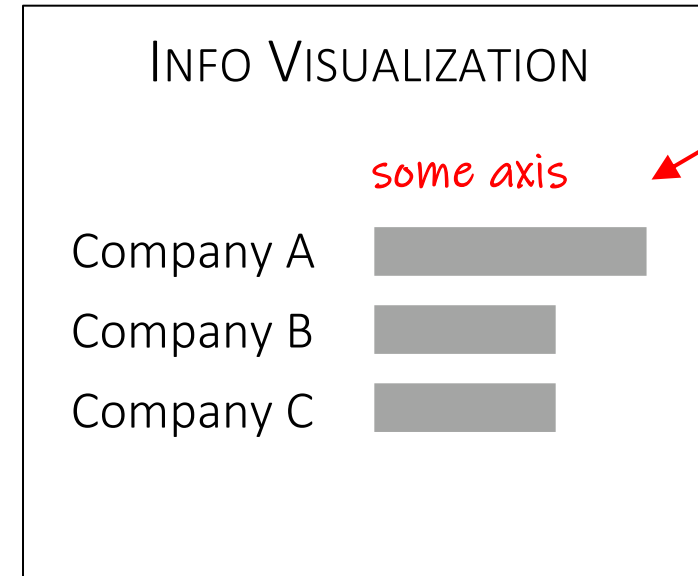
*Q: Find me companies in Utrecht.*

*A: Company A, Company B, Company C*

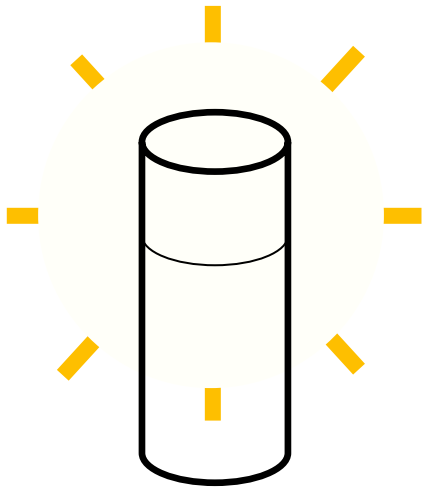




# 1. How do you know your voice assistant understood you correctly?

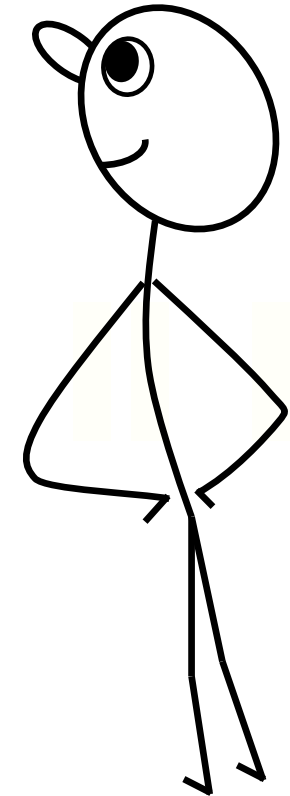


Visualize  
the answer

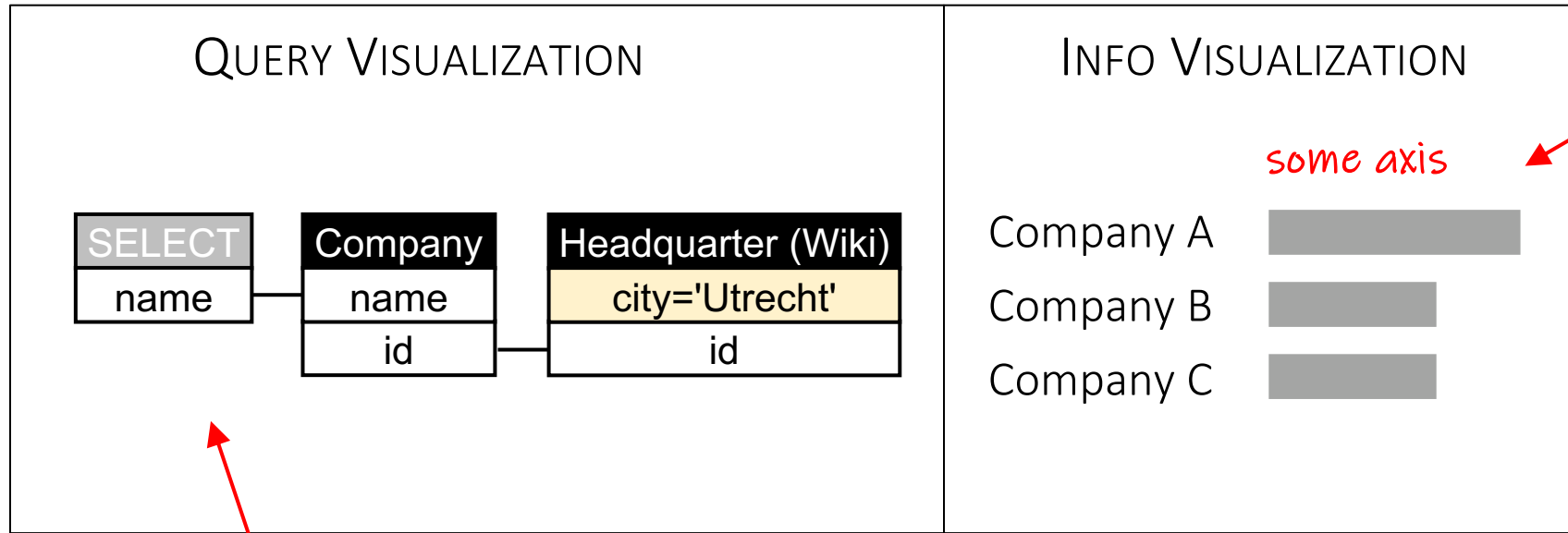


*Q: Find me companies in Utrecht.*

*A: Company A, Company B, Company C*



# 1. How do you know your voice assistant understood you correctly?



Visualize the answer

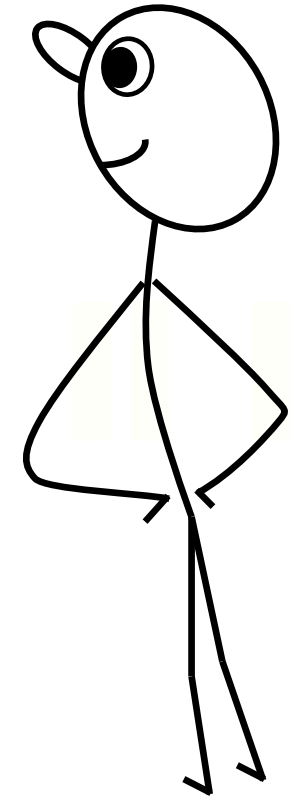
some axis

! Visualize the query

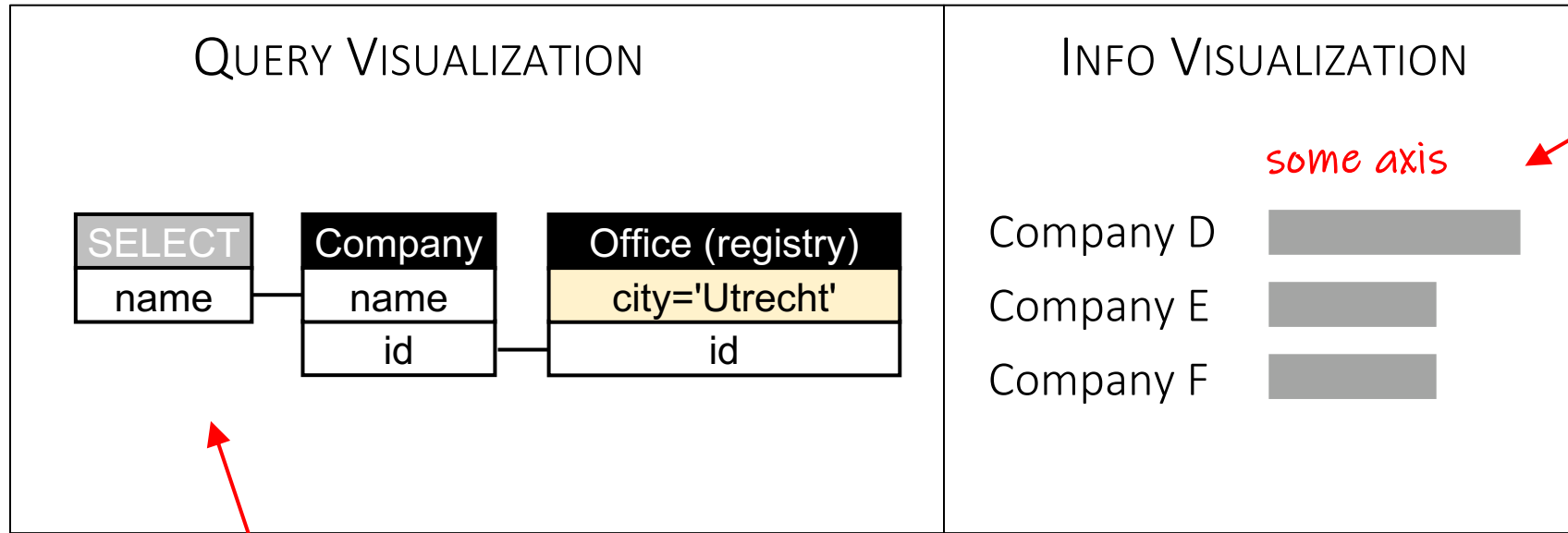
(what the assistant understood, and & how sources are used)

*Q: Find me companies in Utrecht.*

*A: Company A, Company B, Company C*



# 1. How do you know your voice assistant understood you correctly?



Visualize the answer

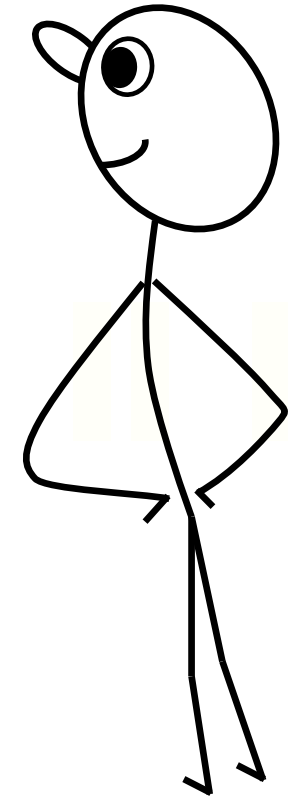
some axis

! Visualize the query

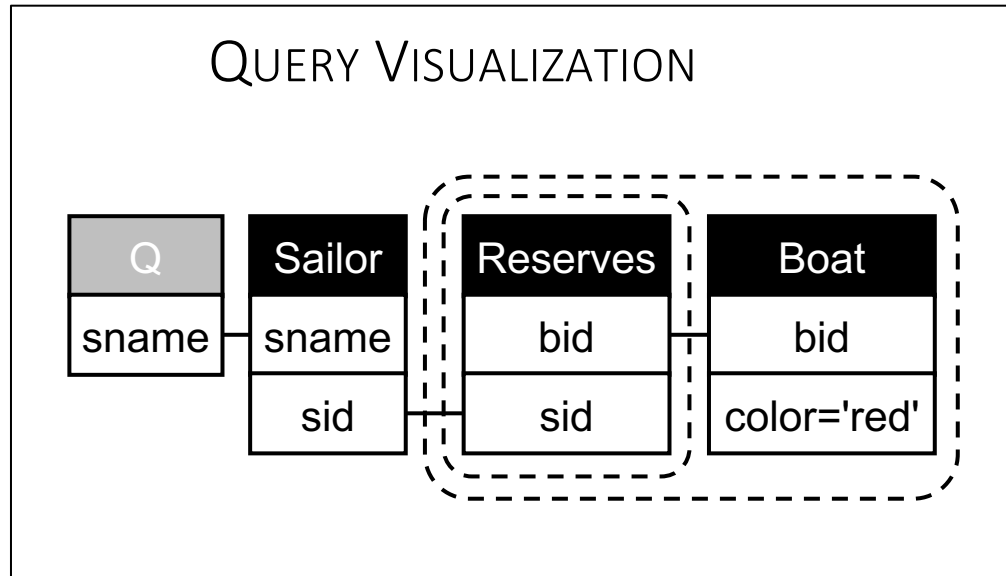
(Do you mean companies with headquarter or office in Utrecht?) ?

*Q: Find me companies in Utrecht.*

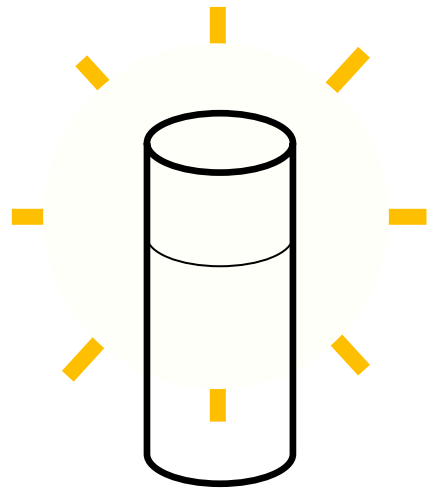
*A: Company D, Company E, Company F*



# 1. How do you know your voice assistant understood you correctly?

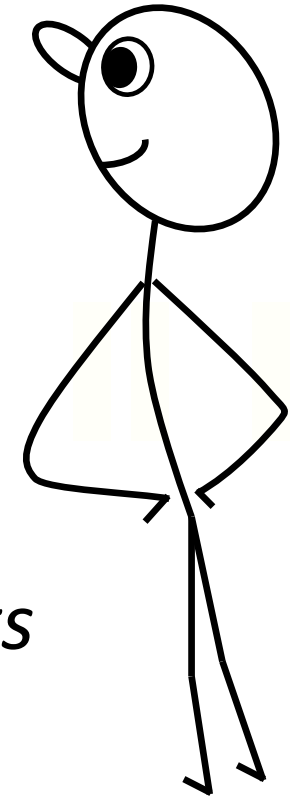


Can a diagrammatic representation of the query help the user quickly "debug" its translation, i.e. check it was understood correctly?



This will be our running example (for didactic reasons)

*Q: Find sailors who reserved all red boats*



# 2. Query Debugging of Student-Submitted Homeworks

Reference solution:

```
select distinct S1.beer, S1.bar
from Likes L, Serves S1
where L.drinker = 'Eve'
and L.beer = S1.beer
and not exists
  (select *
   from Serves S2
   where S2.beer = S1.beer
   and S2.price > S1.price)
```

Homework problem:

Q1: For each beer that Eve likes, find the bar serving it at the highest price.

As TA you need to decide what is wrong with this query:

```
select distinct S1.beer, S1.bar
from Likes L, Serves S1, Serves S2
where L.drinker = 'Eve'
and L.beer = S1.beer
and S1.beer = S2.beer
and S1.price > S2.price
```



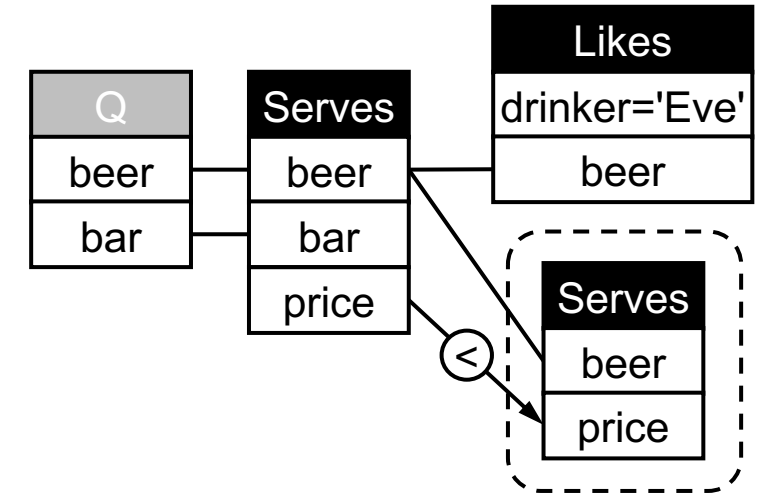
# 2. Query Debugging of Student-Submitted Homeworks

Reference solution:

```
select distinct S1.beer, S1.bar
from Likes L, Serves S1
where L.drinker = 'Eve'
and L.beer = S1.beer
and not exists
  (select *
   from Serves S2
   where S2.beer = S1.beer
   and S2.price > S1.price)
```

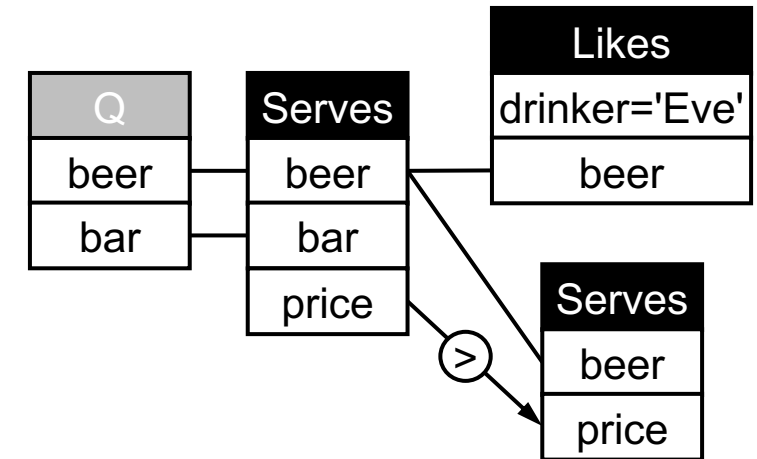
Homework problem:

Q1: For each beer that Eve likes, find the bar serving it at the highest price.



As TA you need to decide what is wrong with this query:

```
select distinct S1.beer, S1.bar
from Likes L, Serves S1, Serves S2
where L.drinker = 'Eve'
and L.beer = S1.beer
and S1.beer = S2.beer
and S1.price > S2.price
```



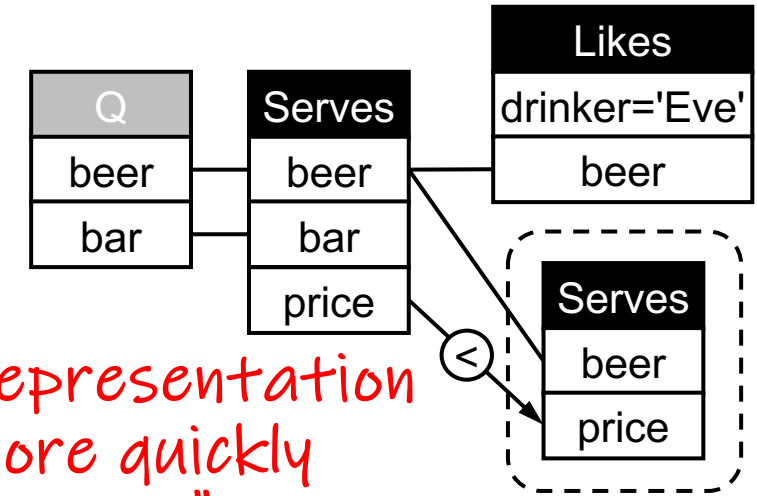
# 2. Query Debugging of Student-Submitted Homeworks

Reference solution:

```
select distinct S1.beer, S1.bar
from Likes L, Serves S1
where L.drinker = 'Eve'
and L.beer = S1.beer
and not exists
  (select *
   from Serves S2
   where S2.beer = S1.beer
   and S2.price > S1.price)
```

Homework problem:

Q1: For each beer that Eve likes, find the bar serving it at the highest price.

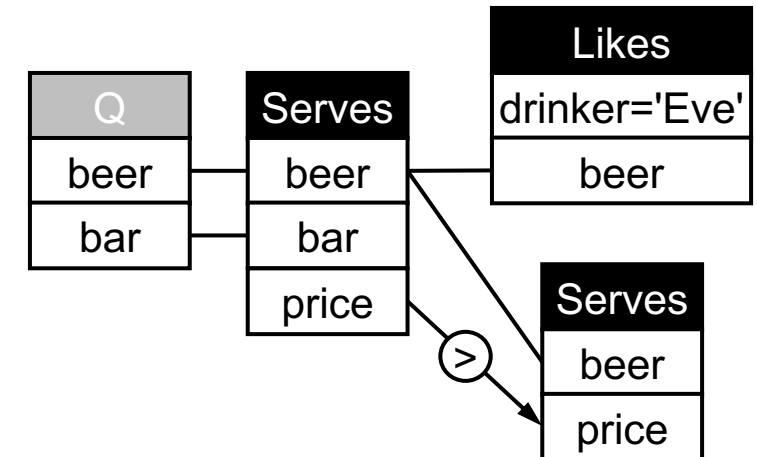


Again: Can a diagrammatic representation of the query help the user more quickly understand its intent, its "pattern"?

As TA you need to decide what is wrong with this query:

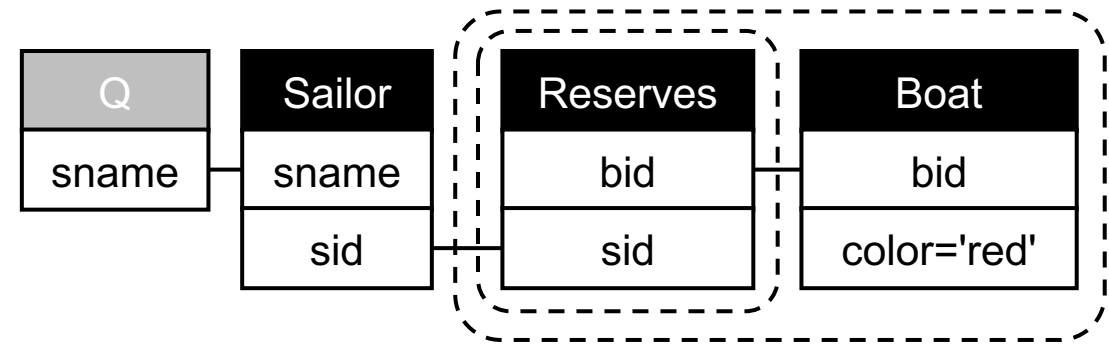
```
select distinct S1.beer, S1.bar
from Likes L, Serves S1, Serves S2
where L.drinker = 'Eve'
and L.beer = S1.beer
and S1.beer = S2.beer
and S1.price > S2.price
```

Q2: For each beer that Eve likes, find the bar not serving it at the lowest price.



### 3. Browsing & understanding existing Queries

```
select distinct S.sname
from Sailor S
where not exists
  (select B.bid
   from Boat B
   where color='red'
   and not exists
     (select R.bid
      from Reserves R
      where R.bid = B.bid
      and R.sid = S.sid))
```

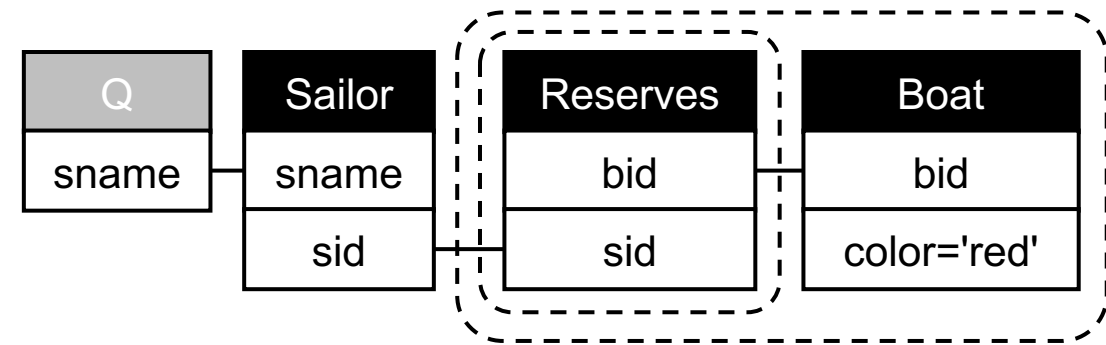


Query Intent: ?



### 3. Browsing & understanding existing Queries

```
select distinct S.sname
from Sailor S
where not exists
  (select B.bid
   from Boat B
   where color='red'
   and not exists
     (select R.bid
      from Reserves R
      where R.bid = B.bid
      and R.sid = S.sid))
```

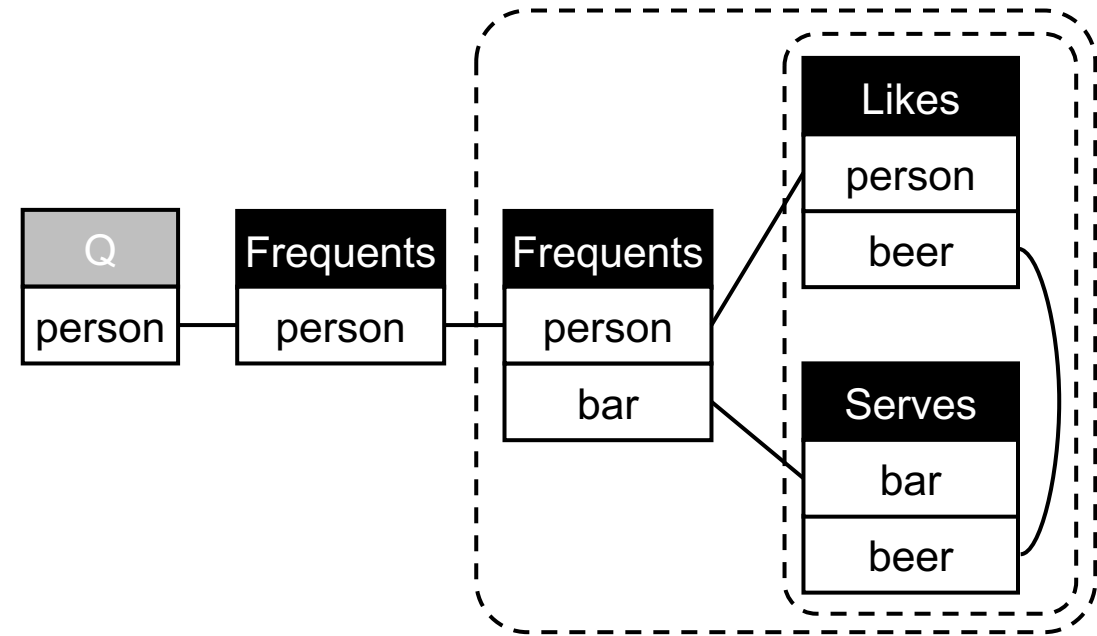


Query Intent: "Find persons who reserved all red boats."

### 3. Browsing & understanding existing Queries

2 2

```
select distinct F1.person
from Frequents F1
where not exists
  (select F2.bar
   from Frequents F2
   where F2.person = F1.person
   and not exists
     (select S3.drink
      from Serves S3, Likes L4
      where L4.person = F2.person
      and L4.drink = S3.drink
      and S3.bar = F2.bar))
```



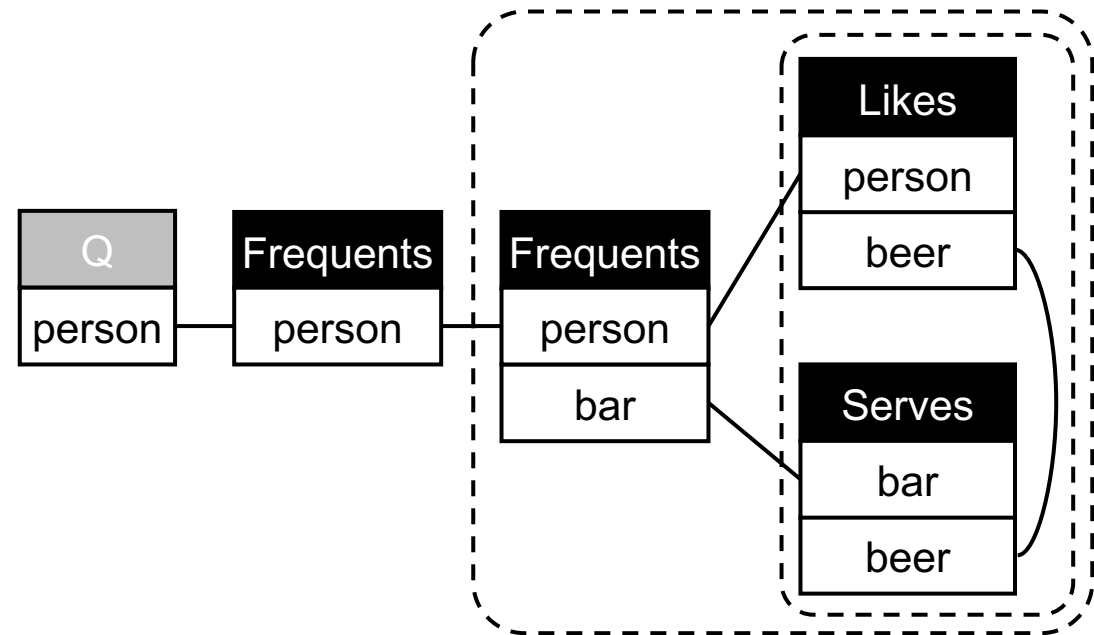
Query Intent: ?

### 3. Browsing & understanding existing Queries

2

```
select distinct F1.person
from Frequents F1
where not exists
  (select F2.bar
   from Frequents F2
   where F2.person = F1.person
   and not exists
     (select S3.drink
      from Serves S3, Likes L4
      where L4.person = F2.person
      and L4.drink = S3.drink
      and S3.bar = F2.bar))
```

2



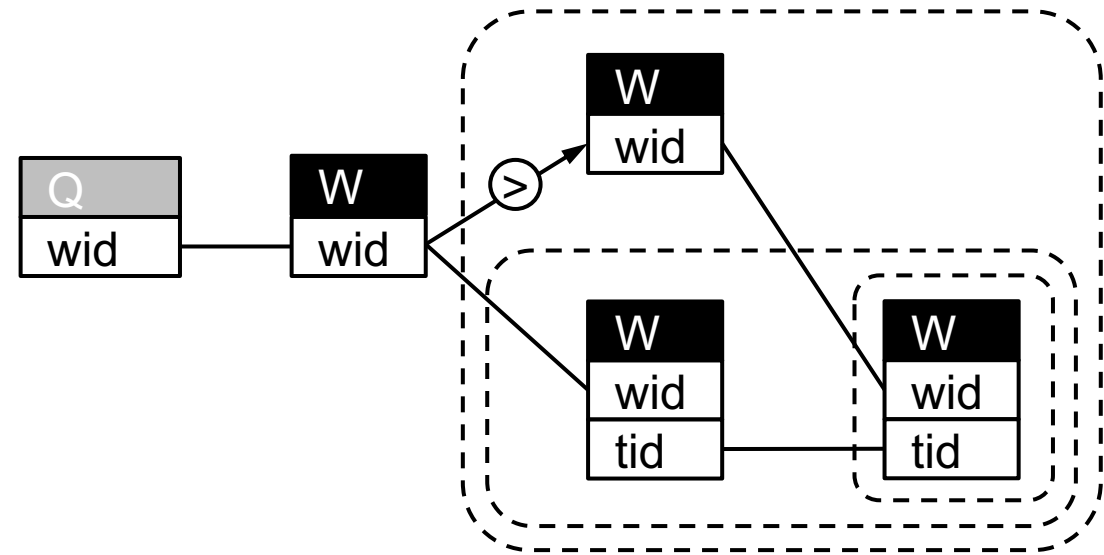
Query Intent: "Find persons who frequent only bars that serve some beer they like."

### 3. Browsing & understanding existing Queries

```
select distinct W1.wid
from Worlds W1
where not exists
  (select *
   from Worlds W2
   where W2.wid < W1.wid
   and not exists
     (select *
      from Worlds W3
      where W3.wid = W1.wid
      and not exists
        (select *
         from Worlds W4
         where W4.wid = W2.wid
         and W4.tid = W3.tid))))
```

3

3



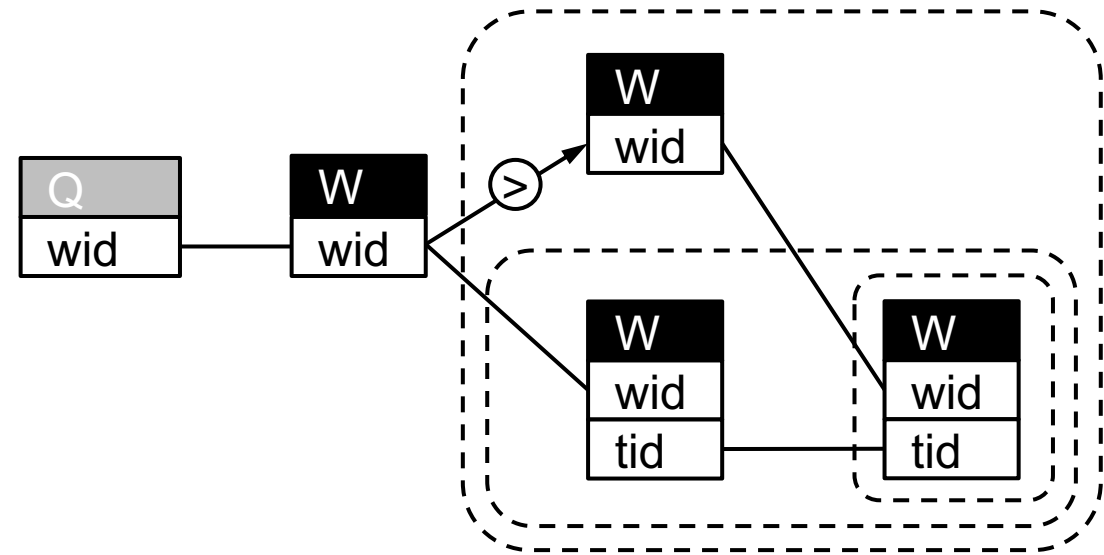
Query Intent: ?

### 3. Browsing & understanding existing Queries

```
select distinct W1.wid
from Worlds W1
where not exists
  (select *
   from Worlds W2
   where W2.wid < W1.wid
   and not exists
     (select *
      from Worlds W3
      where W3.wid = W1.wid
      and not exists
        (select *
         from Worlds W4
         where W4.wid = W2.wid
         and W4.tid = W3.tid))))
```

3

3

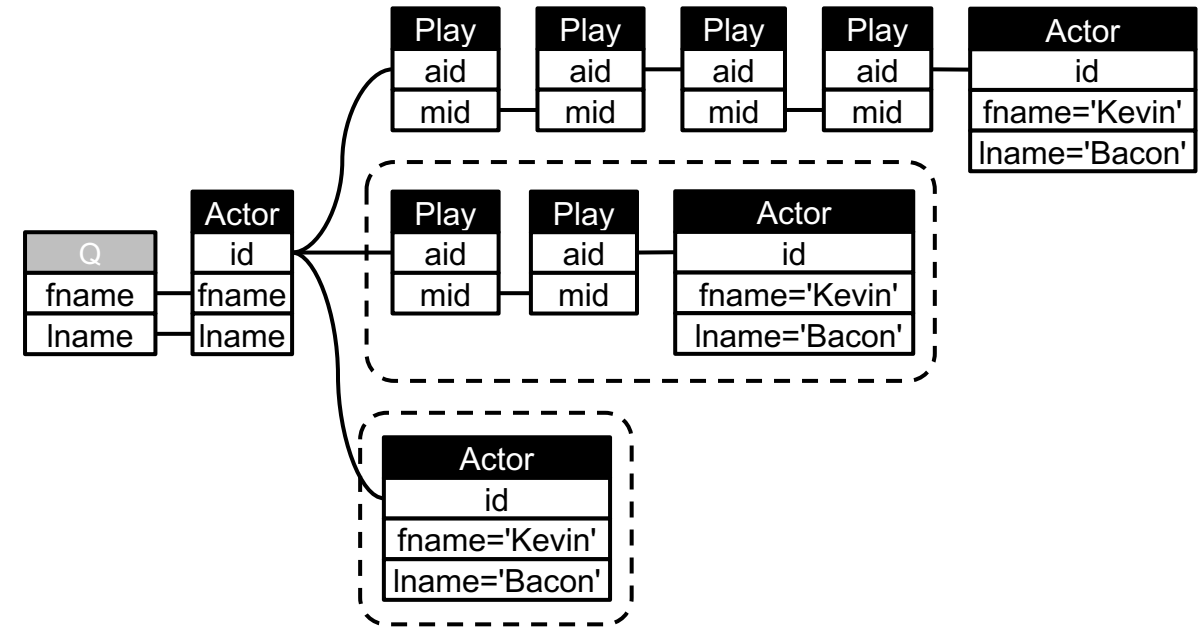


Query Intent: "Find worlds for which no earlier world contains all its tuples"

### 3. Browsing & understanding existing Queries

4

```
select distinct a5.fname, a5.lname
from Actor a0, Play p1, Play p2, Play p3,
     Play p4, Actor a5
where a0.fname = 'Kevin' and a0.lname = 'Bacon'
and a0.id = p1.aid and p1.mid = p2.mid
and p2.aid = p3.aid and p3.mid = p4.mid
and p4.aid = a5.id
and not exists (select *
from Actor a6, Play p7, Play p8
where a6.fname = 'Kevin' and a6.lname = 'Bacon'
and a6.id = p7.aid and p7.mid = p8.mid
and p8.aid = a5.id)
and not exists (select *
from Actor a9
where a9.fname = 'Kevin' and a9.lname = 'Bacon'
and a9.id = a5.id)
```

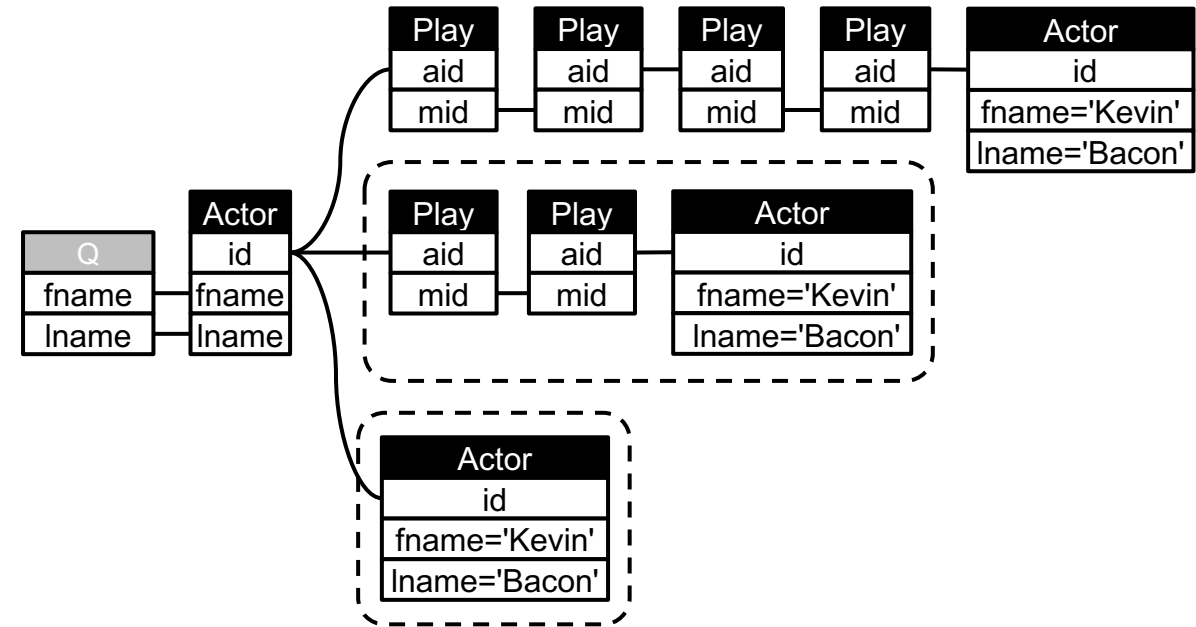


Query Intent: ?

### 3. Browsing & understanding existing Queries

4

```
select distinct a5.fname, a5.lname
from Actor a0, Play p1, Play p2, Play p3,
     Play p4, Actor a5
where a0.fname = 'Kevin' and a0.lname = 'Bacon'
and a0.id = p1.aid and p1.mid = p2.mid
and p2.aid = p3.aid and p3.mid = p4.mid
and p4.aid = a5.id
and not exists (select *
                from Actor a6, Play p7, Play p8
                where a6.fname = 'Kevin' and a6.lname = 'Bacon'
                and a6.id = p7.aid and p7.mid = p8.mid
                and p8.aid = a5.id)
and not exists (select *
                from Actor a9
                where a9.fname = 'Kevin' and a9.lname = 'Bacon'
                and a9.id = a5.id)
```



Query Intent: "Find actors with Bacon number 2."

# Why logical diagrams [Gardner'58]

Figure 42 introduces the notational symbols that will be used throughout this book for all binary (two-term) truth-value relations for which there are commonly used symbols. The diagram for each relation is shown on the left. On the right is the “negative” diagram for the negation of each relation.

To apply these diagrams to relations between  $B$  and  $C$ , we have only to rotate the page until the  $A$  and  $B$  circles correspond to the positions of the  $B$  and  $C$  circles. In the same way we can turn the page to bring the  $A$  and  $B$  circles to the positions of  $C$  and  $A$ . After we work with the diagrams for a while, the patterns are soon memorized and problems involving no more than three terms can be solved with great speed. After a time, elementary problems of this sort can even be solved in the head. One has only to form a mental picture of the circles, then perform on them the necessary shadings. Both Venn and Carroll, incidentally, wrote of the ease with which they learned to solve logic problems mentally by their respective methods, just as an expert abacus operator can move the beads in a mental image of an abacus, or a chess master can play a game of chess blindfolded. Using the circles mentally is, of course, much easier than blindfold chess or abacus operation.

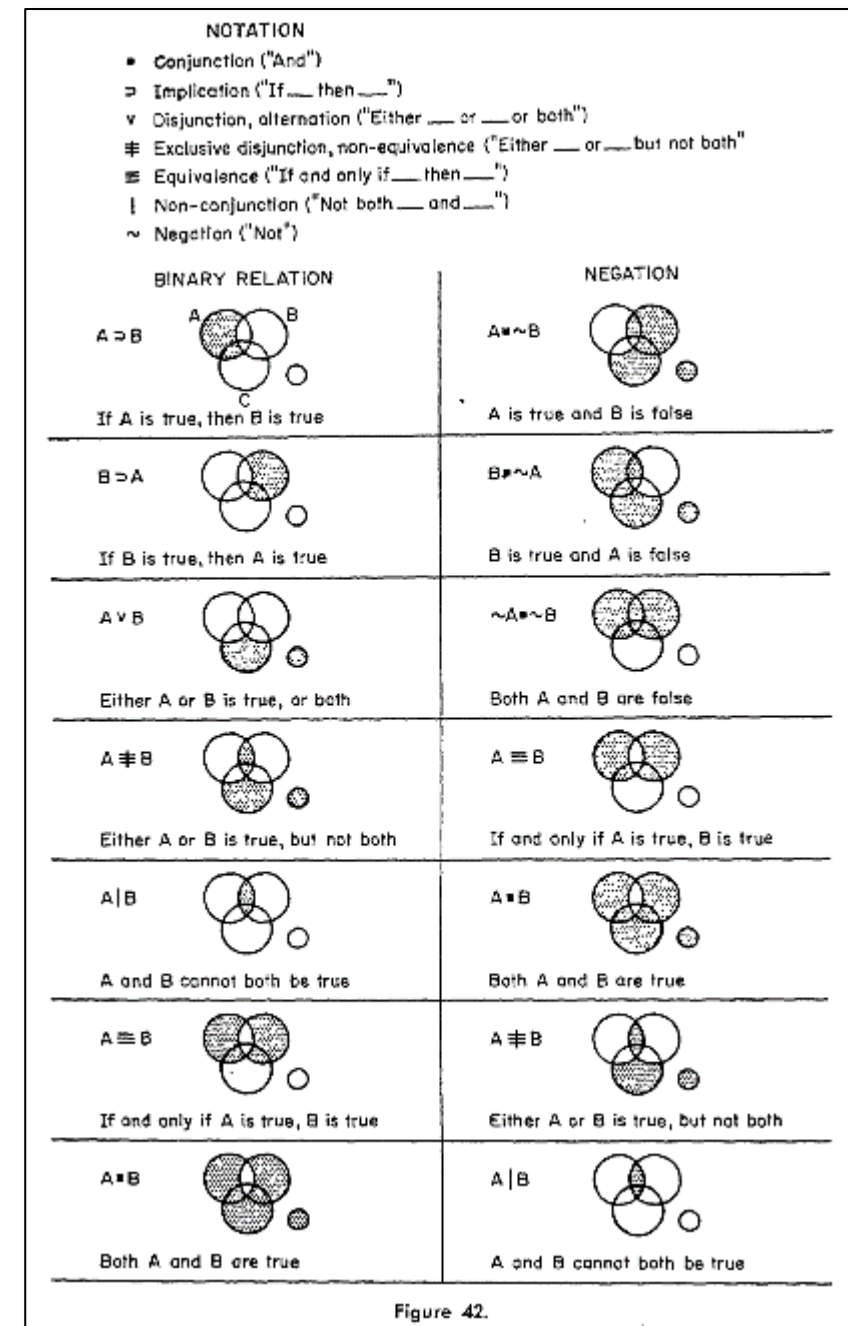


Figure 42.



# 4. Patterns

Sailor (sid, sname, rating, bdate)  
Reserves (sid, bid, day)  
Boat (bid, bname, color, pdate)

	some	not any	not all	all
Sailors renting boats	have reserved some red boat	have not reserved any red boat	reserved not all red boats	reserved all red boats

# 4. Patterns

Student (sid, sname)  
Takes (sid, cid, semester)  
Course (cid, cname, depart)

Sailor (sid, sname, rating, bdate)  
Reserves (sid, bid, day)  
Boat (bid, bname, color, pdate)

	some	not any	not all	all
Sailors renting boats	have reserved some red boat	have not reserved any red boat	reserved not all red boats	reserved all red boats
Students taking classes	took some art class	took no art class	took not all art classes	took all art classes

# 4. Patterns

Actor (id, lname)  
Play (aid, mid, role)  
Movie (id, name, dir)

Student (sid, sname)  
Takes (sid, cid, semester)  
Course (cid, cname, depart)

Sailor (sid, sname, rating, bdate)  
Reserves (sid, bid, day)  
Boat (bid, bname, color, pdate)

	some	not any	not all	all
Sailors renting boats	have reserved some red boat	have not reserved any red boat	reserved not all red boats	reserved all red boats
Students taking classes	took some art class	took no art class	took not all art classes	took all art classes
Actors playing in movies	played in some Hitchcock movie	did not play in a Hitchcock movie	played not in all Hitchcock movies	played in all Hitchcock movies

# 4. Patterns

Actor (id, lname)  
 Play (aid, mid, role)  
 Movie (id, name, dir)

Student (sid, sname)  
 Takes (sid, cid, semester)  
 Course (cid, cname, depart)

Sailor (sid, sname, rating, bdate)  
 Reserves (sid, bid, day)  
 Boat (bid, bname, color, pdate)

	some	not any	not all	all
Sailors	<pre>SELECT DISTINCT S.sname FROM Sailor S WHERE EXISTS(   SELECT *   FROM Reserves R   WHERE R.sid = S.sid   AND EXISTS(     SELECT *     FROM Boat B     WHERE B.color = 'red'     AND B.bid = R.bid))</pre>	<pre>SELECT DISTINCT S.sname FROM Sailor S WHERE EXISTS(   SELECT *   FROM Boat B   WHERE B.color = 'red'   AND NOT EXISTS(     SELECT *     FROM Reserves R     WHERE R.bid = B.bid     AND R.sid = S.sid))</pre>	<pre>SELECT DISTINCT S.sname FROM Sailor S WHERE NOT EXISTS(   SELECT *   FROM Reserves R   WHERE R.sid = S.sid   AND EXISTS(     SELECT *     FROM Boat B     WHERE B.color = 'red'     AND B.bid = R.bid))</pre>	<pre>SELECT DISTINCT S.sname FROM Sailor S WHERE NOT EXISTS(   SELECT *   FROM Boat B   WHERE B.color = 'red'   AND NOT EXISTS(     SELECT *     FROM Reserves R     WHERE R.bid = B.bid     AND R.sid = S.sid))</pre>
Students	<pre>SELECT DISTINCT S.sname FROM Student S WHERE EXISTS(   SELECT *   FROM Takes T   WHERE T.sid = S.sid   AND EXISTS(     SELECT *     FROM Class C     WHERE C.depart = 'art'     AND C.cid = T.cid))</pre>	<pre>SELECT DISTINCT S.sname FROM Student S WHERE EXISTS(   SELECT *   FROM Class C   WHERE C.depart = 'art'   AND NOT EXISTS(     SELECT *     FROM Takes T     WHERE T.cid = C.cid     AND T.sid = S.sid))</pre>	<pre>SELECT DISTINCT S.sname FROM Student S WHERE NOT EXISTS(   SELECT *   FROM Takes T   WHERE T.sid = S.sid   AND EXISTS(     SELECT *     FROM Class C     WHERE C.depart = 'art'     AND C.cid = T.cid))</pre>	<pre>SELECT DISTINCT S.sname FROM Student S WHERE NOT EXISTS(   SELECT *   FROM Class C   WHERE C.depart = 'art'   AND NOT EXISTS(     SELECT *     FROM Takes T     WHERE T.cid = C.cid     AND T.sid = S.sid))</pre>
Actors	<pre>SELECT DISTINCT A.lname FROM Actor A WHERE EXISTS(   SELECT *   FROM Play P   WHERE P.aid = A.aid   AND EXISTS(     SELECT *     FROM Movie M     WHERE M.dir = 'Hitchcock'     AND M.id = P.mid))</pre>	<pre>SELECT DISTINCT A.lname FROM Actor A WHERE EXISTS(   SELECT *   FROM Movie M   WHERE M.dir = 'Hitchcock'   AND NOT EXISTS(     SELECT *     FROM Play P     WHERE P.mid = M.id     AND P.aid = A.aid))</pre>	<pre>SELECT DISTINCT A.lname FROM Actor A WHERE NOT EXISTS(   SELECT *   FROM Play P   WHERE P.aid = A.aid   AND EXISTS(     SELECT *     FROM Movie M     WHERE M.dir = 'Hitchcock'     AND M.id = P.mid))</pre>	<pre>SELECT DISTINCT A.lname FROM Actor A WHERE NOT EXISTS(   SELECT *   FROM Movie M   WHERE M.dir = 'Hitchcock'   AND NOT EXISTS(     SELECT *     FROM Play P     WHERE P.mid = M.id     AND P.aid = A.aid))</pre>

# 4. Patterns

Actor (id, lname)  
Play (aid, mid, role)  
Movie (id, name, dir)

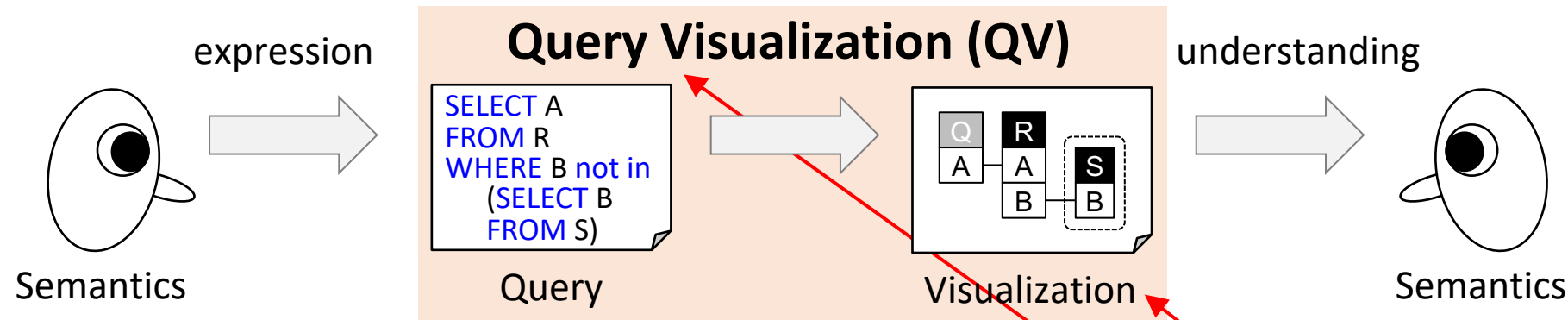
Student (sid, sname)  
Takes (sid, cid, semester)  
Course (cid, cname, depart)

Sailor (sid, sname, rating, bdate)  
Reserves (sid, bid, day)  
Boat (bid, bname, color, pdate)

	some	not any	not all	all
Sailors				
Students				
Actors				

Don't we already have  
visual query languages, and  
interactive query builders?

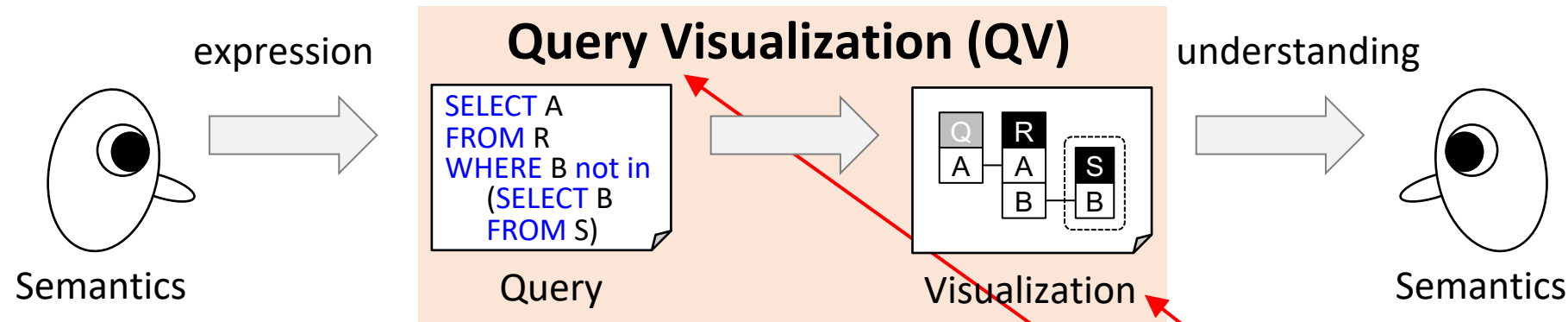
# "Query Visualization" (for understanding) $\neq$ "Visual Query Languages" (for composition)



also: "query diagram"

also: "query diagramming"

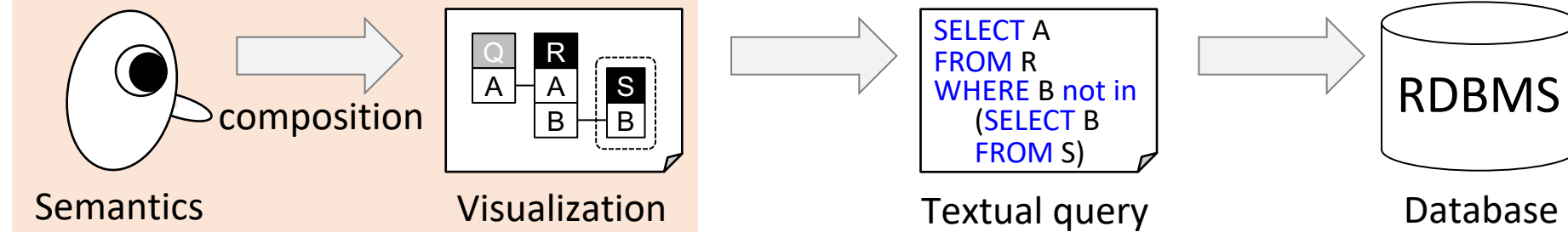
# "Query Visualization" (for understanding) ≠ "Visual Query Languages" (for composition)



also: "query diagram"

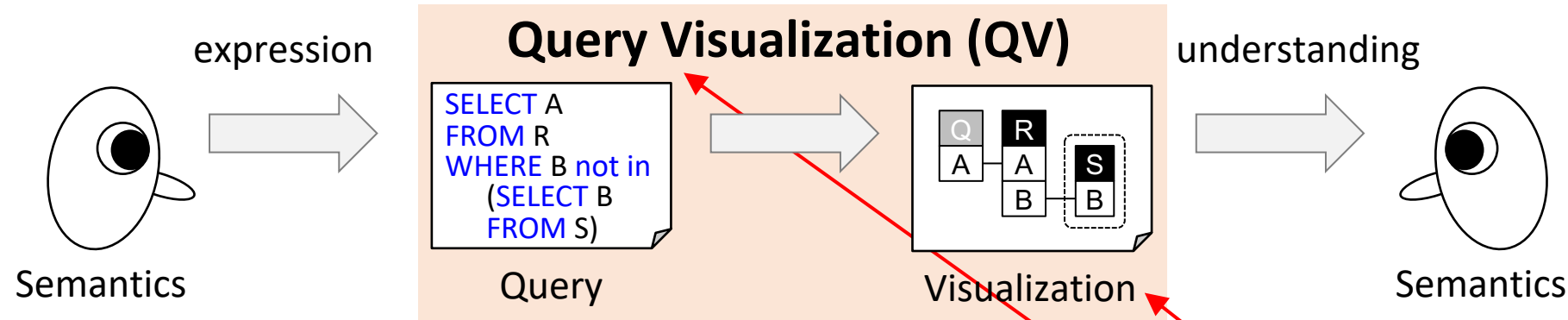
also: "query diagramming"

## Visual Query Languages (VQL)





# "Query Visualization" (for understanding) ≠ "Visual Query Languages" (for composition)

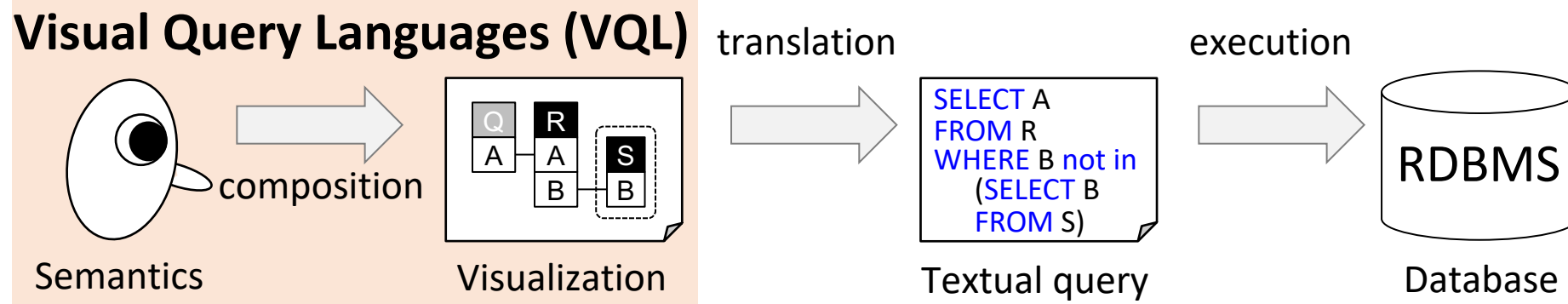


A visual query representation is for: query understanding / explanation / debugging

Both applications use "visual representations",  
but different objectives lead to different criteria!

also: "query diagram"

also: "query diagramming"

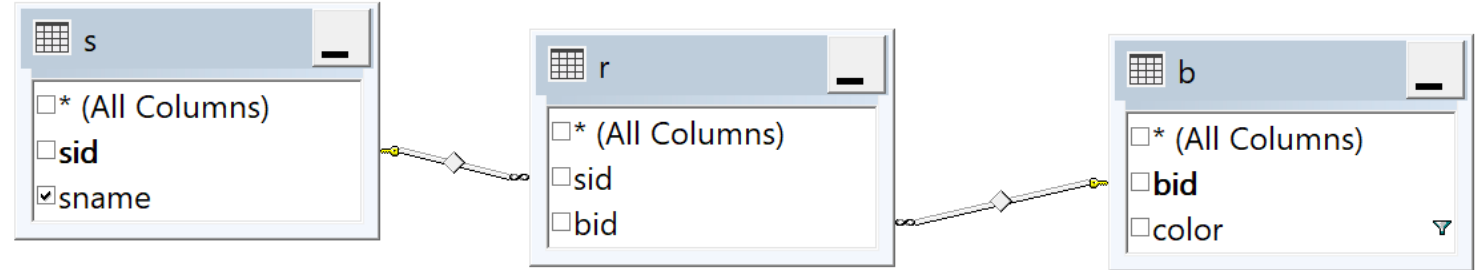


A visual query representation is used for: query writing /composition

# What about visual active query builders? Say SSMS?

Q2: "Find sailors who reserved a red boat."

```
select S.sname
from Sailor s, Reserves r, Boat b
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

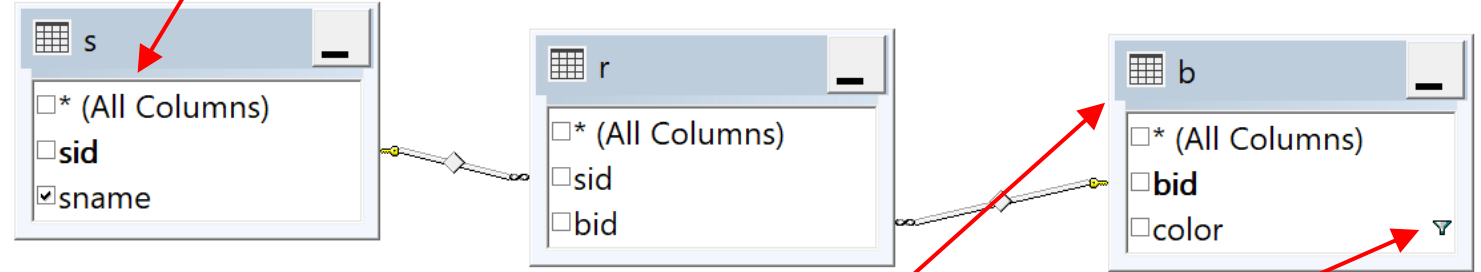


# What about visual active query builders? Say SSMS?

Q2: "Find sailors who reserved a red boat."

```
select S.sname
from Sailor s, Reserves r, Boat b
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Visual elements that are relevant for composition but not understanding



Other important information is not shown (e.g. the filter symbol hides actual predicate)

Additional window reveals selection predicate

The screenshot shows the 'Filter' tab in the SQL Server Enterprise Manager. It displays a table with columns: Column, Alias, Table, Output, Sort Type, Sort Order, Filter, and Or. The 'color' column is selected, and its filter is shown as '= 'red''.

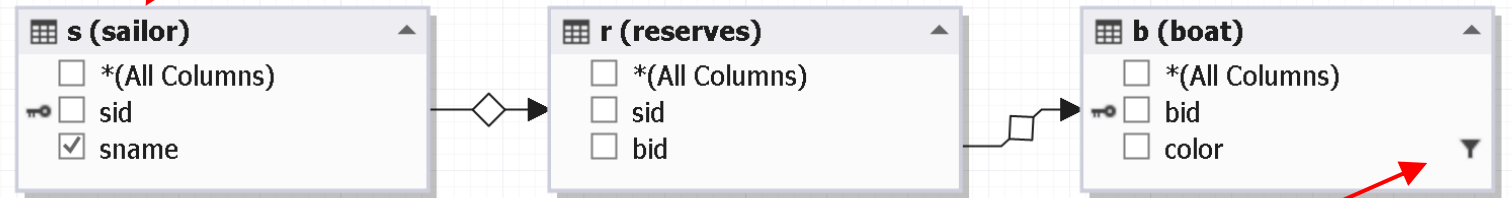
Column	Alias	Table	Output	Sort Type	Sort Order	Filter	Or
color		b	<input type="checkbox"/>			= 'red'	
sname		s	<input checked="" type="checkbox"/>				

# What about visual active query builders? Or dbForge?

Q2: "Find sailors who reserved a red boat."

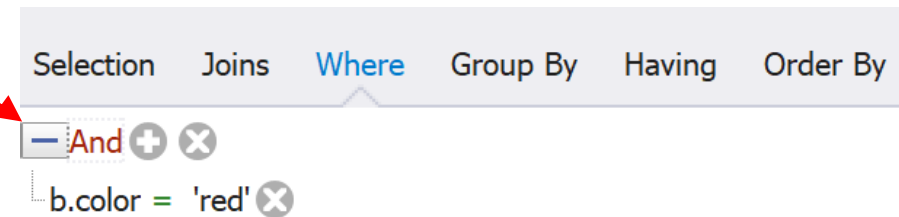
```
select S.sname
from Sailor s, Reserves r, Boat b
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Unnecessary visual elements shown that are relevant for composition but not understanding



Other important information is not shown (e.g. the filter symbol hides actual predicate)

Additional window reveals selection predicate

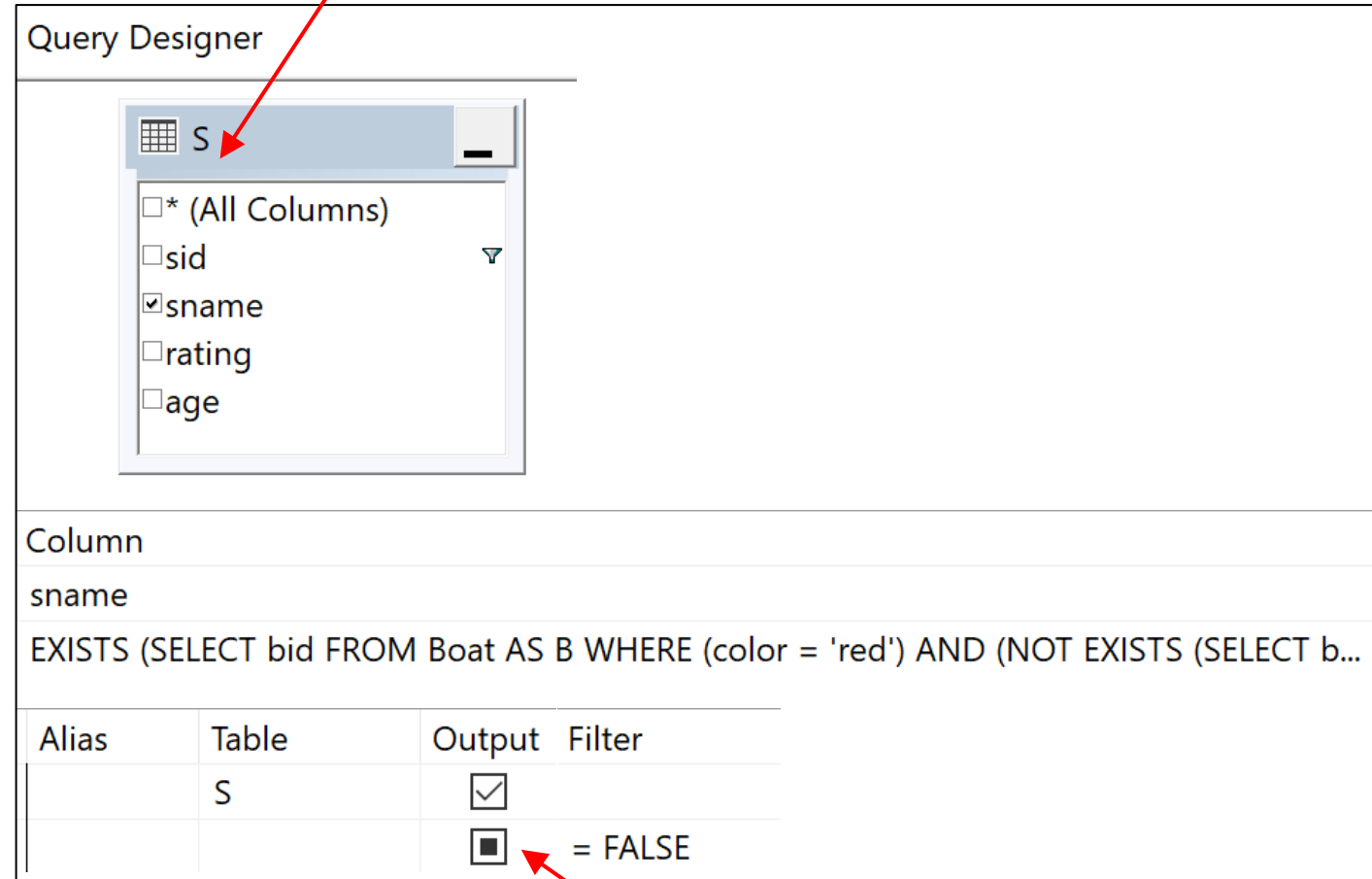


# What about visual active query builders? Back to SSMS...

Q4: "Find sailors who reserved all red boats."

```
select S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

SSMS does not render the nested blocks



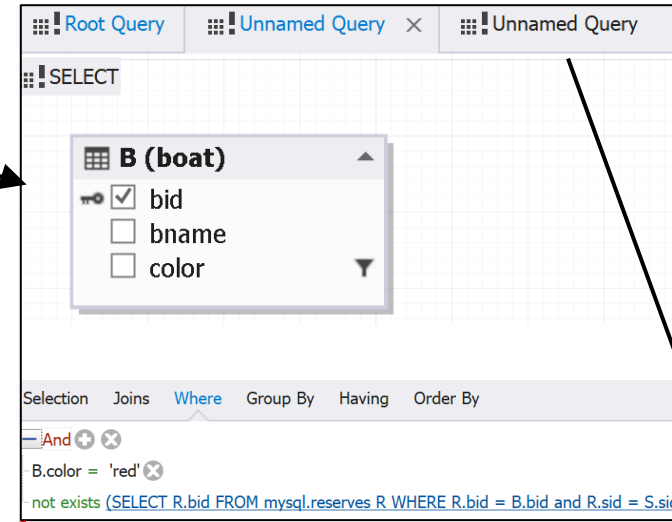
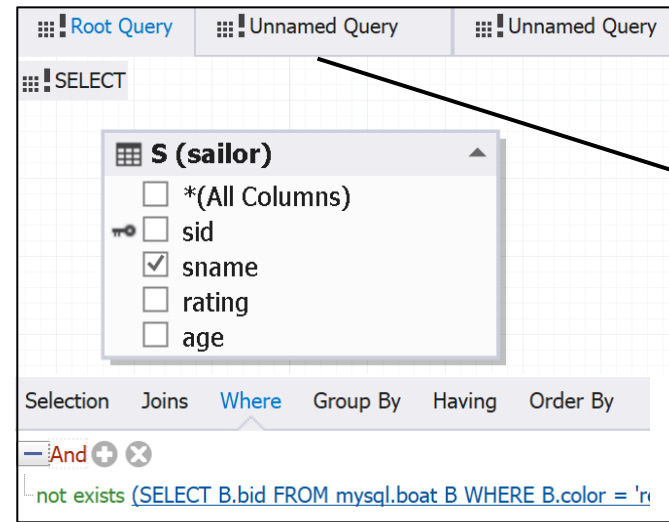
"Not exists" is treated as an expression with a "false" value in the filter

# What about visual active query builders? dbForge...

Q4: "Find sailors who reserved all red boats."

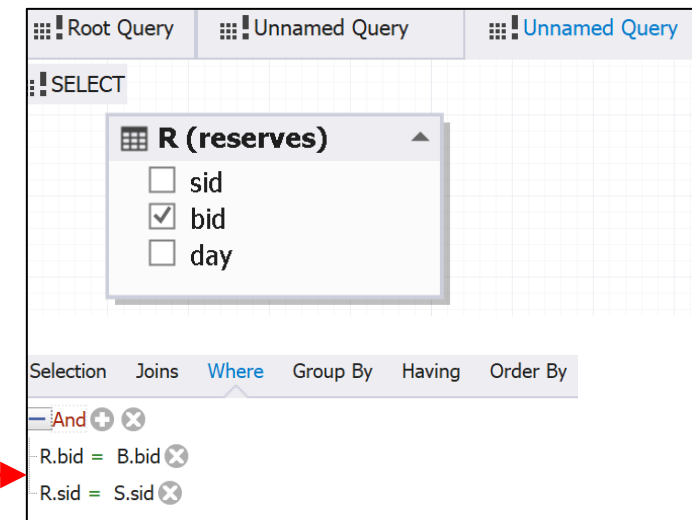
```
select S.sname
from Sailor S
where not exists
(select *
from Boat B
where color = 'red'
and not exists
(select *
from Reserves R
where S.sid=R.sid
and R.bid=B.bid))
```

Individual query blocks shown in separate windows



dbForge does not use 'Expression' + 'Criteria' to represent 'NOT' + 'EXISTS'. It directly shows 'Not Exists' as a part of 'Where' clause

dbForge keeps join conditions in WHERE clause as an expression



DEFINITION (**Query Visualization**): The term “query visualization” refers to both

- i. a graphical representation of a query and  
*(alternatively: "query diagram")*
- ii. the process of transforming a given query into a graphical representation.

*(alternatively: "query diagramming")*

The goal of query visualization is to help users more quickly understand the intent of a query, as well as its relational query pattern.

# Intended Agenda today

Please leave  
feedback 😊



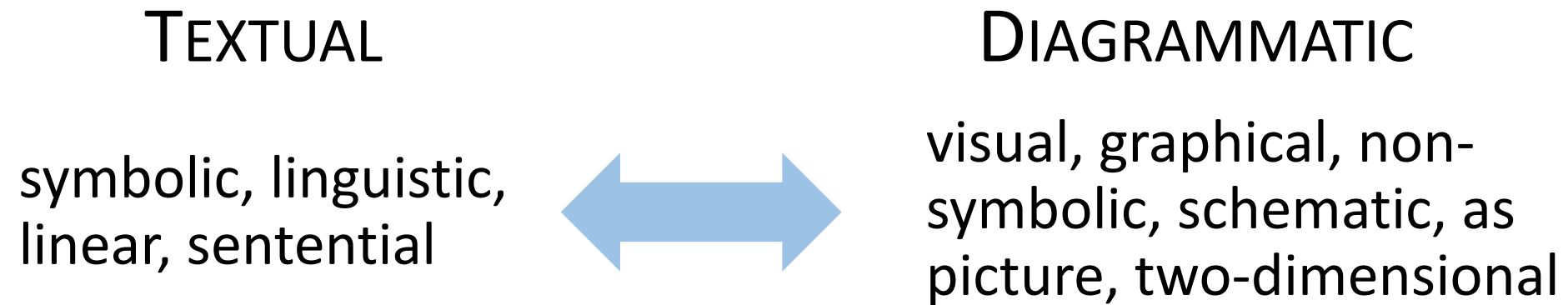
1. Why visualizing queries and why now?
2. Principles of Query Visualization
3. Logical foundations of relational query languages
4. (Early) Diagrammatic representations
5. Visual Query Representations (from DB community)
6. Lessons Learned and Open Challenges



What does it mean for  
a QL to be "visual"?

# What is actually a "visual" representation?

- Many attempts on defining an exact notion of "visual" (it's *not easy*)
- In general, authorities acknowledge a spectrum between TEXT and DIAGRAMS



The exact boundary b/w text and "visual" is not clear-cut!  
(And as we will see, "visual" gets interpreted very differently)  
Next: We try to develop an intuition for "practical visualization"

# Let's explore the boundary between text and diagram

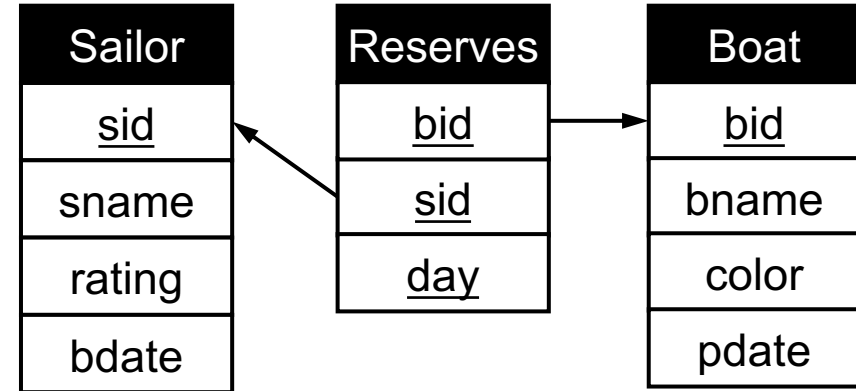
Sailor(sid, sname, rating, bdate)

Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)

FK Reserves.sid references Sailor

FK Reserves.bid references Boat



UML diagram of  
relational schema.

# Let's explore the boundary between text and diagram

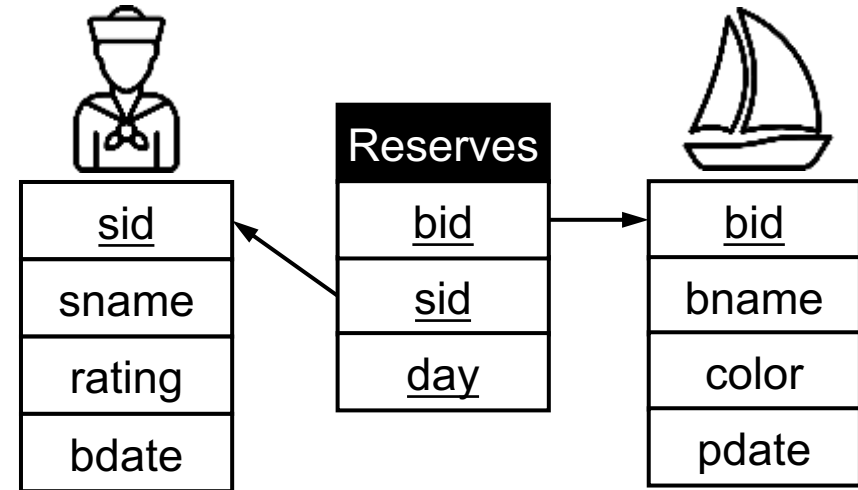
Sailor(sid, sname, rating, bdate)

Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)

FK Reserves.sid references Sailor

FK Reserves.bid references Boat



UML diagram of  
relational schema.

But no need for icons!

# Let's explore the boundary between text and diagram

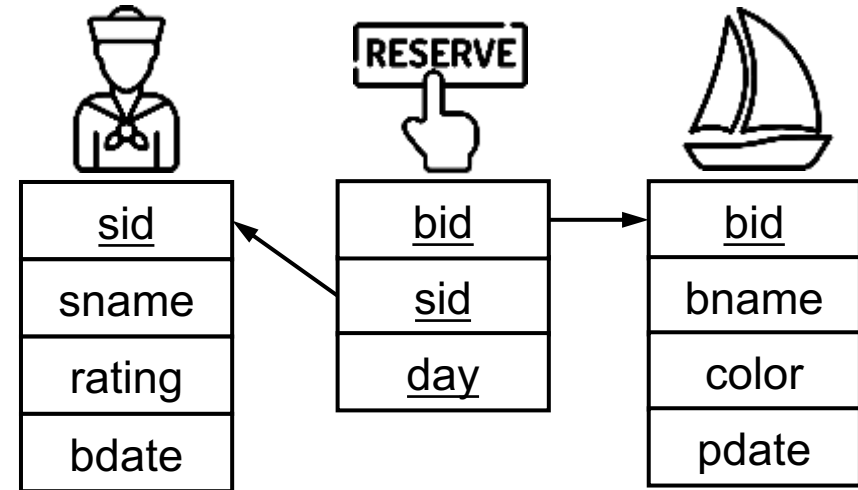
Sailor(sid, sname, rating, bdate)

Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)

FK Reserves.sid references Sailor

FK Reserves.bid references Boat



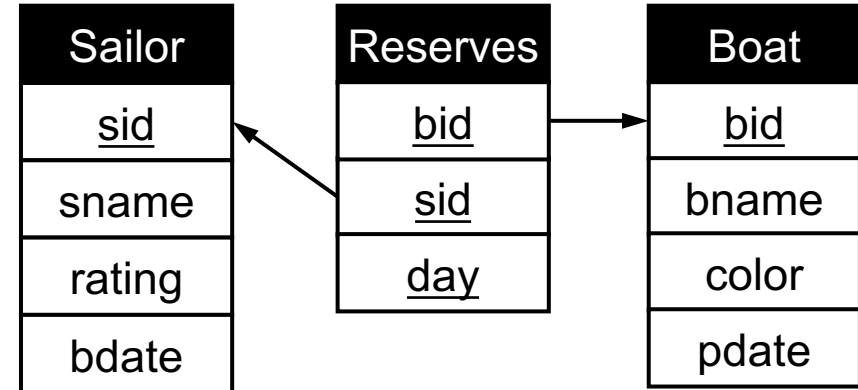
UML diagram of  
relational schema.

But no need for icons!  
(Actually which icons?)

# Let's explore the boundary between text and diagram

Sailor(sid, sname, rating, bdate)  
Reserves(sid, bid, day)  
Boat(bid, bname, color, pdate)

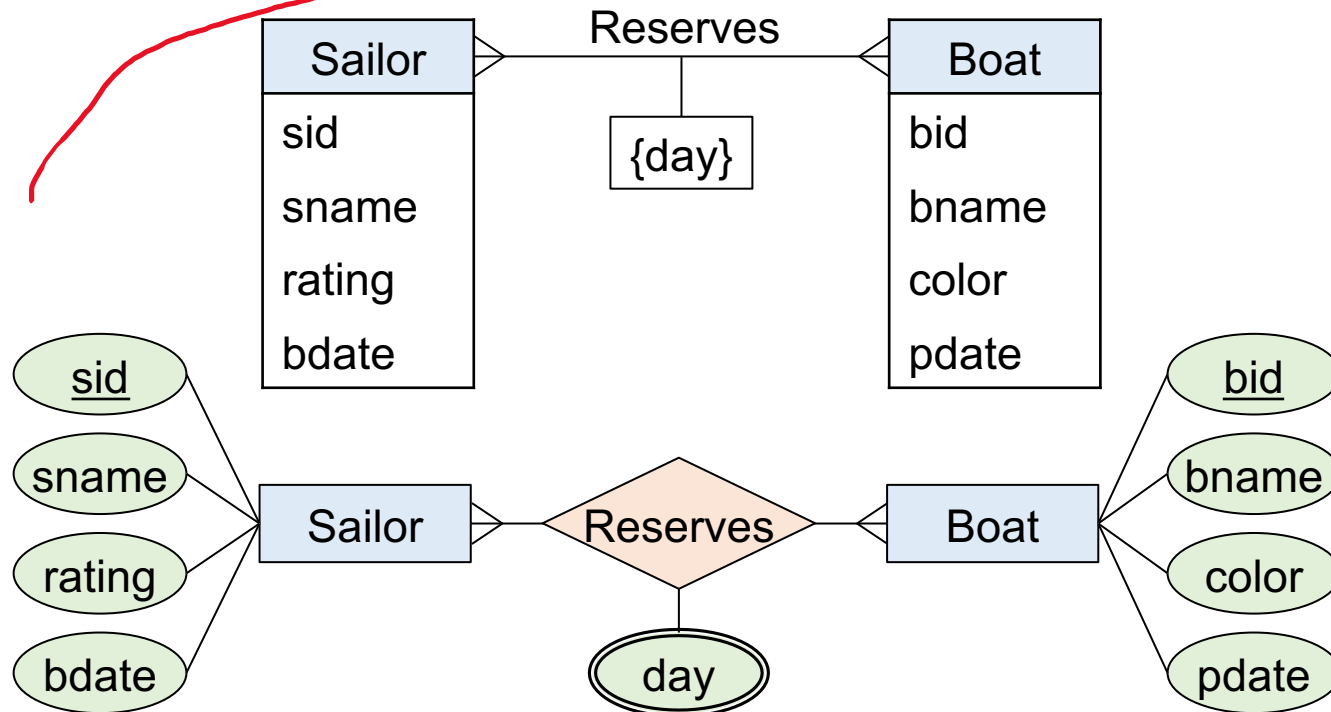
FK Reserves.sid references Sailor  
FK Reserves.bid references Boat



UML diagram of  
relational schema.

But no need for icons!  
(Actually which icons?)

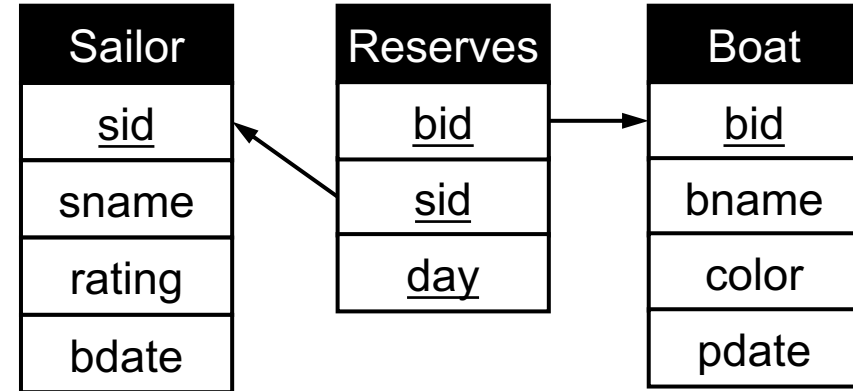
ER diagrams also use text



# Text vs diagrammatic representations

Sailor(sid, sname, rating, bdate)  
Reserves(sid, bid, day)  
Boat(bid, bname, color, pdate)

FK Reserves.sid references Sailor  
FK Reserves.bid references Boat



## Observations:

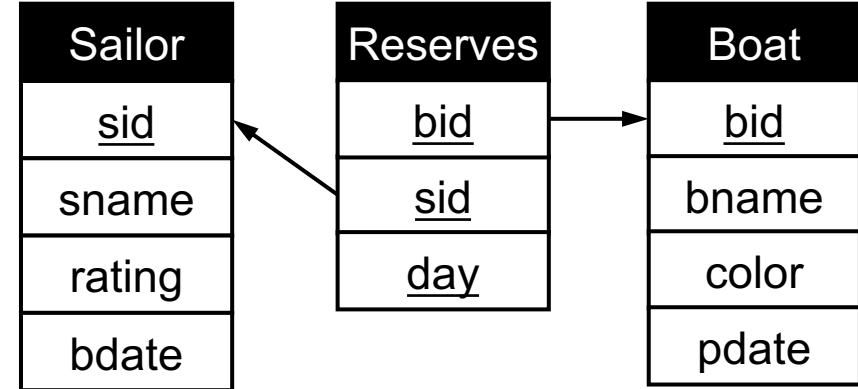
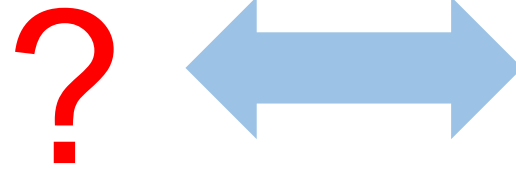
1. We prefer text as names/labels for atomic elements (tables, attributes)
2. We prefer to "visualize" relationships (the "structure") between these elements.

# Text vs diagrammatic representations

Sailor(sid, sname, rating, bdate)

Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)

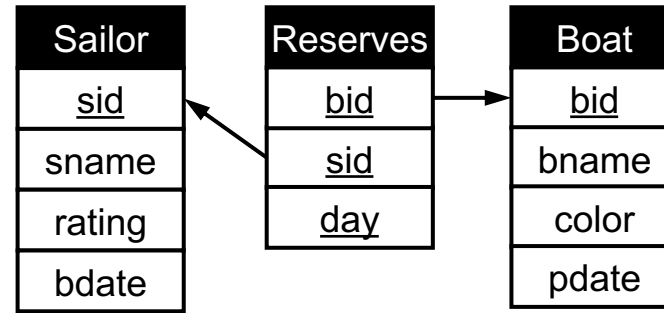


*Observations:*

- 1. We prefer text as names/labels for atomic elements (tables, attributes)*
- 2. We prefer to "visualize" relationships (the "structure") between these elements.*



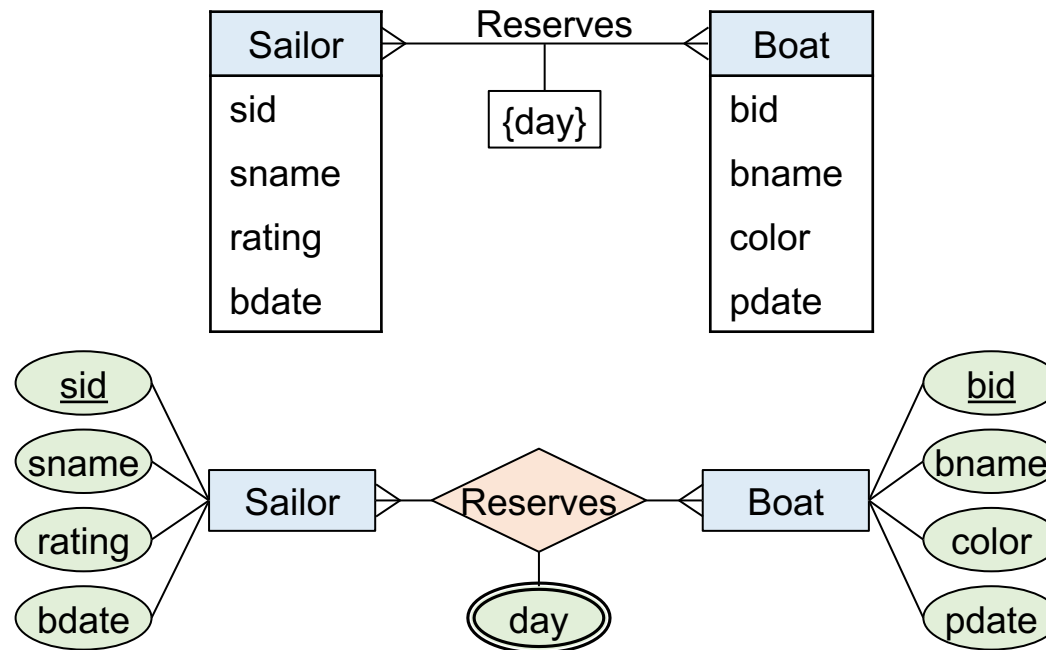
# There seems to be a sweet spot for visualizing relations



Sailor(sid, sname, rating, bdate)

Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)

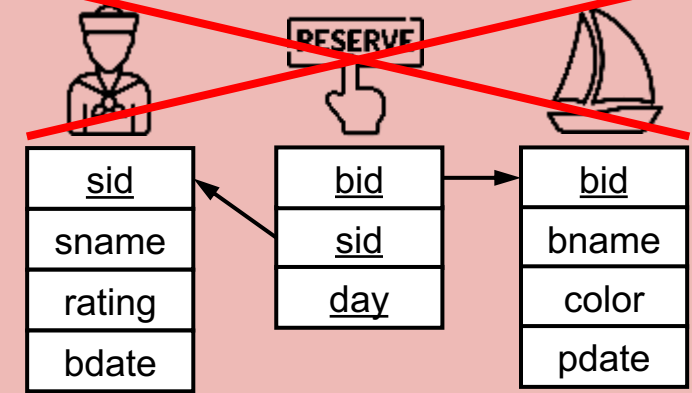
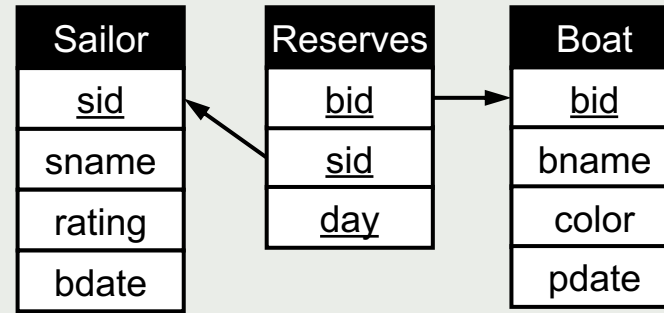


1. We prefer text as names/labels for atomic elements (tables, attributes)
2. We prefer to "visualize" relationships (the "structure") between these elements.

# There seems to be a sweet spot for visualizing relations

Sailor(sid, sname, rating, bdate)  
Reserves(sid, bid, day)  
Boat(bid, bname, color, pdate)

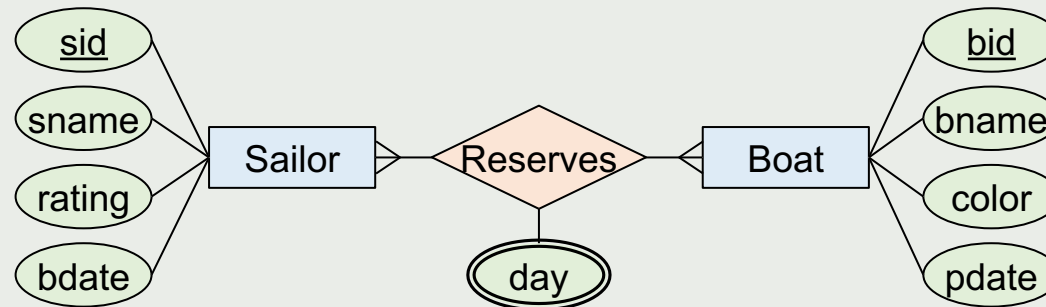
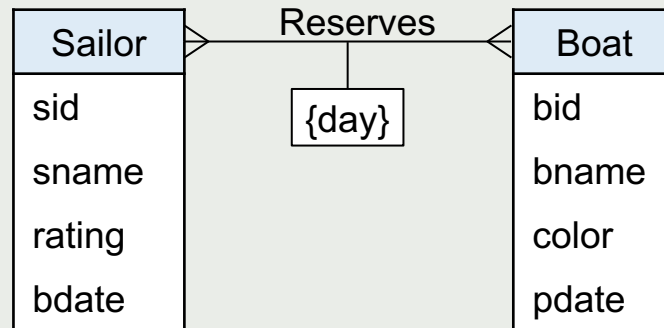
~~FK Reserves.sid references Sailor~~  
~~FK Reserves.bid references Boat~~



Sailor(sid, sname, rating, bdate)

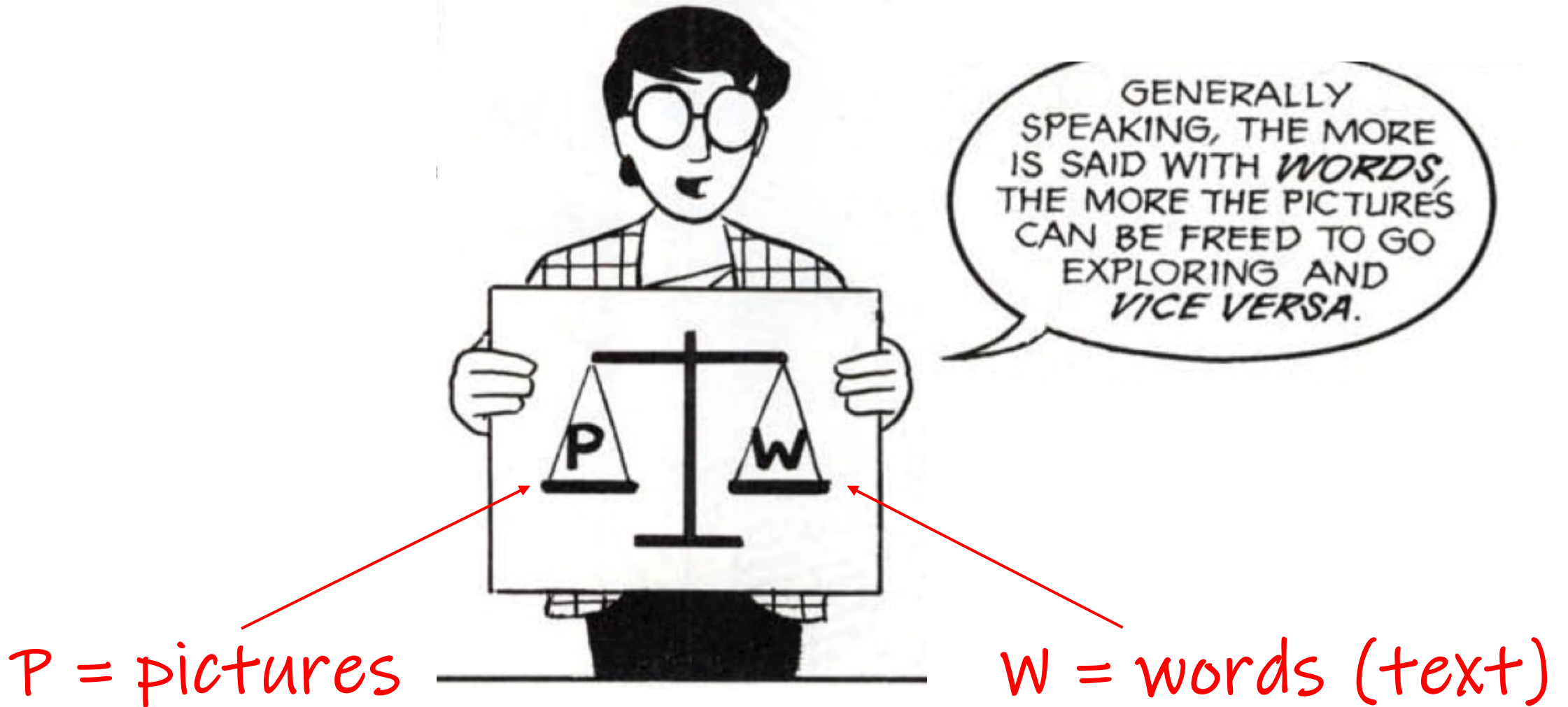
Reserves(sid, bid, day)

Boat(bid, bname, color, pdate)



1. We prefer text as names/labels for atomic elements (tables, attributes)
2. We prefer to "visualize" relationships (the "structure") between these elements.

# Text (= words) vs. pictures in Comics



# Text vs. visualization for "information visualization"

## **Show It or Tell It?** **Text, Visualization, and Their Combination**

Marti A. Hearst

hearst@berkeley.edu

University of California, Berkeley  
Berkeley, CA, USA



- How much text should appear on a visualization?
- What should it say?
- Where should it be placed?
- And how do the visual and the language components interact?

What important "structures"  
(relationships) do we actually  
have in relational queries?  
Answer: the join structures!

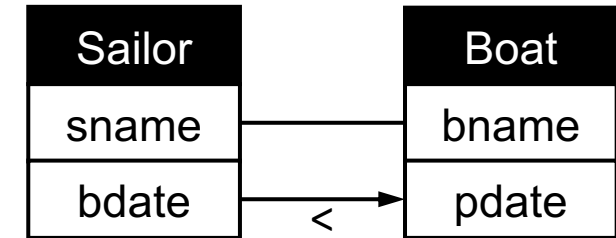
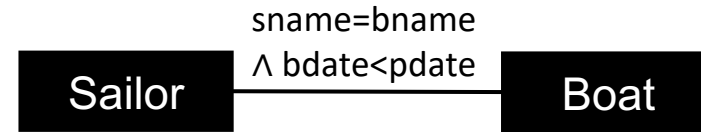
# Textual vs diagrammatic representations

Schema

Sailor	Boat
sid	bid
sname	bname
rating	color
bdate	pdate

Q: "There is a sailor with the same name as a boat,  
and that boat was purchased before the sailor was born."

```
select exists
(select *
from Sailor, Boat
where sname=bname
and bdate<pdate)
```



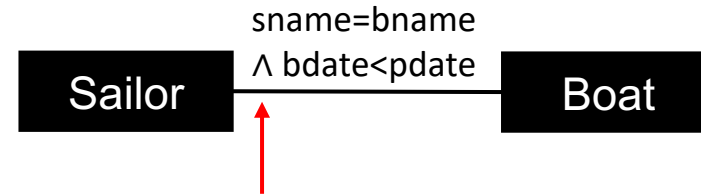
# Textual vs diagrammatic representations

Schema

Sailor	Boat
sid	bid
sname	bname
rating	color
bdate	pdate

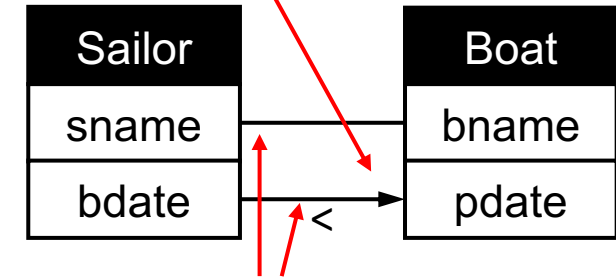
Q: "There is a sailor with the same name as a boat,  
and that boat was purchased before the sailor was born."

```
select exists
(select *
from Sailor, Boat
where sname=bname
and bdate<pdate)
```



a new syntactic device "Λ"  
for conjunction, used in text

arrowhead shows:  
"bdate < pdate"



juxtaposition of conjunctive information  
(we perceive them independently)

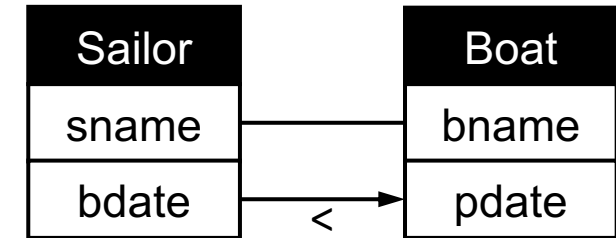
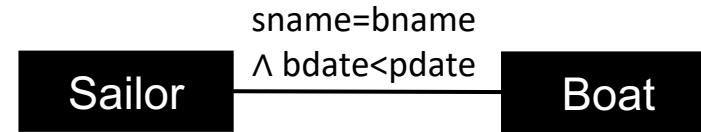
# Textual vs diagrammatic representations

Schema

Sailor	Boat
sid	bid
sname	bname
rating	color
bdate	pdate

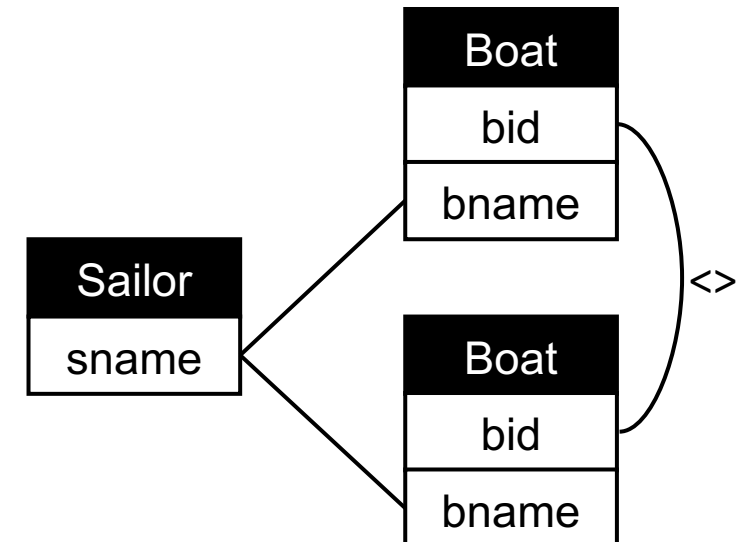
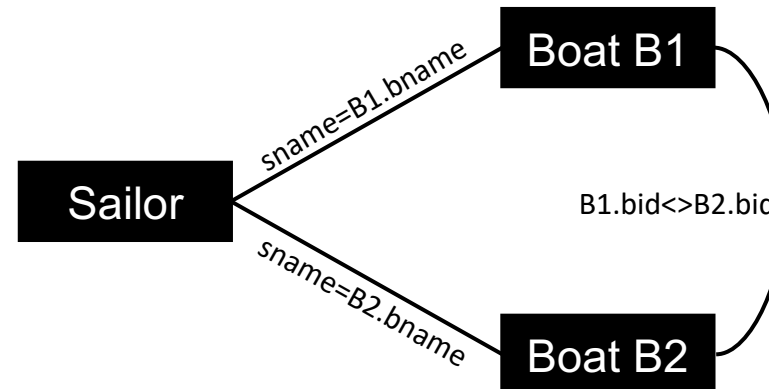
Q: "There is a sailor with the same name as a boat, and that boat was purchased before the sailor was born."

```
select exists
(select *
from Sailor, Boat
where sname=bname
and bdate<pdate)
```



Q: "There is a sailor who shares the same name with 2 different boats."

```
select exists
(select *
from Sailor, Boat B1, Boat B2
where sname=B1.bname
and sname=B2.bname
and B1.bid<>B2.bid)
```





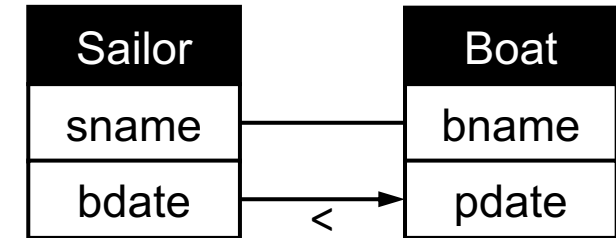
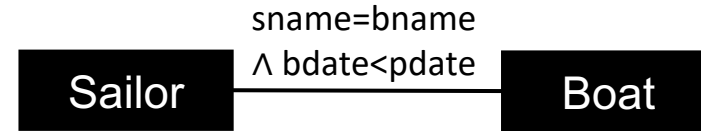
# Textual vs diagrammatic representations

Schema

Sailor	Boat
sid	bid
sname	bname
rating	color
bdate	pdate

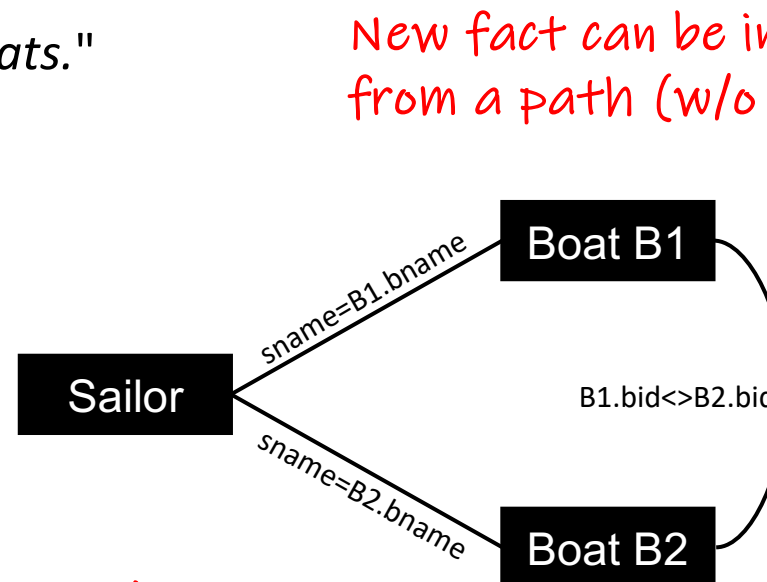
Q: "There is a sailor with the same name as a boat, and that boat was purchased before the sailor was born."

```
select exists
(select *
from Sailor, Boat
where sname=bname
and bdate<pdate)
```

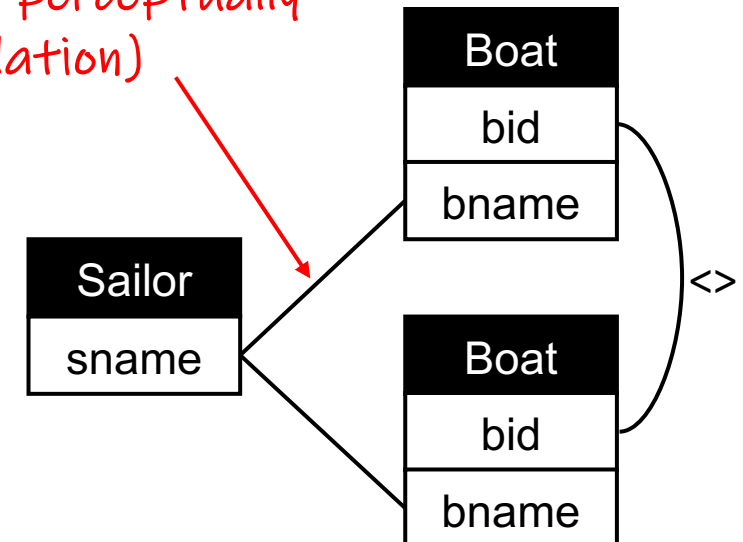


Q: "There is a sailor who shares the same name with 2 different boats."

```
select exists
(select *
from Sailor, Boat B1, Boat B2
where sname=B1.bname
and sname=B2.bname
and B1.bid<>B2.bid)
```



New fact can be inferred "perceptually" from a path (w/o manipulation)



⇒ B1.bname=B2.bname  
(the two boats share the names too!)

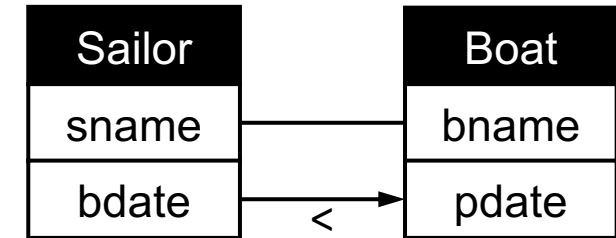
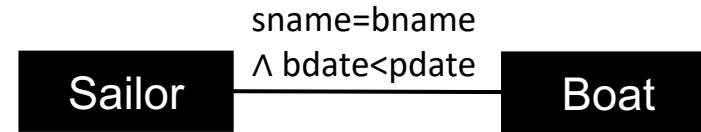
# Textual vs diagrammatic representations

Schema

Sailor	Boat
sid	bid
sname	bname
rating	color
bdate	pdate

Q: "There is a sailor with the same name as a boat, and that boat was purchased before the sailor was born."

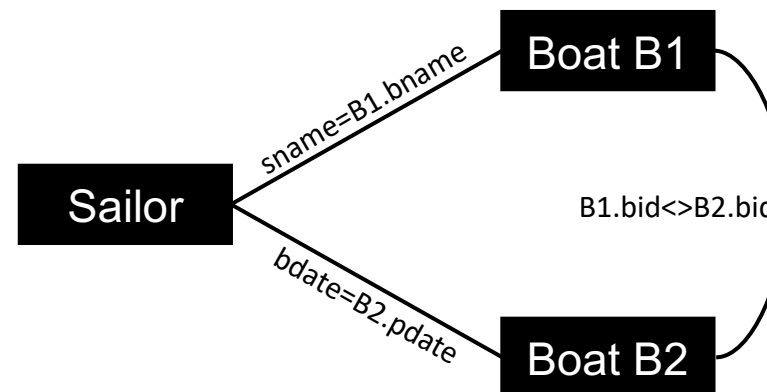
```
select exists
(select *
from Sailor, Boat
where sname=bname
and bdate<pdate)
```



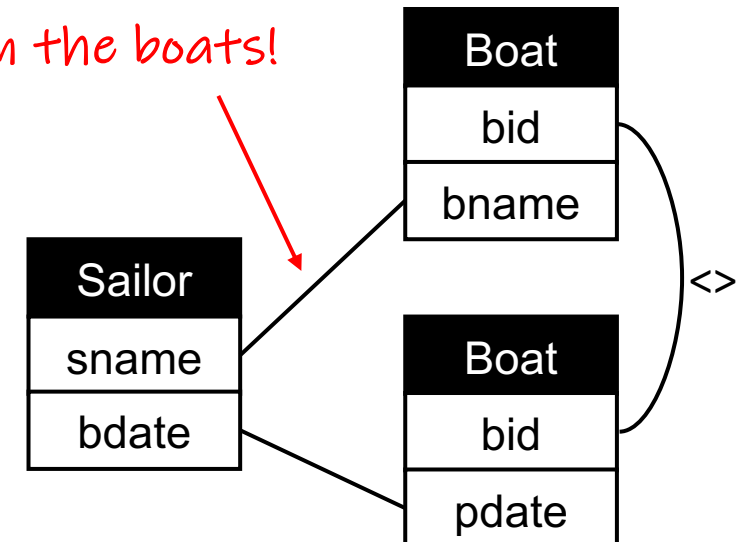
Q: "There is a sailor who shares the name with one boat and the birthday with the purchase day of another boat."

```
select exists
(select *
from Sailor, Boat B1, Boat B2
where sname=B1.bname
and bdate=B2.pdate
and B1.bid<>B2.bid)
```

⇒ ~~B1.bname B2.bname~~



No path between the boats!



# "Textual" vs "Diagrammatic" Representations

"structure" / "relation" / "relationship" = join structure !

## TEXTUAL

symbolic, linguistic,  
linear, sentential



## DIAGRAMMATIC

visual, graphical, non-  
symbolic, schematic, as  
picture, two-dimensional

*"Diagram: a simplified drawing showing the appearance, structure, or workings of something; a schematic representation."* [Oxford languages]

*"Diagram: a graphic design that explains rather than represents; especially: a drawing that shows arrangement and relations (as of parts)"* [Merriam-Webster]

*"Logic diagram: a two-dimensional geometric figure with spatial relations that are isomorphic with the structure of a logical statement"* [Gardner, 1958, p. 28]

*"The relationships established between two sets of elements constitute a diagram."* [Bertin, 1981, p. 129]

[Oxford languages]: <https://www.google.com/search?q=diagram>, [Merriam-Webster]: <https://www.merriam-webster.com/dictionary/diagram>,

[Gardner, 1958]: Martin Gardner, Logic machines and diagrams, McGraw-Hill 1958. <https://archive.org/details/logicmachinesdia227gard/mode/2up>,

[Bertin, 1981]: Jacques Bertin. Graphics and graphic information-processing. de Gruyter. 1981

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

Now we have a shared notion of "diagrams"  
Next: What are desiderata for QV?

We call those "principles". But they are not meant to be irrevocable axioms, but rather intuitive objectives, whose formulation help us develop a shared vocabulary to discuss various approaches. They can be revisited when needed.

# Algebraic Visualization Design [Kindlmann, Scheidegger 2014]

$$\Delta D \longrightarrow \Delta V$$

Goal: describe how changes in data lead to changes in the visualization

Data  $\longrightarrow$  Representation  $\longrightarrow$  Visualization

Key insight: visualizations don't act on data itself, but on representations of data

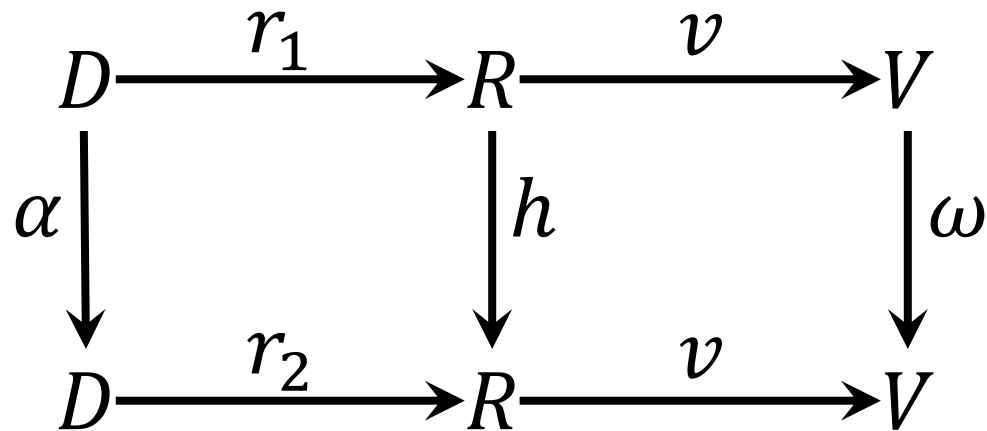
# Algebraic Visualization Design [Kindlmann, Scheidegger 2014]

$$\Delta D \longrightarrow \Delta V$$

Goal: describe how changes in data lead to changes in the visualization

Data  $\longrightarrow$  Representation  $\longrightarrow$  Visualization

Key insight: **visualizations don't act on data itself, but on representations of data**

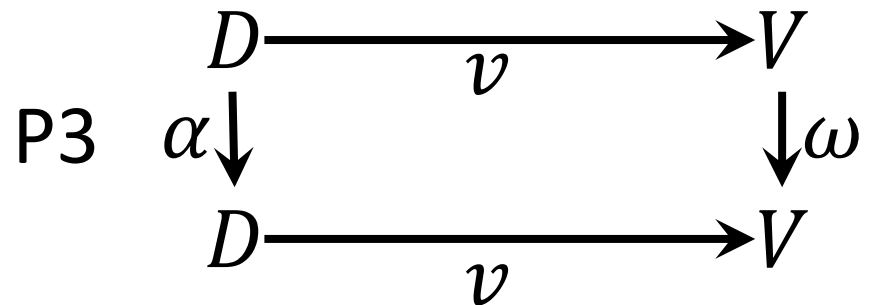
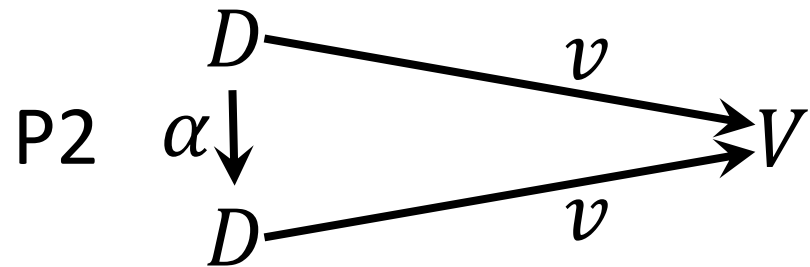
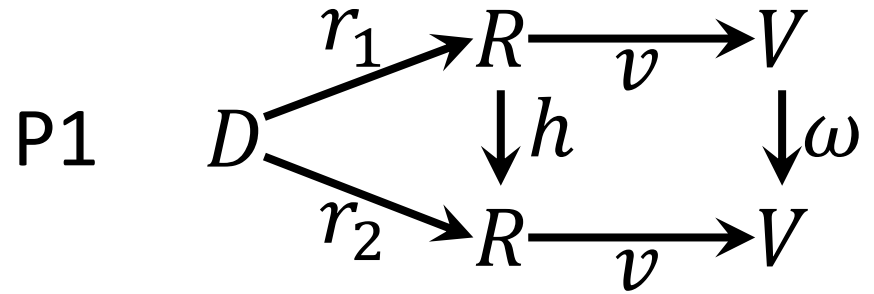


Formulate 3 "algebraic" design principles in the language of a commutative diagram.

Vertical arrows represent transformations. "no difference" expressed as identity transformation, e.g.  $\alpha = I$  for  $\alpha(D) = D$

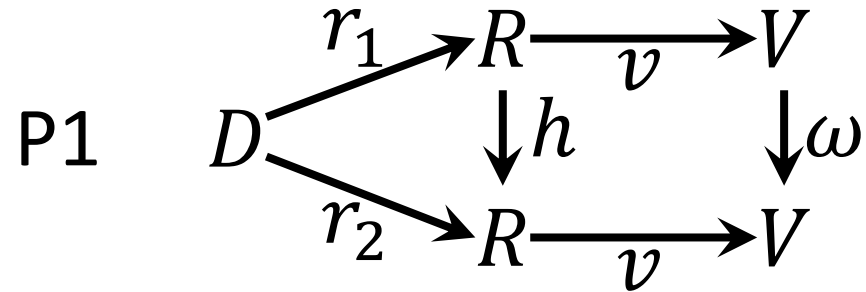
# 3 algebraic visualization principles by [Kindlmann, Scheidegger 2014]

Data  $\rightarrow$  Representation  
 $\rightarrow$  Visualization



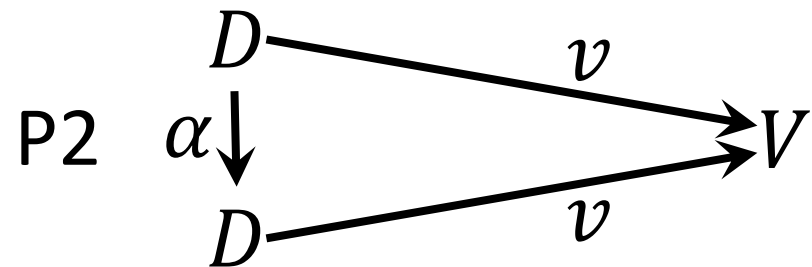
# 3 algebraic visualization principles by [Kindlmann, Scheidegger 2014]

Data  $\rightarrow$  Representation  
 $\rightarrow$  Visualization

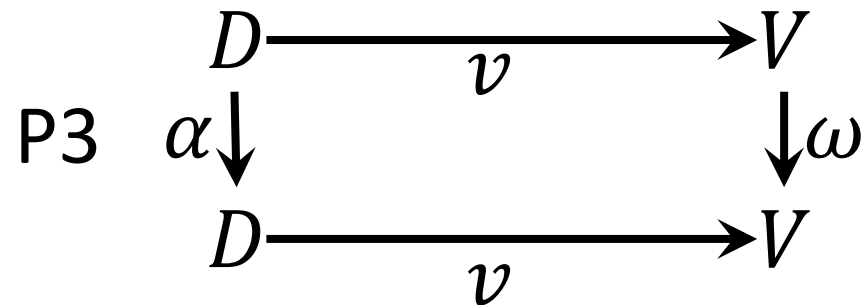


## P1: PRINCIPLE OF REPRESENTATION INVARIANCE

A different representation, for the same data, does not lead to a different visualization. ( $\alpha = I_D \Rightarrow \omega = I_V$ )

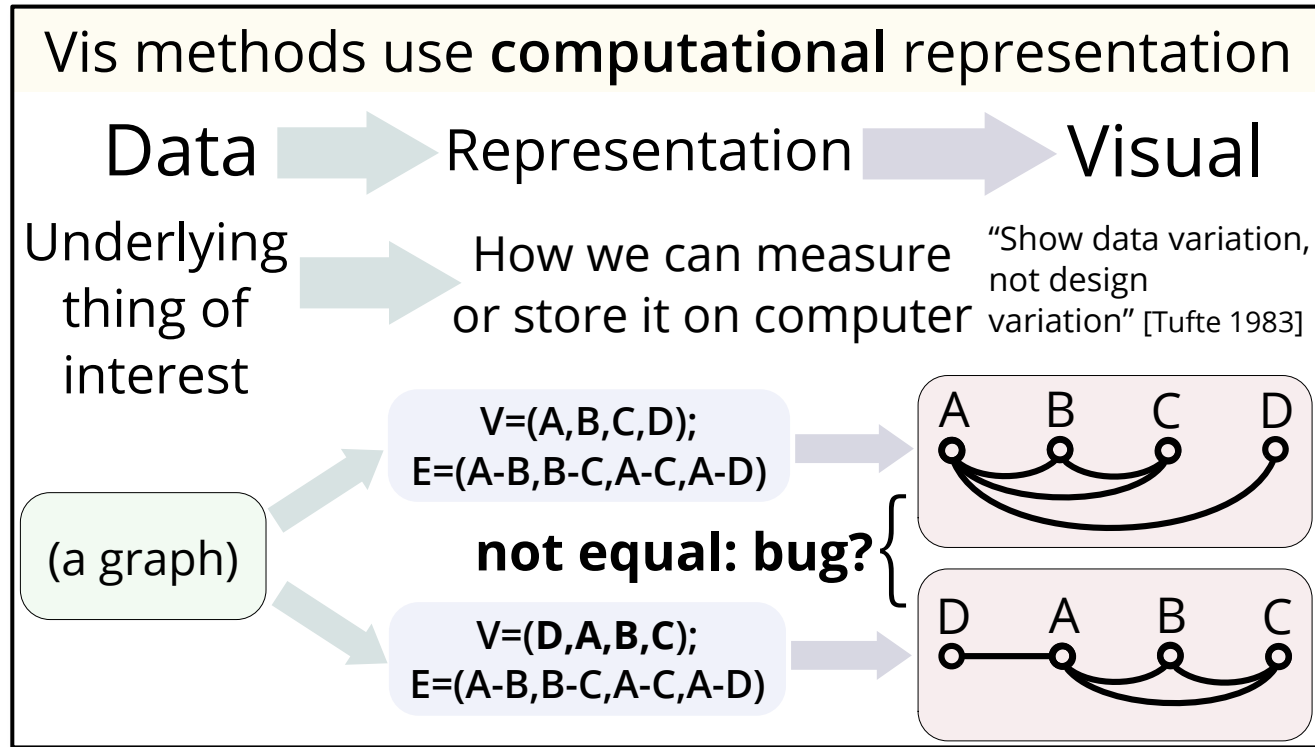


Reminiscent of logical data independence (however you normalize, you get the same information)

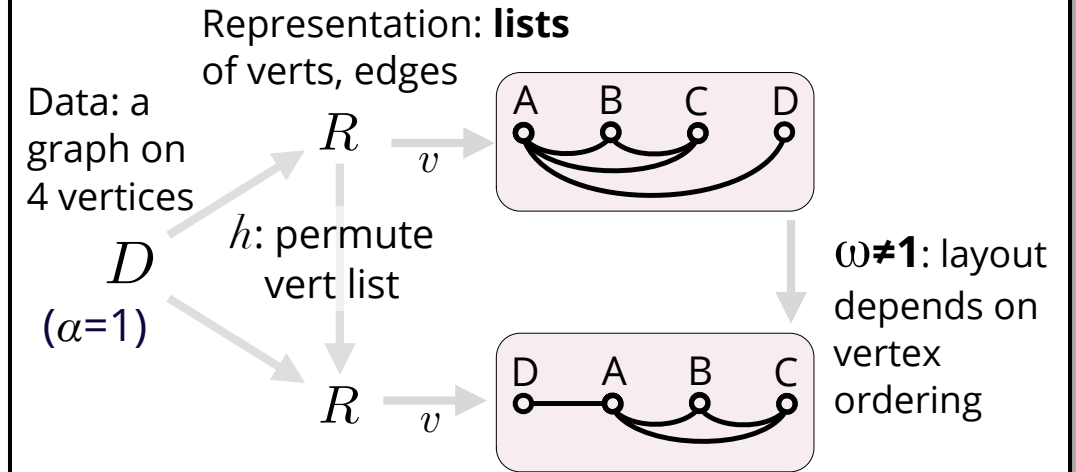




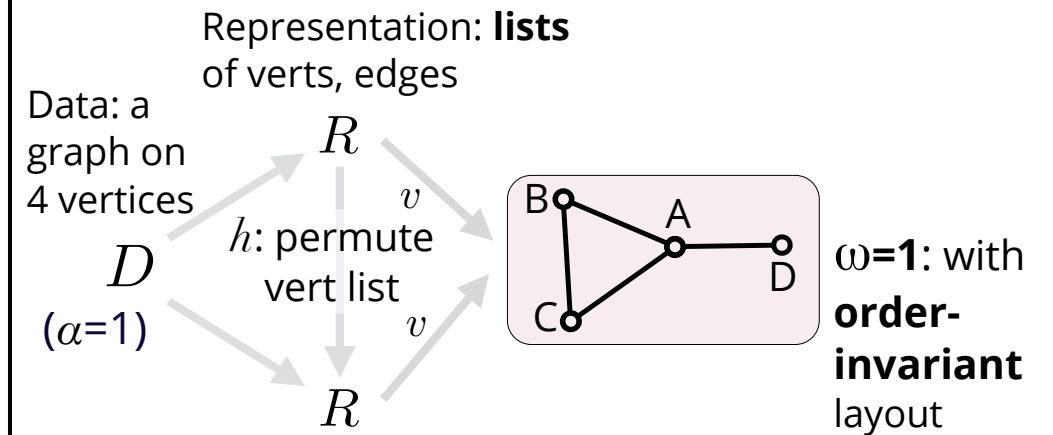
# Example of P1: Representation Invariance for InfoViz



## Invariance example: Graph layout

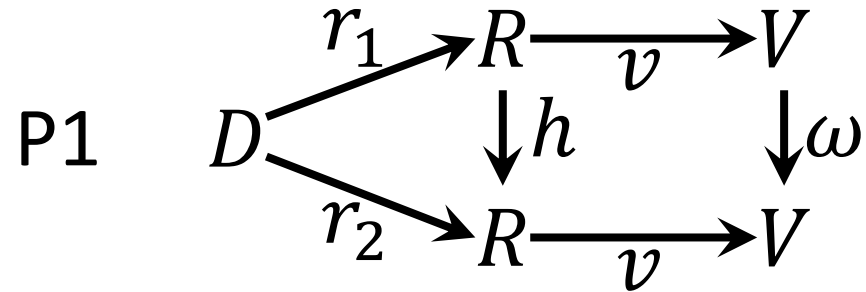


## Invariance example: Graph layout



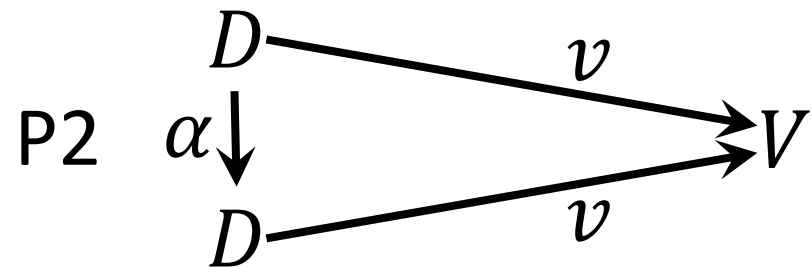
# 3 algebraic visualization principles by [Kindlmann, Scheidegger 2014]

Data  $\rightarrow$  Representation  
 $\rightarrow$  Visualization



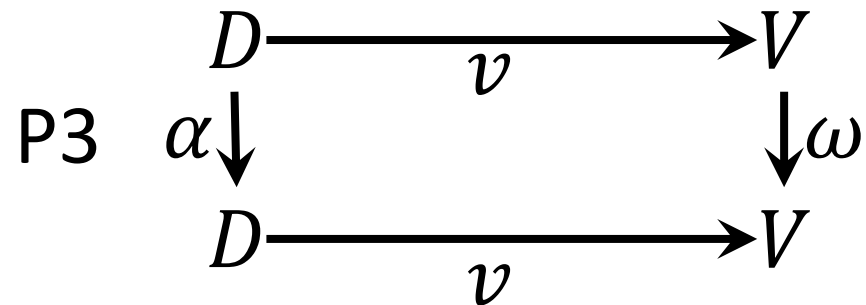
## P1: PRINCIPLE OF REPRESENTATION INVARIANCE

A different representation, for the same data, does not lead to a different visualization. ( $\alpha = I_D \Rightarrow \omega = I_V$ )



## P2: UNAMBIGUOUS DATA DEPICTION PRINCIPLE

"An interesting  $\alpha$  applied to the data should induce a non-trivial  $\omega$ ." ( $\omega = I_V \Rightarrow \alpha = I_D$ )



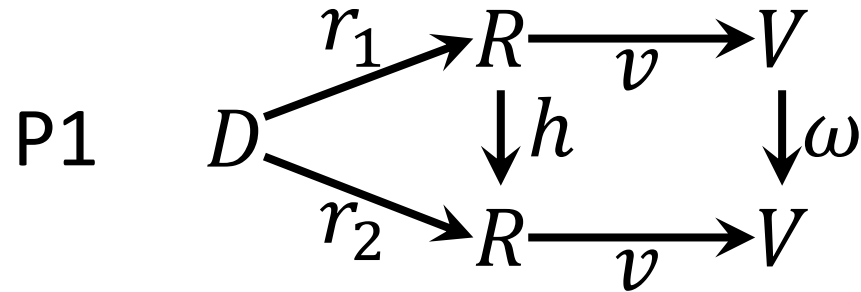
## P3: CORRESPONDENCE PRINCIPLE ("congruence")

" $\omega$  somehow makes sense, given  $\alpha$ ." ( $\alpha \cong \omega$ )  
(also: noticeable, "meaningful" changes)

# 3 algebraic visualization principles by [Kindlmann, Scheidegger 2014]

Data  $\rightarrow$  Representation  
 $\rightarrow$  Visualization

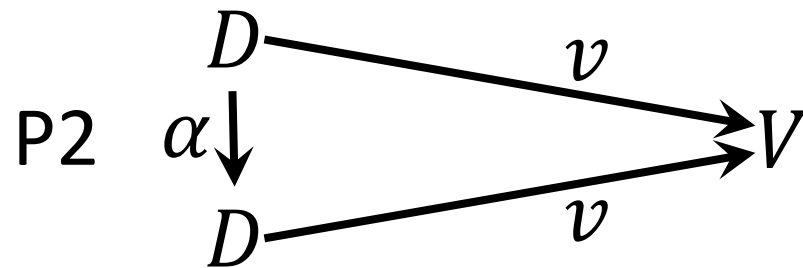
*We will adapt these 3 "principles", originally meant for InfoViz, instead to Query Visualization*



**P1: PRINCIPLE OF REPRESENTATION INVARIANCE**

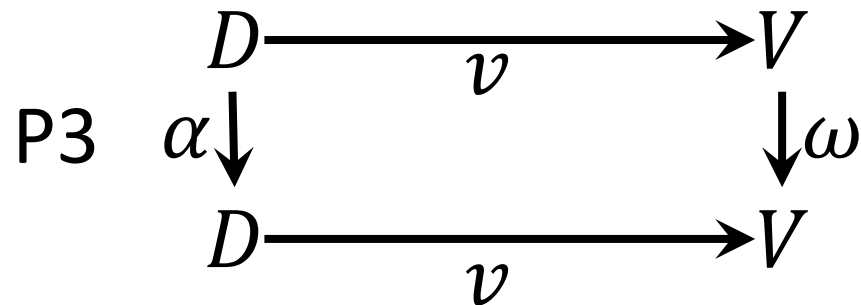
A different representation, for the same data, does not lead to a different visualization. ( $\alpha = I_D \Rightarrow \omega = I_V$ )

*$\rightarrow$  4 bijection principles for Query Visualization*



**P2: UNAMBIGUOUS DATA DEPICTION PRINCIPLE**

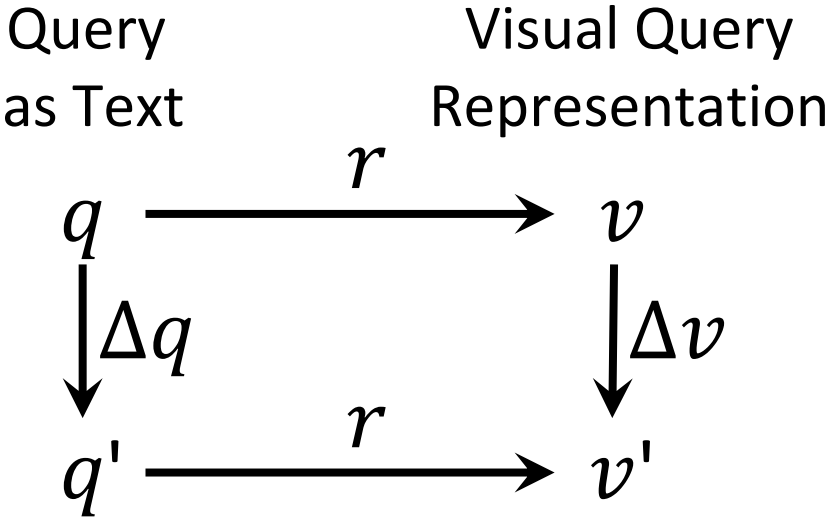
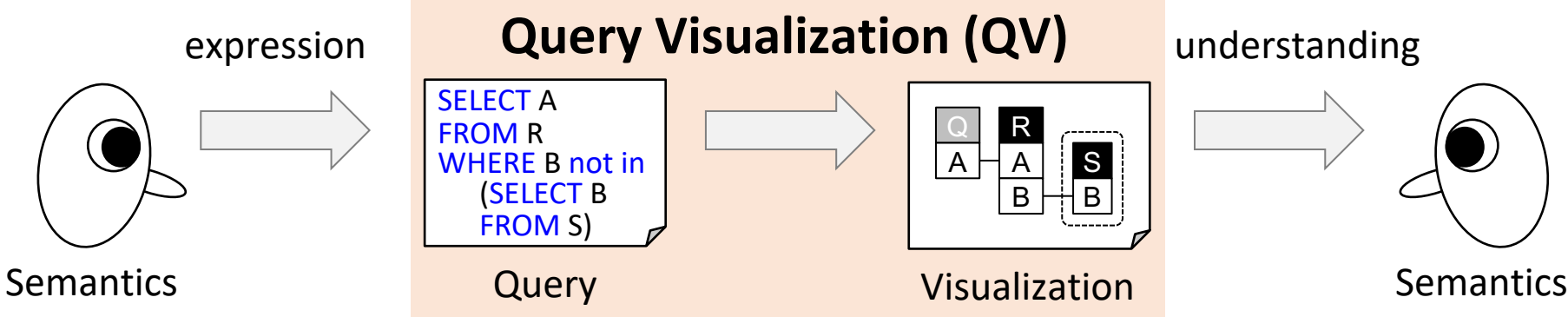
"An interesting  $\alpha$  applied to the data should induce a non-trivial  $\omega$ ." ( $\omega = I_V \Rightarrow \alpha = I_D$ )



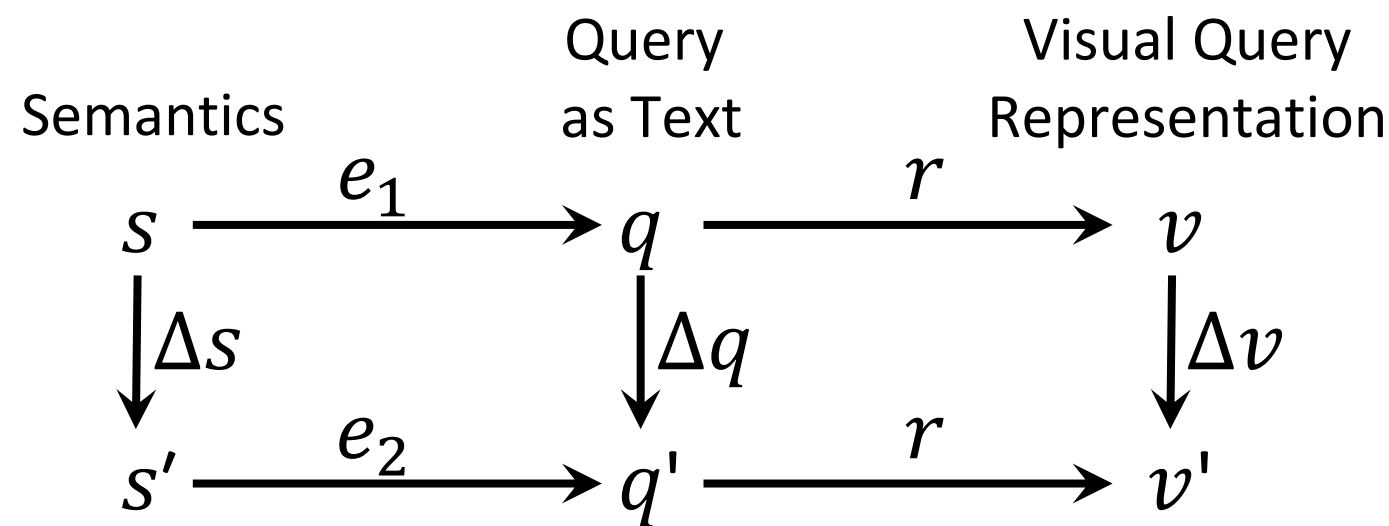
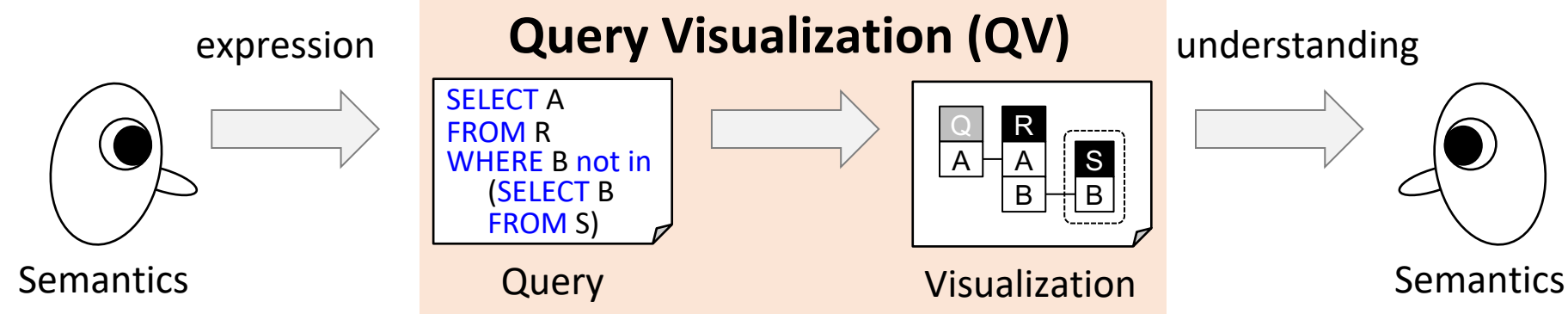
**P3: CORRESPONDENCE PRINCIPLE ("congruence")**

" $\omega$  somehow makes sense, given  $\alpha$ ." ( $\alpha \cong \omega$ )  
(also: noticeable, "meaningful" changes)

# An Algebraic Framework for Query Visualization

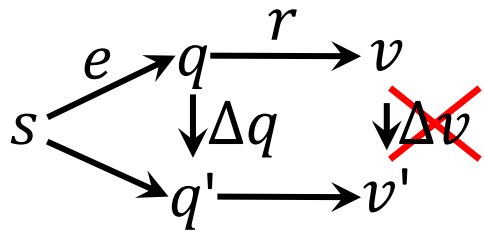


# An Algebraic Framework for Query Visualization

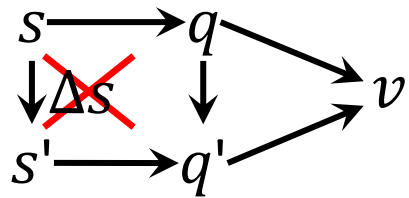


# 4 Bijection principles of Query Visualization

## P1. REPRESENTATION INVARIANCE



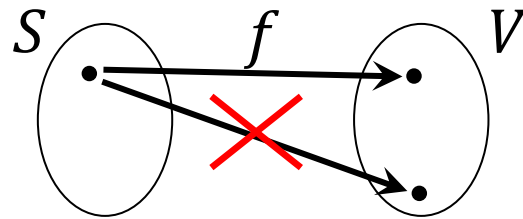
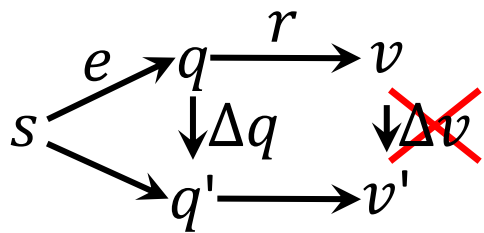
## P2. UNAMBIGUOUS



# 4 Bijection principles of Query Visualization

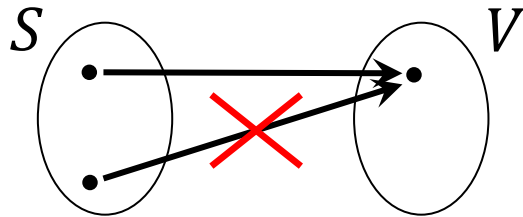
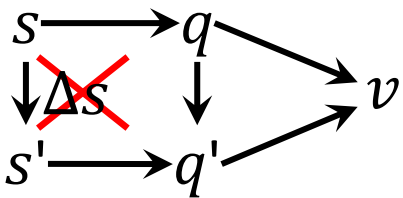
More on this controversial principle later (thus "seven")

## P1. REPRESENTATION INVARIANCE



FUNCTION  
(instead  
of Relation)

## P2. UNAMBIGUOUS



INJECTIVE  
(preserve  
distinction)

P7:

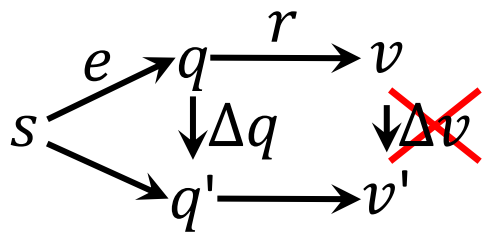
Visualizations abstract away from syntax details ("syntactic invariance"): Each query semantics gets mapped to exactly one visualization  $\Delta S=0 \Rightarrow \Delta V=0$

P2:

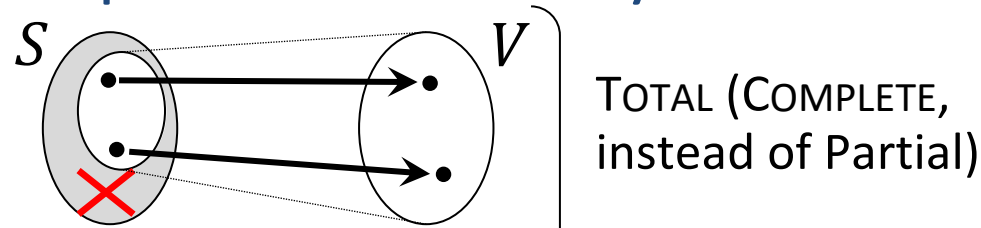
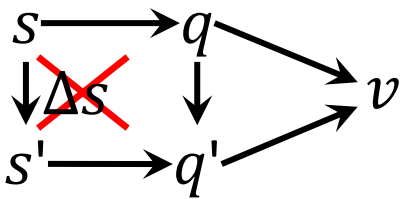
Visualizations are unambiguous: Every visualization represents at most one query semantics

# 4 Bijection principles of Query Visualization

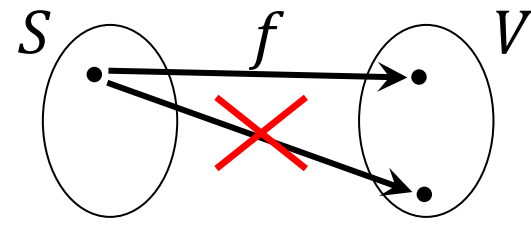
P1. REPRESENTATION INVARIANCE



P2. UNAMBIGUOUS

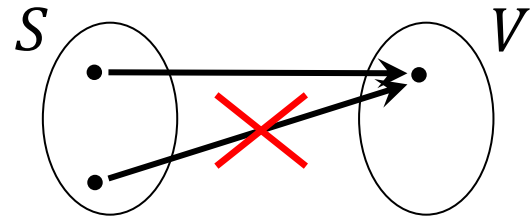


TOTAL (COMPLETE,  
instead of Partial)



TOTAL FUNCTION

FUNCTION  
(instead  
of Relation)



INJECTIVE  
(preserve  
distinction)

P1:

The visual query representation is relationally complete: every query semantics can be represented

P7:

Visualizations abstract away from syntax details ("syntactic invariance"): Each query semantics gets mapped to exactly one visualization  $\Delta S=0 \Rightarrow \Delta V=0$

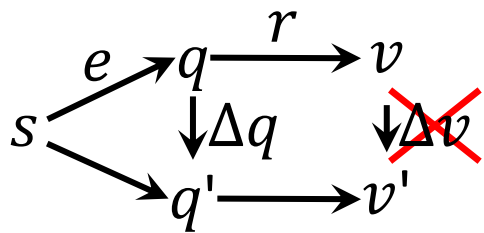
P2:

Visualizations are unambiguous: Every visualization represents at most one query semantics

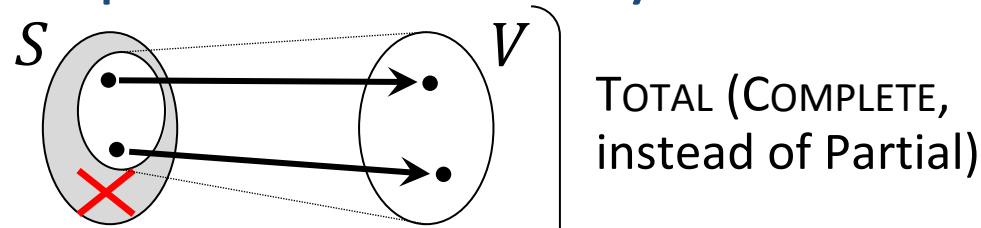
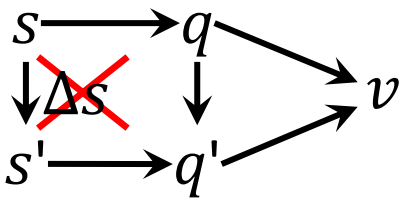


# 4 Bijection principles of Query Visualization

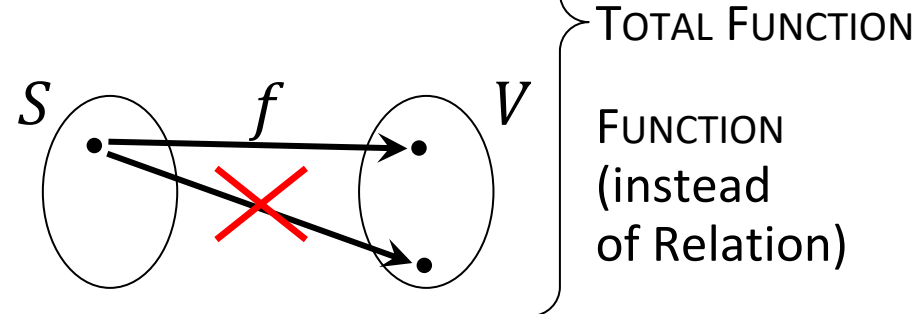
P1. REPRESENTATION INVARIANCE



P2. UNAMBIGUOUS

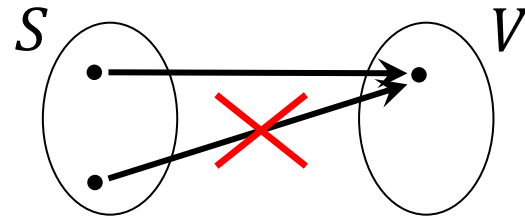


TOTAL (COMPLETE,  
instead of Partial)

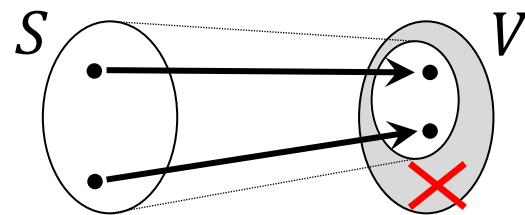


TOTAL FUNCTION

FUNCTION  
(instead  
of Relation)



INJECTIVE  
(preserve  
distinction)



SURJECTIVE  
(covering)

P1:

The visual query representation is relationally complete: every query semantics can be represented

P7:

Visualizations abstract away from syntax details ("syntactic invariance"): Each query semantics gets mapped to exactly one visualization  $\Delta S=0 \Rightarrow \Delta V=0$

P2:

Visualizations are unambiguous: Every visualization represents at most one query semantics

P3:

Visualizations are sound: Every valid visualization has some valid interpretation (query semantics)

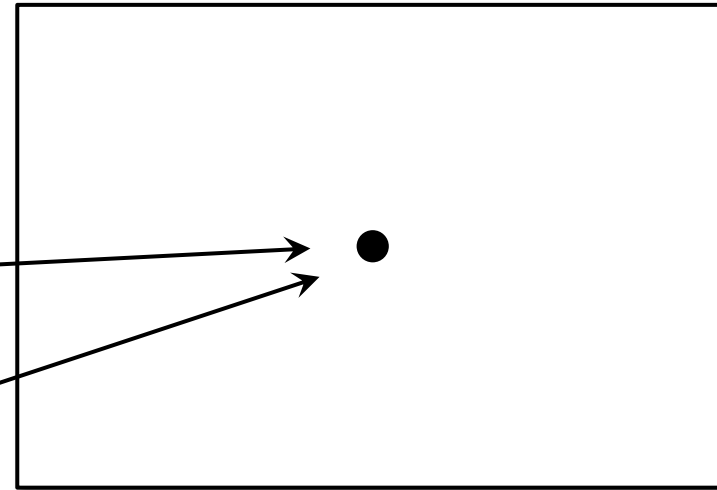
# Exercise: Discuss following new "query visualization"

Take any query and represent it by a centered dot in the plane  
(You can make it "interactive": a clicking on the dot reveals the SQL query)

Which of the 4 principles to the right does this fulfill ?

```
select S.sname
from Sailor s, Reserves r, Boat b
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'

select S.sname
from Sailor S
where not exists
(select *
from Boat B
where color = 'red'
and not exists
(select *
from Reserves R
where S.sid=R.sid
and R.bid=B.bid))
```



? P1:  
The visual query representation is relationally complete: every query semantics can be represented

? P7:  
Visualizations abstract away from syntax details ("syntactic invariance"): Each query semantics gets mapped to exactly one visualization  $\Delta S=0 \Rightarrow \Delta V=0$

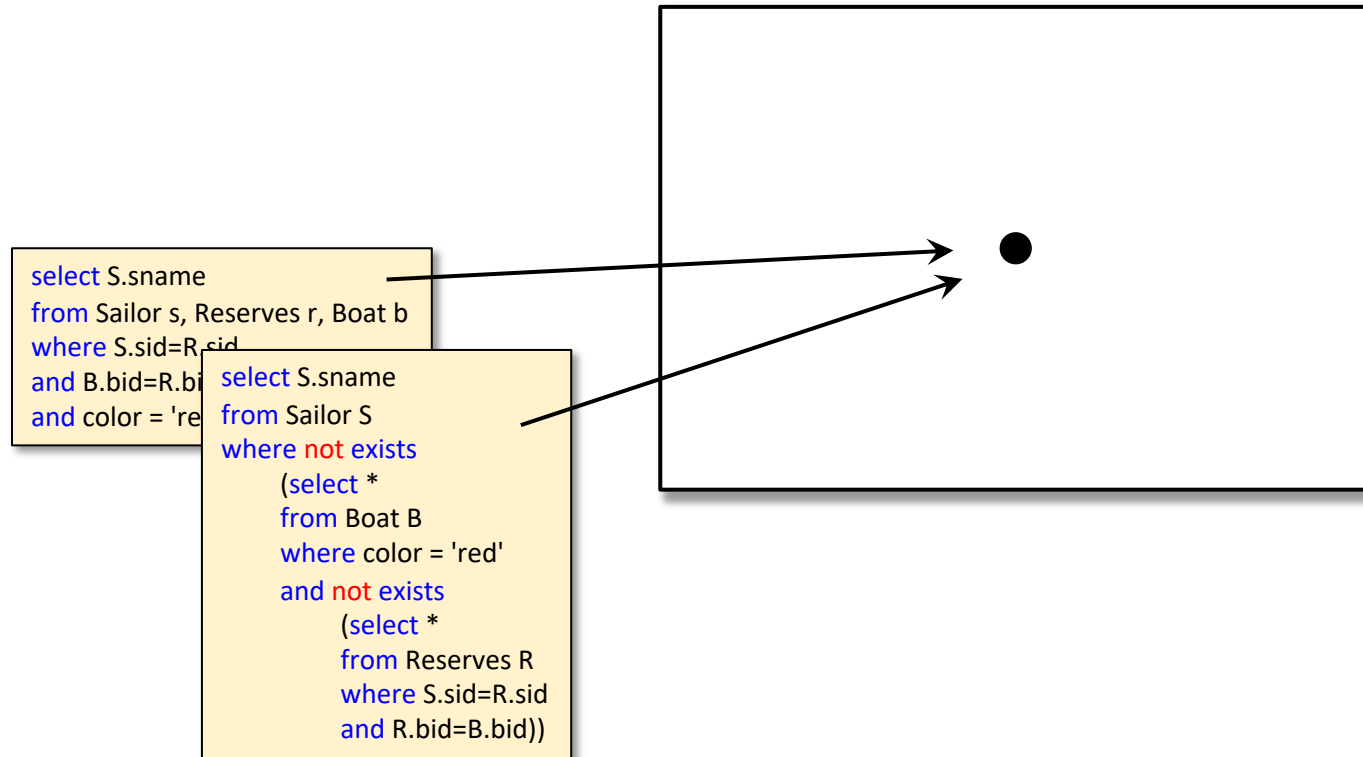
? P2:  
Visualizations are unambiguous: Every visualization represents at most one query semantics


? P3:  
Visualizations are sound: Every valid visualization has some valid interpretation (query semantics)


# Exercise: Discuss following new "query visualization"


Take any query and represent it by a centered dot in the plane  
(You can make it "interactive": a clicking on the dot reveals the SQL query)


Which of the 4 principles to the right does this fulfill ?



P1:  The visual query representation is relationally complete: every query semantics can be represented

P7:  Visualizations abstract away from syntax details ("syntactic invariance"): Each query semantics gets mapped to exactly one visualization  $\Delta S=0 \Rightarrow \Delta V=0$

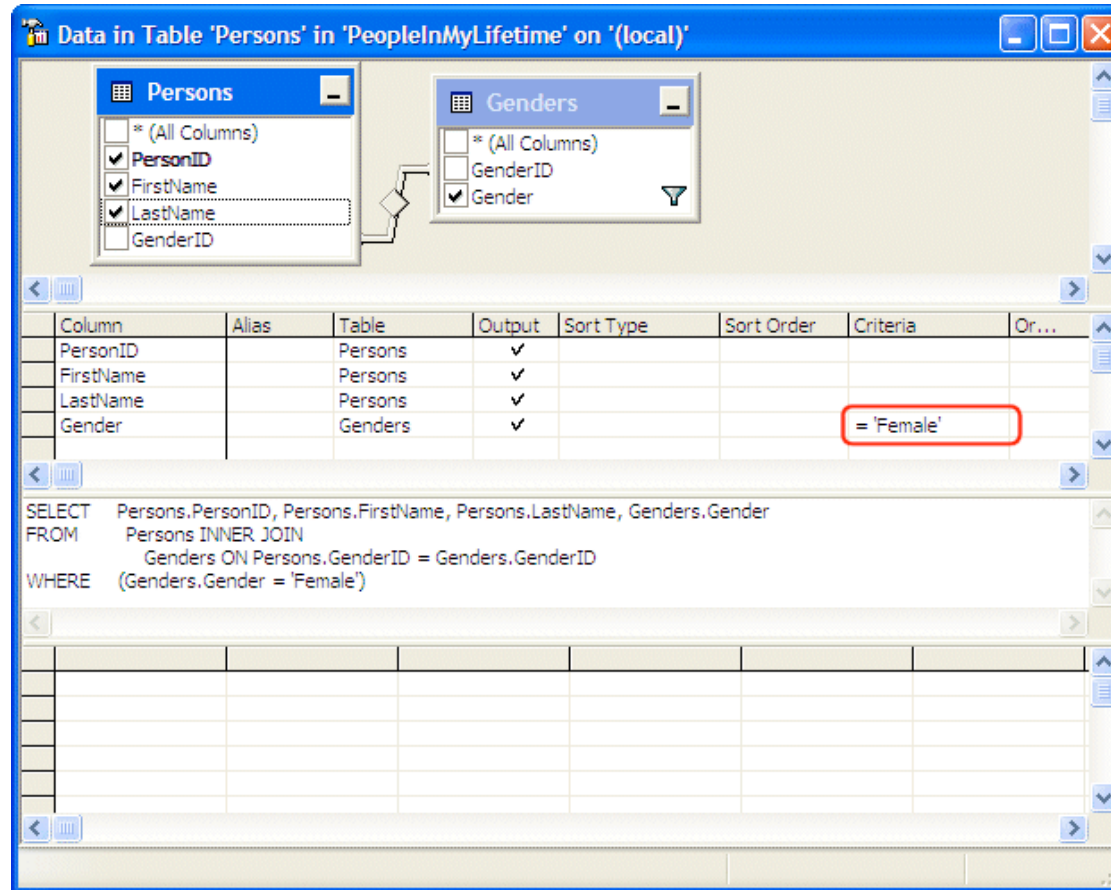
P2:  Visualizations are unambiguous: Every visualization represents at most one query semantics

P3:  Visualizations are sound: Every valid visualization (*here: every single dot!*) has some valid interpretation (query semantics)

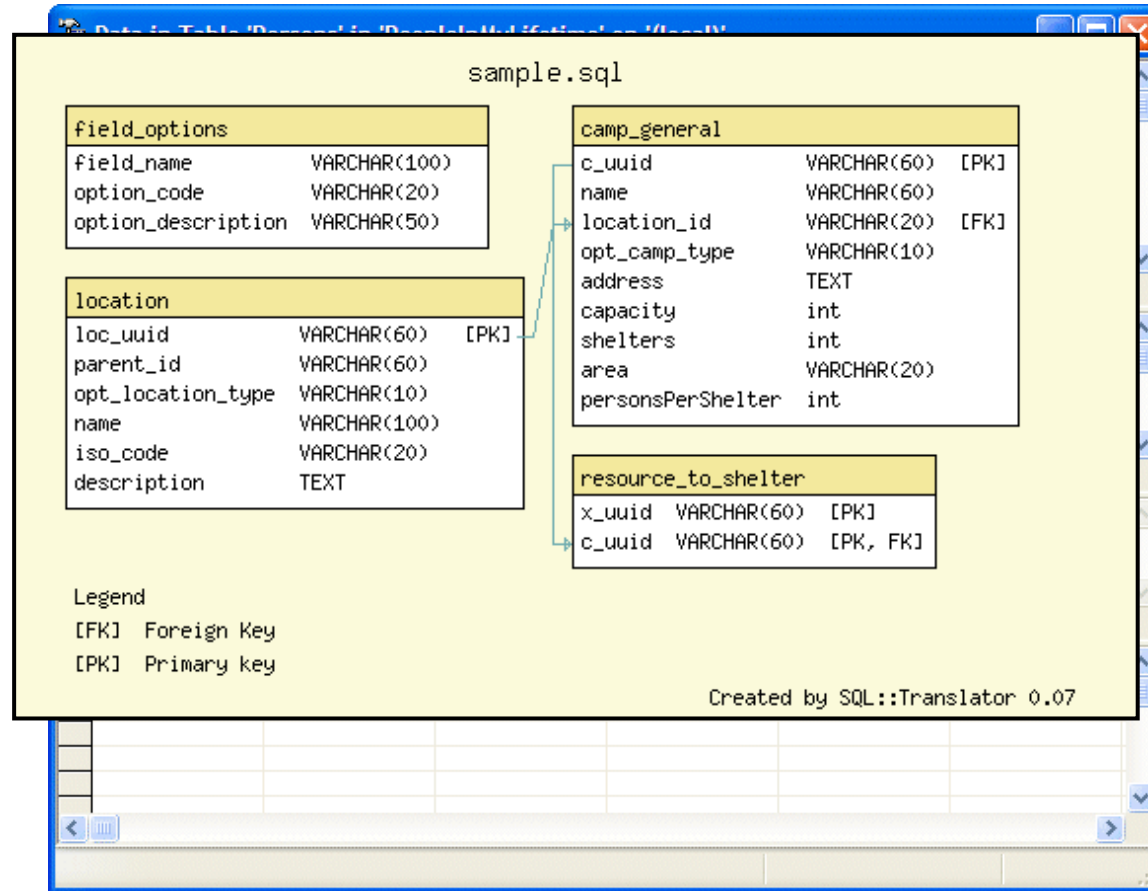
Those were the 4 bijection principles

Next: 7 additional "correspondence"  
principles

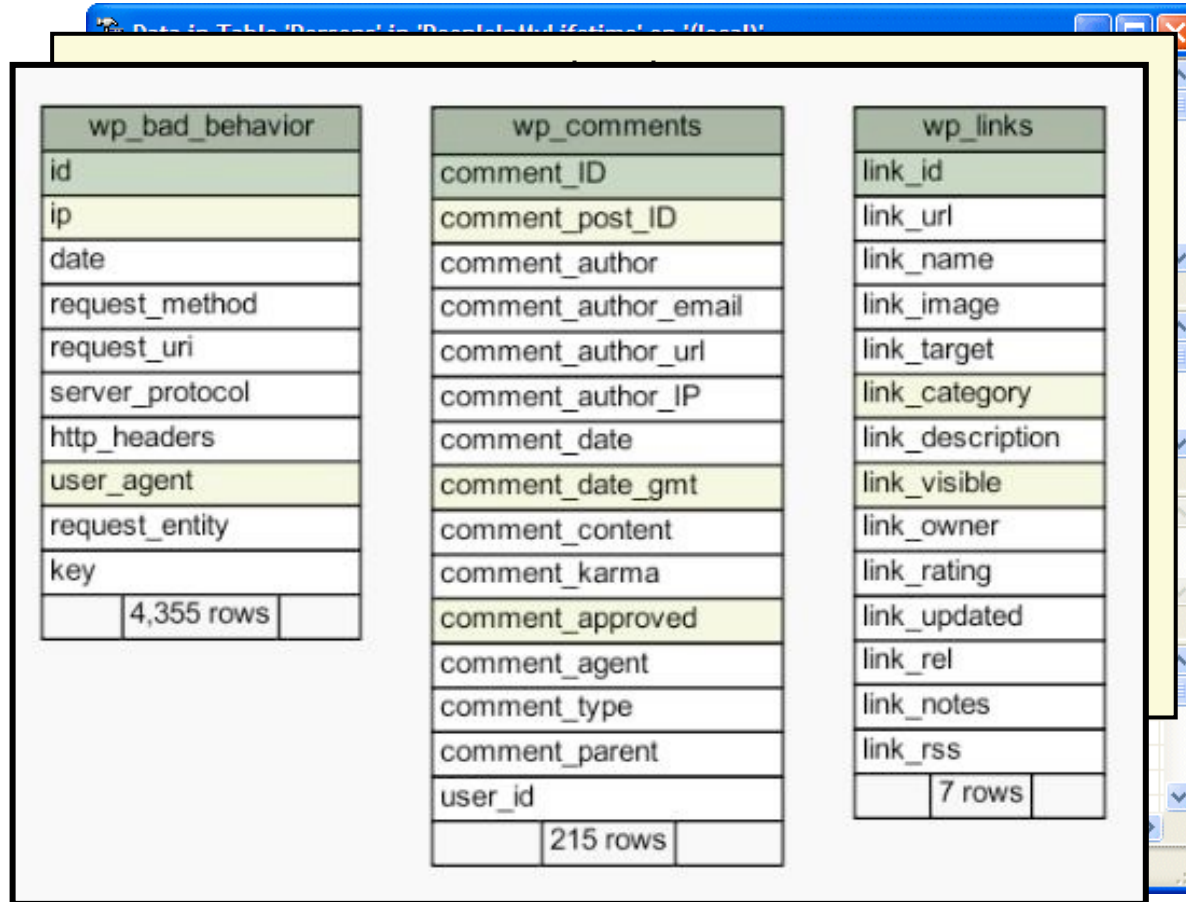
# P4: Existing visual metaphors as starting point



# P4: Existing visual metaphors as starting point



# P4: Existing visual metaphors as starting point



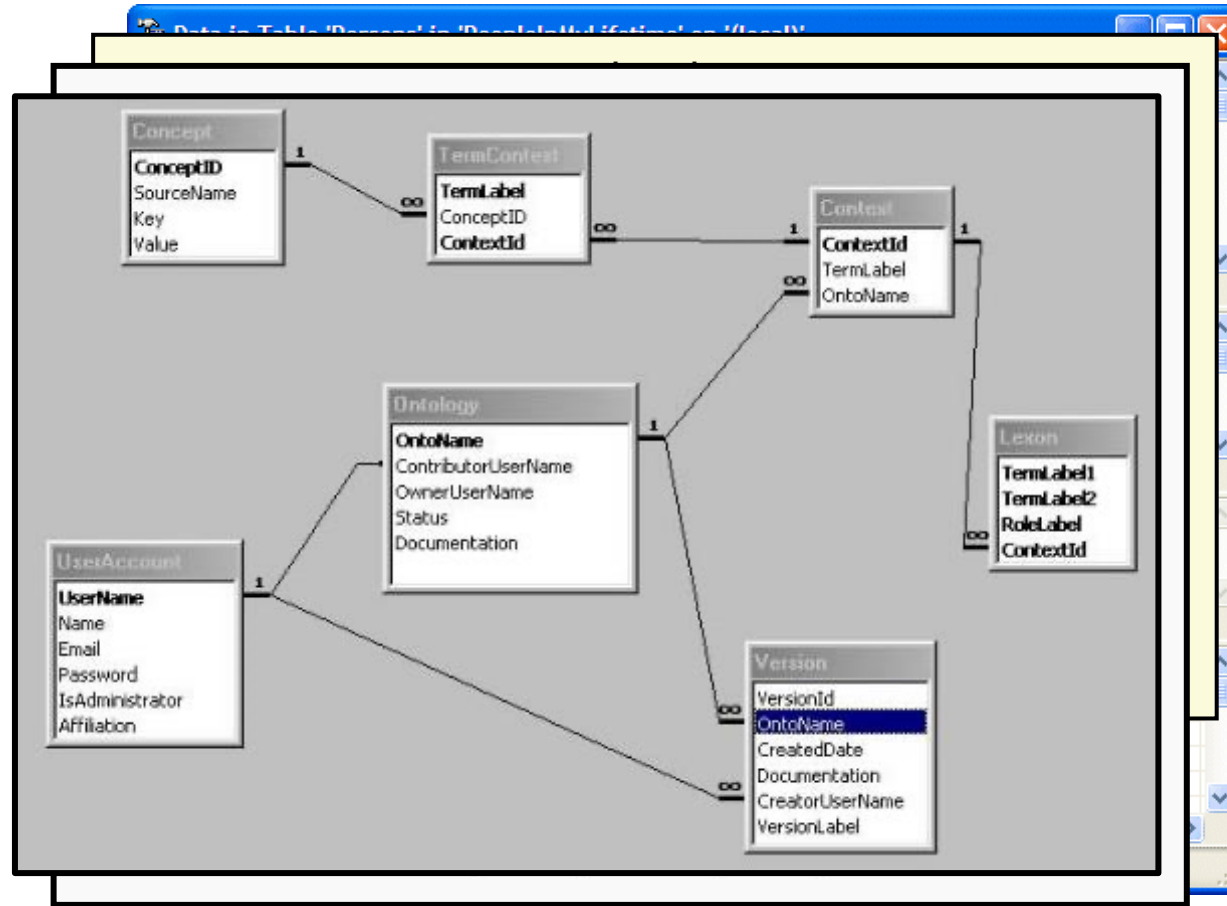
The image shows a screenshot of a database management tool interface. It displays three tables side-by-side: wp\_bad\_behavior, wp\_comments, and wp\_links. Each table is represented as a grid with columns for field names and a summary row at the bottom showing the total number of rows. The wp\_bad\_behavior table has 12 fields and 4,355 rows. The wp\_comments table has 15 fields and 215 rows. The wp\_links table has 13 fields and 7 rows. The interface includes a title bar at the top and a sidebar on the right with various tool icons.

wp_bad_behavior		
id		
ip		
date		
request_method		
request_uri		
server_protocol		
http_headers		
user_agent		
request_entity		
key		
	4,355 rows	

wp_comments		
comment_ID		
comment_post_ID		
comment_author		
comment_author_email		
comment_author_url		
comment_author_IP		
comment_date		
comment_date_gmt		
comment_content		
comment_karma		
comment_approved		
comment_agent		
comment_type		
comment_parent		
user_id		
	215 rows	

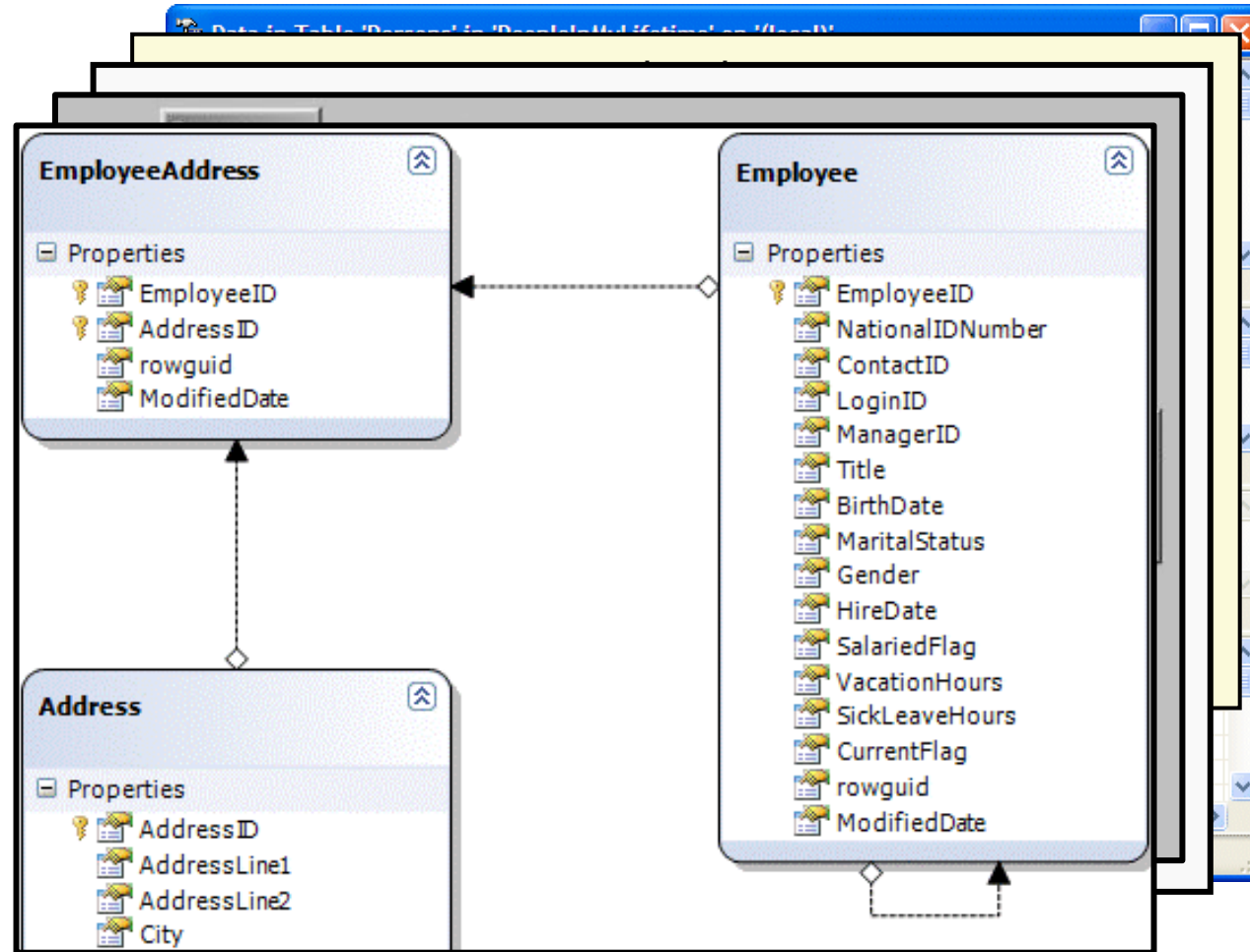
wp_links		
link_id		
link_url		
link_name		
link_image		
link_target		
link_category		
link_description		
link_visible		
link_owner		
link_rating		
link_updated		
link_rel		
link_notes		
link_rss		
	7 rows	

# P4: Existing visual metaphors as starting point

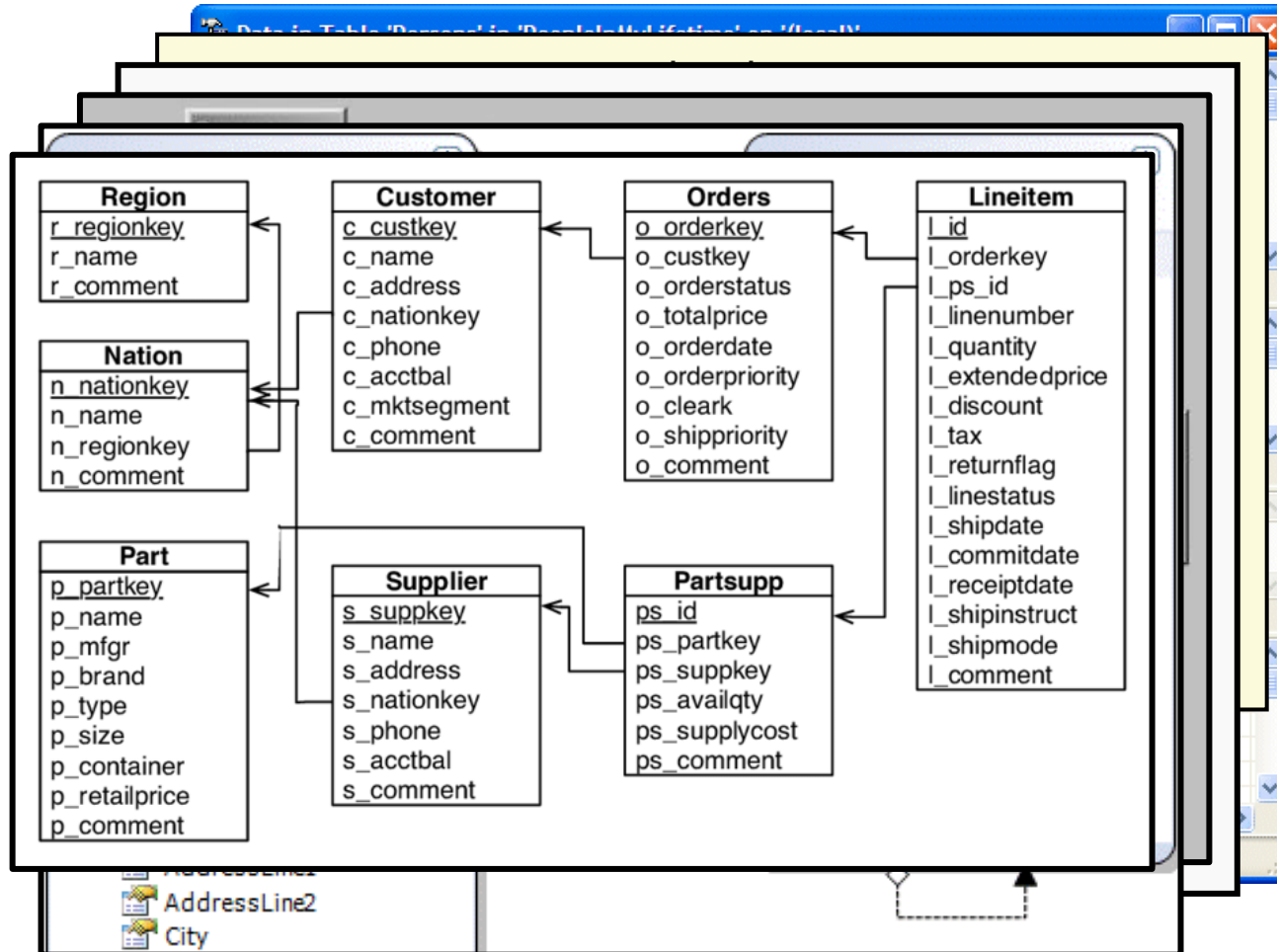




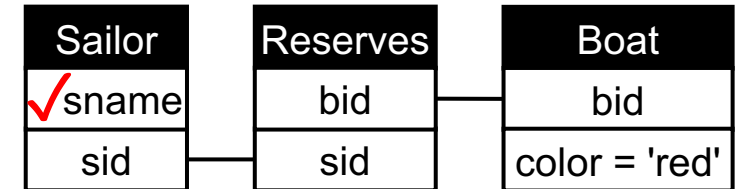
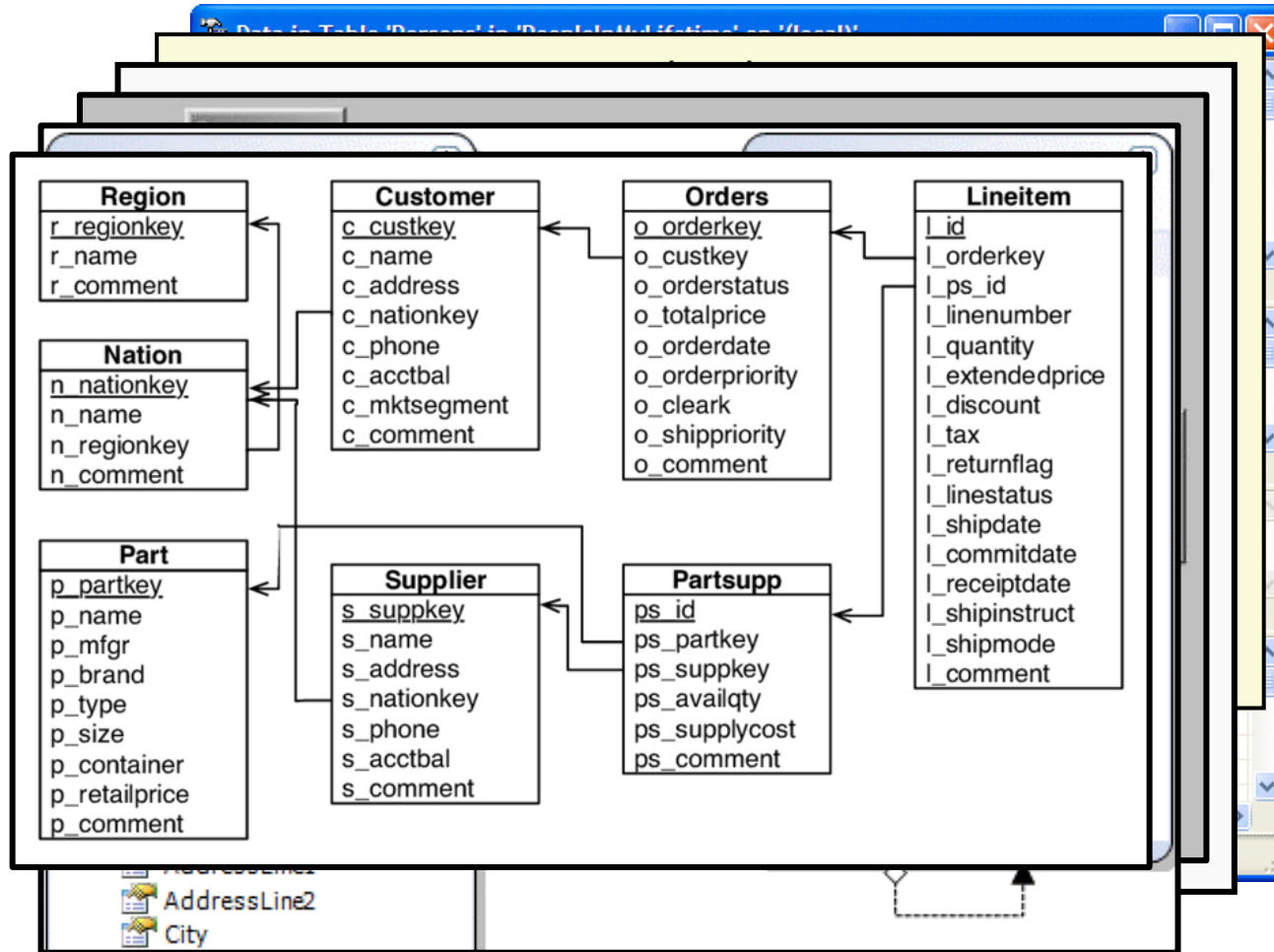
# P4: Existing visual metaphors as starting point



# P4: Existing visual metaphors as starting point



# P4: Existing visual metaphors as starting point



Q: "Find sailors who reserved a red boat."

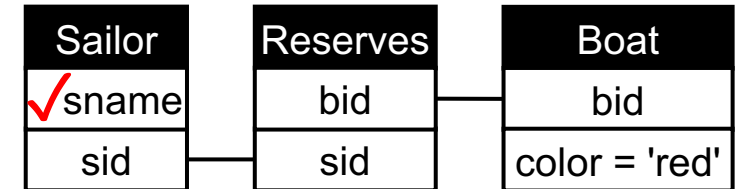
P4: Start from known visual UML metaphors for relational schemas

Conjunctive queries resemble schema notation with FK/PK constraints

# P5: Compositionality of the relational model

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red'] \}$$

## Datalog

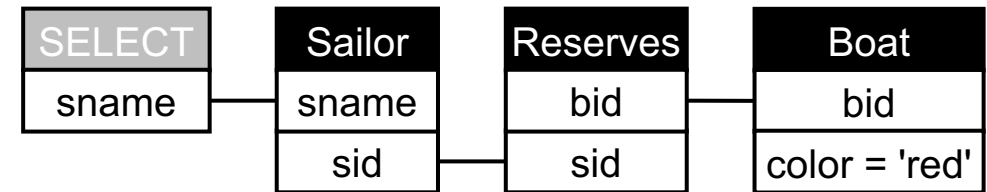
$Q(x) \text{ :- } \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, 'red', \_)$

# P5: Compositionality of the relational model

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

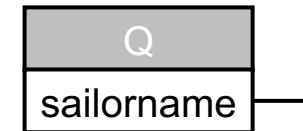
P5: Show the output relation



Relational queries are compositional:

- Input are relations (tables)
- Output are tables

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red']\}$$


Explicit output table  
also allow renaming of  
tables and attributes

## Datalog

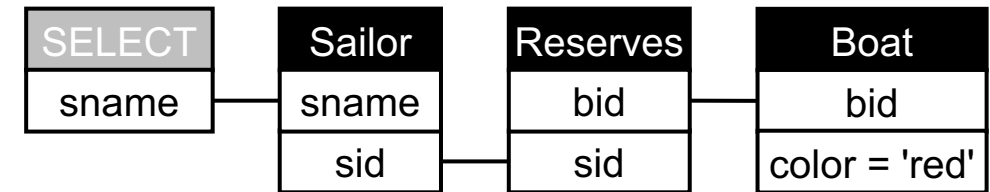
$Q(x) :- \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, 'red', \_)$

# P5: Compositionality of the relational model

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

P5: Show the output relation



Relational composition:

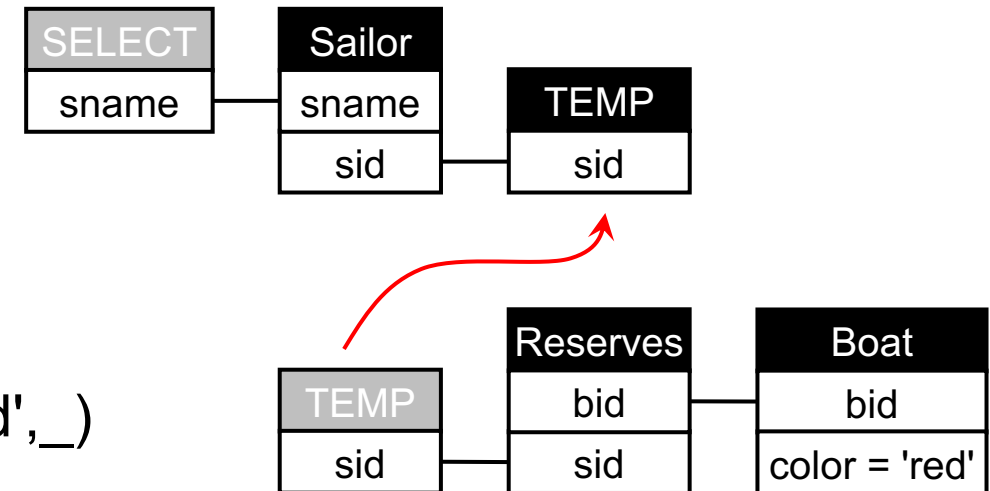
- One may want to use/define intermediate relations

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red'] \}$$

## Datalog

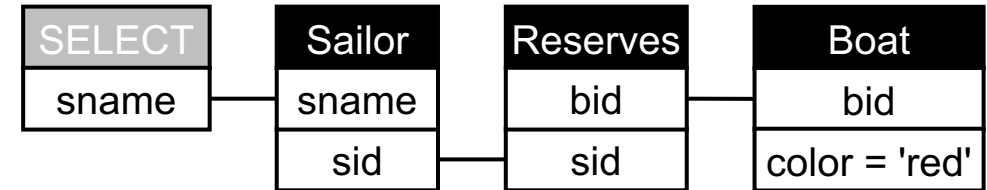
$Q(x) \text{ :- } \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, 'red', \_)$



# P6: Progressive visual complexity

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



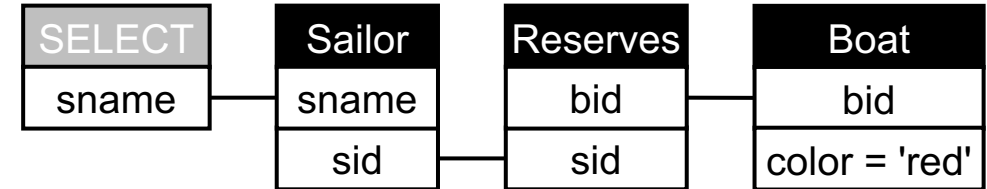
Q: "Find sailors who reserved only red boats."

?

# P6: Progressive visual complexity

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



+67% more SQL text

Q: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

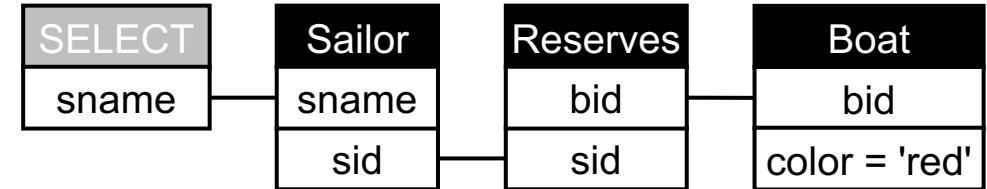


# P6: Progressive visual complexity

P6: Conjunctive queries are simplest, then gradually add visual metaphors

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

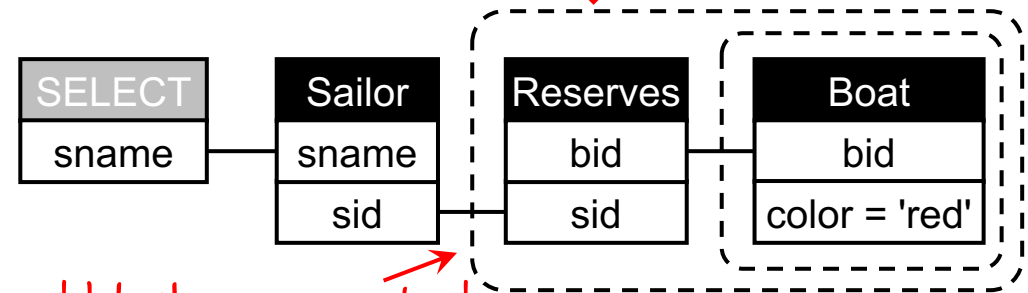


+67% more SQL text

Q: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
(select *
from Reserves R
where S.sid=R.sid
and not exists
(select *
from Boat B
where R.bid=B.bid
and color = 'red'))
```

+13% more  
"visual symbols"



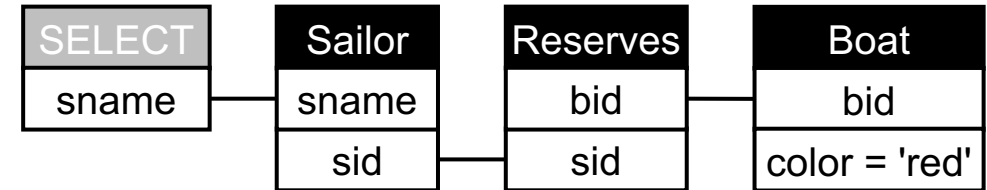
interpret query block with dashed block as negated

# P6: Progressive visual complexity

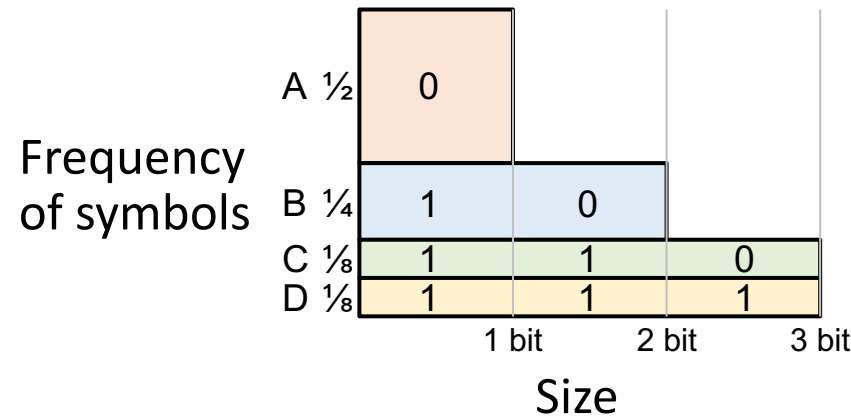
P6: Conjunctive queries are simplest, then gradually add visual metaphors

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



Variable-length entropy codes

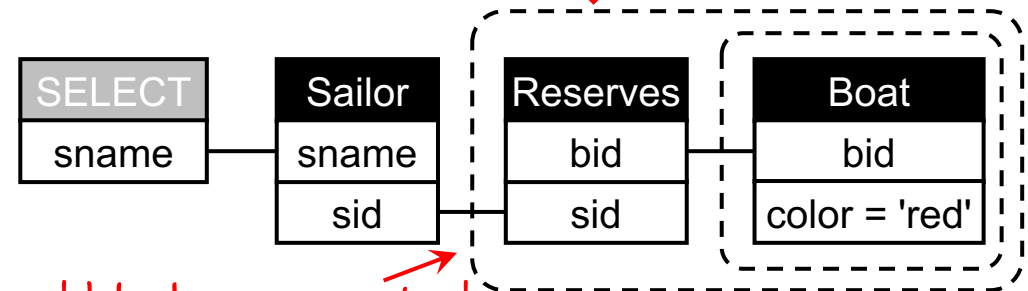


+67% more SQL text

Q: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
(select *
from Reserves R
where S.sid=R.sid
and not exists
(select *
from Boat B
where R.bid=B.bid
and color = 'red'))
```

+13% more "visual symbols"



interpret query block with dashed block as negated

# P7: Abstract away from syntax details

*Are these two SQL queries identical?*

```
select distinct S.sname  
from Sailor S, Reserves R  
where S.sid=R.sid
```

```
select distinct S.sname  
from Sailor S  
where exists (  
  select S.sname  
  from Reserves R  
  where S.sid=R.sid)
```

# P7: Abstract away from syntax details

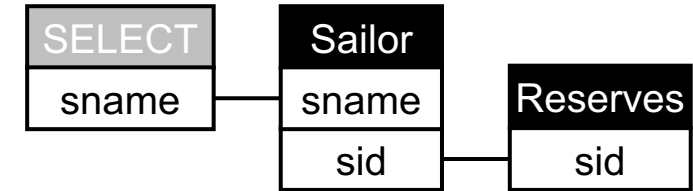
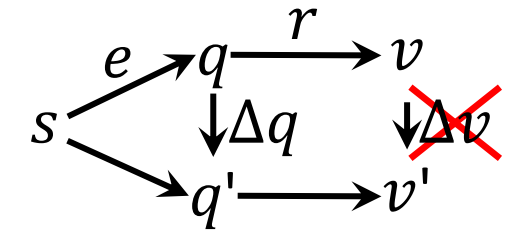
Q: "Find sailors who made some reservation."

```
select distinct S.sname
from Sailor S, Reserves R
where S.sid=R.sid
```

```
select distinct S.sname
from Sailor S
where exists (
  select S.sname
  from Reserves R
  where S.sid=R.sid)
```

These two SQL queries are identical!

P7. SYNTACTIC INVARIANCE



P7: Ignore peculiarities of SQL and focus on common logical core of relational queries

## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves} [q.\text{sname} = s.\text{sname} \wedge r.\text{sid} = s.\text{sid}]\}$$
$$\{q(\text{sname}) \mid \exists s \in \text{Sailor} [q.\text{sname} = s.\text{sname} \wedge \exists r \in \text{Reserves} [r.\text{sid} = s.\text{sid}]]\}$$

# P7: Abstract away from syntax details

Q: "Find sailors who made no reservation."

```
select distinct sname
from Sailor
where sid not in (
  select sid
  from Reserves R)
```

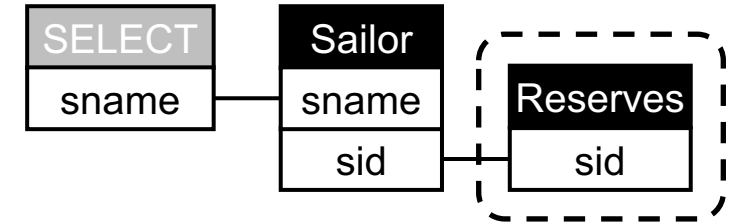
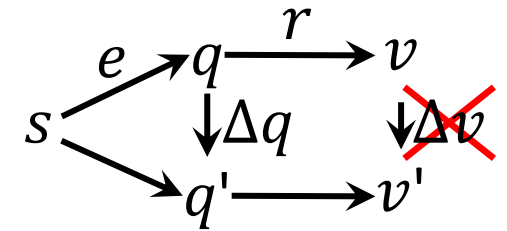
```
select distinct S.sname
from Sailor S
where not exists (
  select S.sname
  from Reserves R
  where S.sid=R.sid)
```

These two SQL queries are also identical  
(if R.sid contains no NULL value ...)

## TRC (Tuple Relational Calculus)

$$\{q(sname) \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \neg(\exists r \in \text{Reserves}[r.sid = s.sid])]\}$$

P7. SYNTACTIC INVARIANCE



P7: Ignore peculiarities of SQL  
and focus on common logical  
core of relational queries

# P8: Expose (and not hide) relational patterns

Reserves	
sid	
bid	

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2
   where R1.sid <> R2.sid
   and not exists
     (select *
      from Reserves R3
      where R3.sid = R2.sid
      and not exists
        (select *
         from Reserves R4
         where R4.sid = R1.sid
         and R4.bid = R3.bid)))
and not exists
  (select *
   from Reserves R5
   where R5.sid = R1.sid
   and not exists
     (select *
      from Reserves R6
      where R6.sid = R2.sid
      and R6.bid = R5.bid)))
```

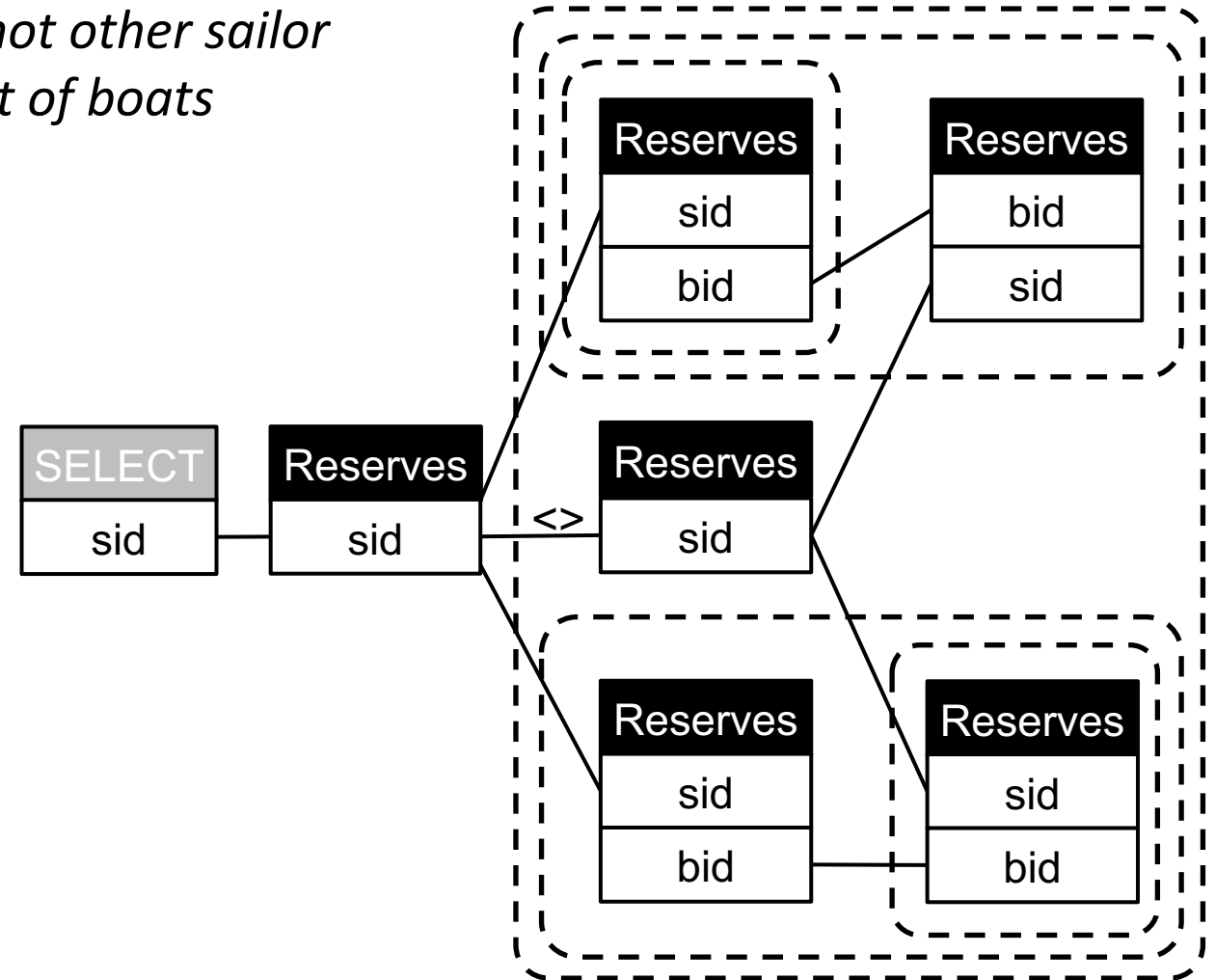


# P8: Expose (and not hide) relational patterns

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2
   where R1.sid <> R2.sid
   and not exists
     (select *
      from Reserves R3
      where R3.sid = R2.sid
      and not exists
        (select *
         from Reserves R4
         where R4.sid = R1.sid
         and R4.bid = R3.bid)))
and not exists
  (select *
   from Reserves R5
   where R5.sid = R1.sid
   and not exists
     (select *
      from Reserves R6
      where R6.sid = R2.sid
      and R6.bid = R5.bid)))
```

Q: "Find sailors with a unique set of reserved boats"

= Find sailors s.t. there is not other sailor that reserved the same set of boats

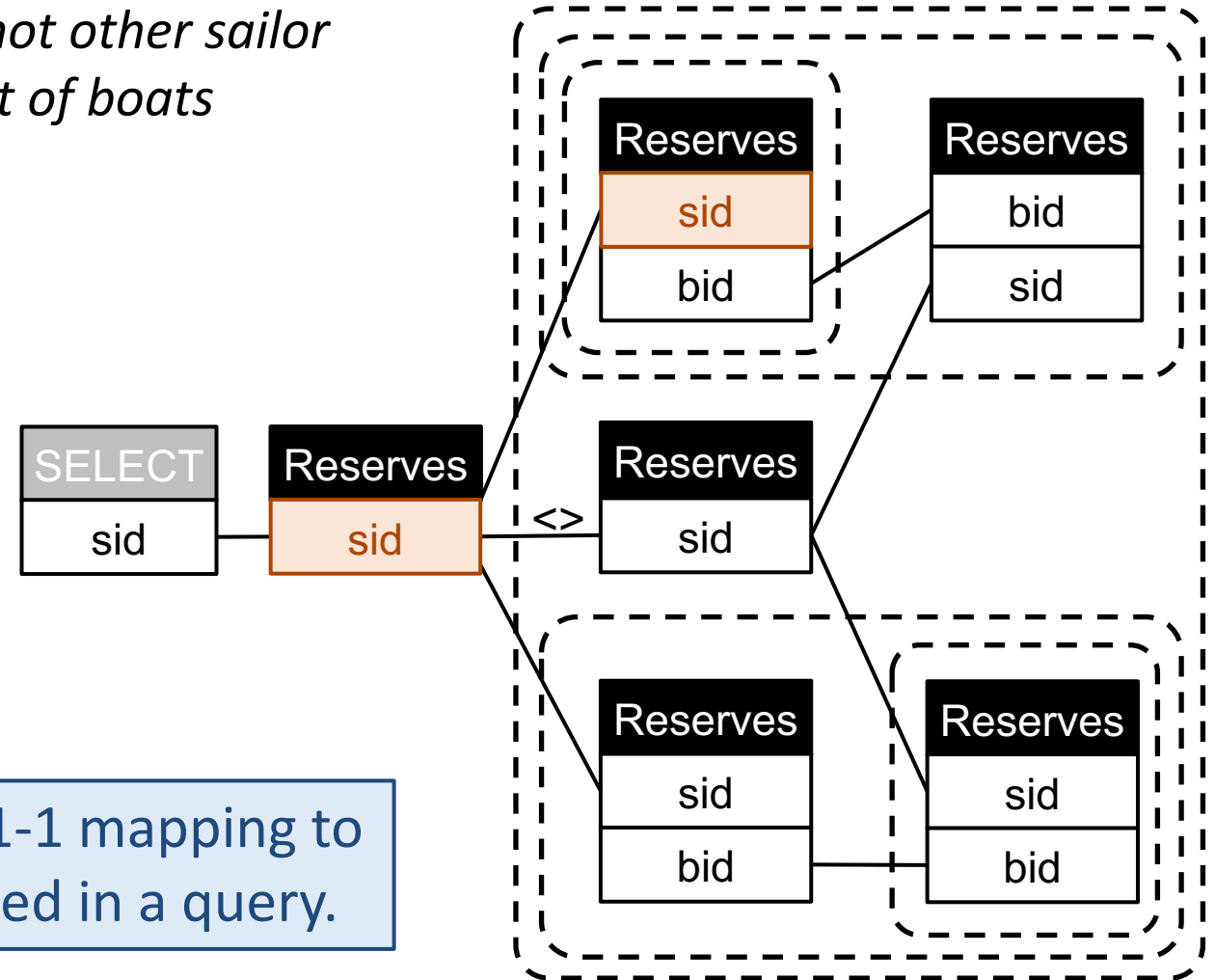


# P8: Expose (and not hide) relational patterns

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2
   where R1.sid <> R2.sid
   and not exists
     (select *
      from Reserves R3
      where R3.sid = R2.sid
      and not exists
        (select *
         from Reserves R4
         where R4.sid = R1.sid
         and R4.bid = R3.bid)))
and not exists
  (select *
   from Reserves R5
   where R5.sid = R1.sid
   and not exists
     (select *
      from Reserves R6
      where R6.sid = R2.sid
      and R6.bid = R5.bid)))
```

Q: "Find sailors with a unique set of reserved boats"

= Find sailors s.t. there is not other sailor that reserved the same set of boats





# P8: Expose (and not hide) relational patterns

*Are these two SQL queries identical?*

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2, Reserves R3
   where R2.sid = R3.sid
   and R2.bid < R3.bid
   and R2.sid = R1.sid)
```

```
select sid
from Reserves
group by sid
having count(distinct bid)=1
```

# P8: Expose (and not hide) relational patterns

Are these two SQL queries identical?

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2, Reserves R3
   where R2.sid = R3.sid
   and R2.bid < R3.bid
   and R2.sid = R1.sid)
```

```
select sid
from Reserves
group by sid
having count(distinct bid)=1
```

These two SQL queries give the same answers, but arguably use very different patterns (that goes beyond syntax). The underlying logic differs.

P8: Preserve a 1-1 mapping to the relations used in a query.

Contrast this principle with P7:  
"Abstract away from syntax details"

# P9: Minimal visual complexity

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname  
from Sailor S, Reserves R, Boat B  
where S.sid = R.sid  
and B.bid = R.bid  
and color = 'red'
```

SQL requires aliases for self-joins (i.e. repeated appearances of the same input table), which implies an inconvenient indirection to the database schema

Q(x) :- Sailor(y,x,\_,\_) Reserves(y,z,\_), Boat(z,\_, 'red', \_)

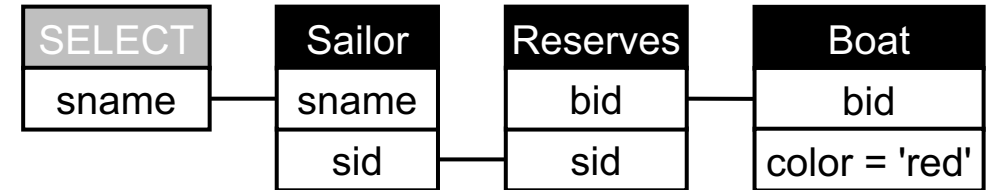
Datalog needs to show all attributes due to positional encoding (though it allows the use of "anonymous variables", via underscores)

# P9: Minimal visual complexity

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid = R.sid
and B.bid = R.bid
and color = 'red'
```

P9: Obey some kind of minimality criteria:  
only show information relevant for a query



- no aliases needed
- no need to show unused predicates

SQL requires aliases for self-joins (i.e. repeated appearances of the same input table), which implies an inconvenient indirection to the database schema

Q(x) :- Sailor(y,x,\_,\_) Reserves(y,z,\_), Boat(z,\_, 'red',\_)

Datalog needs to show all attributes due to positional encoding (though it allows the use of "anonymous variables", via underscores)

Only use as much "ink" as necessary

$$\text{Data-ink ratio} = \frac{\text{data-ink}}{\text{total ink used to print the graphic}}$$

= proportion of a graphic's ink devoted to the non-redundant display of data-information

# P10: Output-oriented reading order

*Q: "Find sailors who reserved a red boat."*

```
select distinct S.sname  
from Sailor S, Reserves R, Boat B  
where S.sid = R.sid  
and B.bid = R.bid  
and color = 'red'
```

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red']\}$$

## Datalog

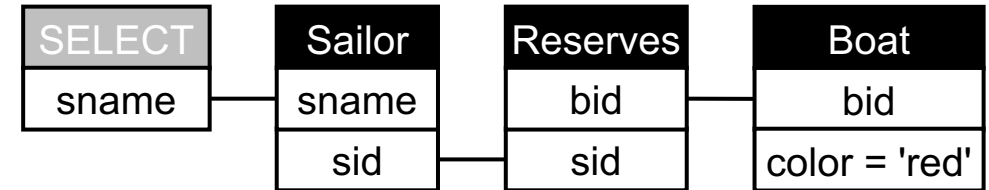
$Q(x) \text{ :- } \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, 'red', \_)$

# P10: Output-oriented reading order

P10: use an output-oriented reading order (as in SQL, Datalog, calculus)

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid = R.sid
and B.bid = R.bid
and color = 'red'
```



Start with the output on the left!

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red'] \}$$

## Datalog

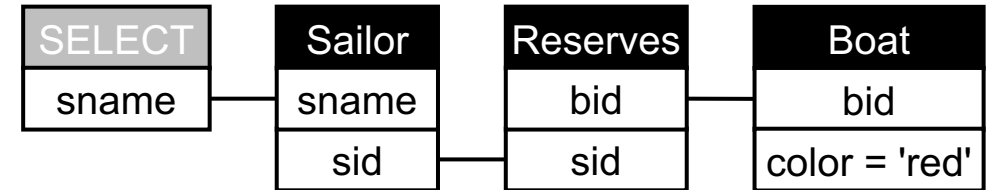
$Q(x) \text{ :- } \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, 'red', \_)$

# P10: Output-oriented reading order

P10: use an output-oriented reading order (as in SQL, Datalog, calculus)

Q: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid = R.sid
and B.bid = R.bid
and color = 'red'
```



Start with the output on the left!

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [ \\ q.sname = s.sname \wedge r.sid = s.sid \wedge \\ b.bid = r.bid \wedge b.color = 'red']\}$$

Notice that this is notably different from typical workflow visualizations!



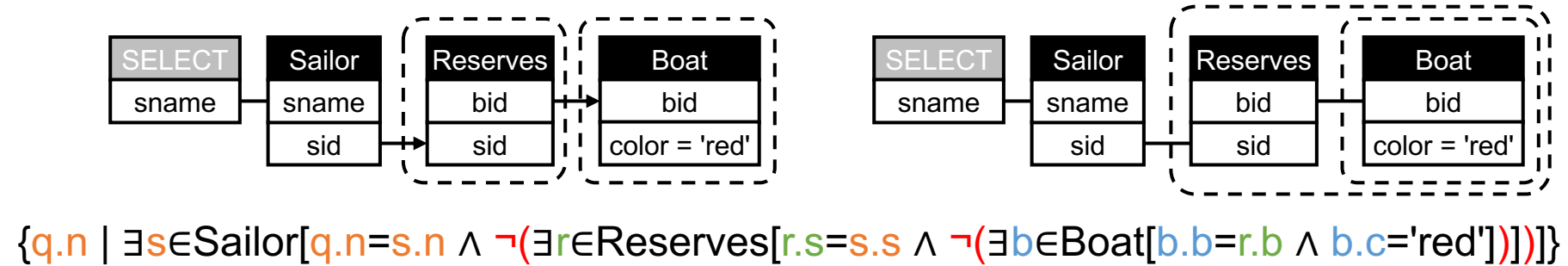
## Datalog

Q(x) :- Sailor(y,x,\_,\_), Reserves(y,z,\_), Boat(z,\_, 'red', \_)

# P11: Logic-based visual transformations

Q: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



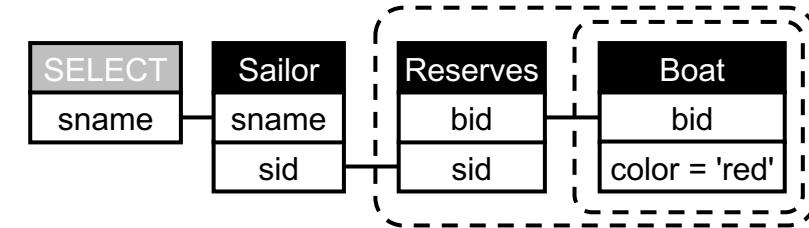
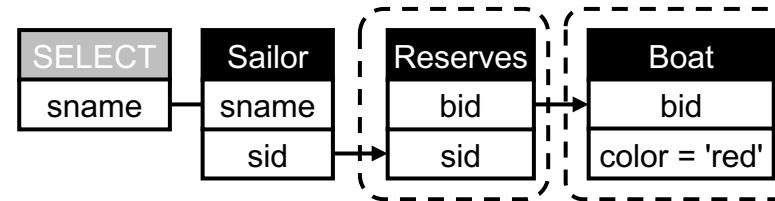


# P11: Logic-based visual transformations

P11: Allow limited visual transformations that help reading nested negations

Q: "Find sailors who reserved only red boats."

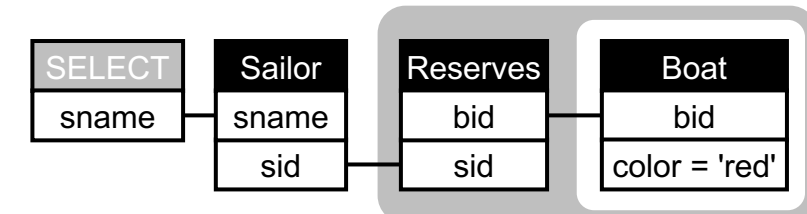
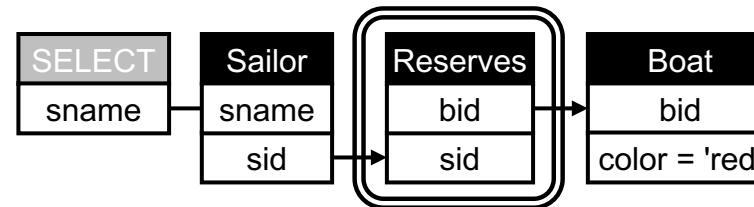
```
select distinct S.sname
from Sailor S
where not exists
(select *
 from Reserves R
 where S.sid=R.sid
 and not exists
 (select *
  from Boat B
  where R.bid=B.bid
  and color = 'red'))
```



$\{q.n \mid \exists s \in \text{Sailor}[q.n=s.n \wedge \neg(\exists r \in \text{Reserves}[r.s=s.s \wedge \neg(\exists b \in \text{Boat}[b.b=r.b \wedge b.c='red'])))]\}$

$\{q.n \mid \exists s \in \text{Sailor}[q.n=s.n \wedge (\forall r \in \text{Reserves}[r.s=s.s \rightarrow (\exists b \in \text{Boat}[b.b=r.b \wedge b.c='red'])))]\}$

Double negation in logic allows a rewriting and replacing with universal quantification



Double lines represent for all  $\forall$

Human perception can "manipulate" shaded areas without new symbols

# Intended Agenda today

Please leave  
feedback 😊



1. Why visualizing queries and why now?
2. Principles of Query Visualization
3. Logical foundations of relational query languages
4. (Early) Diagrammatic representations
5. Visual Query Representations (from DB community)
6. Lessons Learned and Open Challenges

# On the Unusual Effectiveness of Logic in Computer Science<sup>\*</sup>

Joseph Y. Halpern<sup>†</sup>

Robert Harper<sup>‡</sup>

Neil Immerman<sup>§</sup>

Phokion G. Kolaitis<sup>¶</sup>

Moshe Y. Vardi<sup>||</sup>

Victor Vianu<sup>\*\*</sup>

THE  
BULLETIN OF  
SYMBOLIC  
LOGIC

## 3 Logic as a Database Query Language

The database area is an important area of computer science concerned with storing, querying and updating large amounts of data. Logic and databases have been intimately connected since the birth of database systems in the early 1970's. Their relationship is an unqualified success story. Indeed, first-order logic (FO) lies at the core of modern database systems, and the standard query languages such as *Structured Query Language* (SQL) and *Query-By-Example* (QBE) are syntactic variants of FO. More powerful query languages are based on extensions of FO with recursion, and are reminiscent of the well-known fixpoint queries studied in finite-model theory (see Section 2). The impact of logic on databases is one of the most striking examples of the effectiveness of logic in computer science.

# Towards a principled comparison of visual metaphors

- Our goal is to highlight similarities and differences of various visual query representations.
- To achieve a unified comparison of visual formalisms, we will represent a consistent yet diverse set of queries from the fragment of first order logic (FOL) with equalities.
- We give these queries in different textual QLs since various visual formalisms align more naturally with different textual QL:
  - Relational Algebra (RA)
  - Relational Calculus (RC): Domain RC (DRC) vs. Tuple RC (TRC)
  - Datalog
  - SQL, restricted to a limited fragment and set semantics

# Part 3: Logical Foundations of Relational Query Languages

## Sailor queries (for Part 5)

- 1 practical database schema (sailors-reserve-boats)
- 5 queries (with variants) in 5 slides
- Each query in 5 Query Languages (QLs)

## Monadic predicate calculus = unary predicates (for Part 4)

- 1 abstract schema  $(R, S)$
- 4 queries in 4 slides
- Each statement in 5 textual and 3 visual QLs

# Query 1

We focus on set semantics (which is the semantics in logics and algebra)

Schema

Boat
<u>bid</u>
bname
color
pdate

Q1: "Find boats that are red or blue."

```
select distinct bname
from Boat
where color = 'red'
or color = 'blue'
```

Q1a: "Find boats that are red."

Q1b: "Find boats that are not red."

Q1c: "Find boats that are red or blue and purchased before 1980."

Comparison predicate

## TRC (Tuple Relational Calculus)

$$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge (b.\text{color} = \text{'red'} \vee b.\text{color} = \text{'blue'})]\}$$

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists y, z, u [\text{Boat}(z, x, y, u) \wedge (y = \text{'red'} \vee y = \text{'blue'})]\}$$
$$\{(x) \mid \exists y [\text{Boat}(\_, x, y, \_) \wedge (y = \text{'red'} \vee y = \text{'blue'})]\}$$

Anonymous variables are possible in both DRC and Datalog

## Datalog

$Q(x) \text{ :- Boat}(\_, x, \text{'red'}, \_)$   
 $Q(x) \text{ :- Boat}(\_, x, \text{'blue'}, \_)$

$Q(x) \text{ :- Boat}(\_, x, y, \_), (y = \text{'red'}; y = \text{'blue'})$

Disjunctions in Datalog are not standard but used in some Datalog implementations like Souffle (see <https://souffle-lang.github.io/rules#disjunction>)

## Relational Algebra

$$\sigma_{\text{color} = \text{'red'} \vee \text{color} = \text{'blue'}} B$$

# Query 2

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid = R.sid
and B.bid = R.bid
and color = 'red'
```

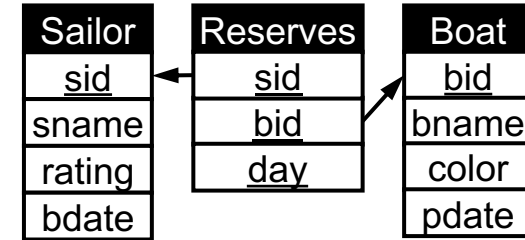
## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \\ \exists b \in \text{Boat} [q.\text{sname} = s.\text{sname} \wedge \\ r.\text{sid} = s.\text{sid} \wedge b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}]\}$$

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v, z, w, y, t, u, s [\text{Sailor}(v, x, z, w) \wedge \\ \text{Reserves}(v, y, t) \wedge \\ \text{Boat}(y, u, \text{'red'}, s)]\}$$

## Schema



## Datalog

Q2a: "Find sailors and red boats they reserved."

$$Q(x) \text{ :- } \text{Sailor}(y, x, \_, \_), \text{Reserves}(y, z, \_), \text{Boat}(z, \_, \text{'red'}, \_)$$

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie R \bowtie \sigma_{\text{color}=\text{'red'}}B)$$



# Query 3

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
(select *
from Reserves R
where S.sid = R.sid
and not exists
(select *
from Boat B
where R.bid = B.bid
and color = 'red'))
```

Q3a: "Find sailors who reserved no boat."

Q3b: "Find sailors who reserved no red boat."

## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor} [q.\text{sname} = s.\text{sname} \wedge \\ \neg(\exists r \in \text{Reserves} [r.\text{sid} = s.\text{sid} \wedge \\ \neg(\exists b \in \text{Boat} [b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}])])]\}$$

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v, z, w [\text{Sailor}(v, x, z, w) \wedge \\ \neg(\exists y, t [\text{Reserves}(v, y, t) \wedge \\ \neg(\exists u, s [\text{Boat}(y, u, \text{'red'}, s)])])]\}$$

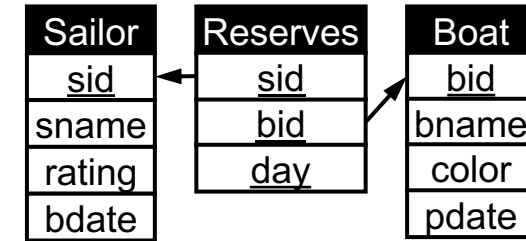
## Non-recursive Datalog with negation

```
RedBoat(z) :- Boat(z, _, 'red', _)
BadSid(y) :- Reserves(y, z, _), not RedBoat(z)
Q(x) :- Sailor(y, x, _, _), not BadSid(y)
```

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - \pi_{\text{sid}}(R \bowtie \sigma_{\text{color}=\text{'red'}} B)))$$
$$\pi_{\text{sname}}(S \bar{\bowtie} \pi_{\text{sid}}(R \bowtie \sigma_{\text{color}=\text{'red'}} B))$$

## Schema



Datalog requires an intermediate view due to safety conditions

BadSids: sailors who reserved some non-red boat

Antijoin operator (also anti-semijoin)

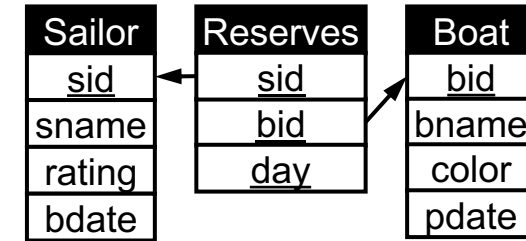


# Query 4

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
(select *
from Boat B
where color = 'red'
and not exists
(select *
from Reserves R
where S.sid = R.sid
and R.bid = B.bid))
```

Schema



## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor} [q.\text{sname} = s.\text{sname} \wedge \neg(\exists b \in \text{Boat} [b.\text{color} = \text{'red'} \wedge \neg(\exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])))]\}$$

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v, z, w [\text{Sailor}(v, x, z, w) \wedge \neg(\exists y, u, s [\text{Boat}(y, u, \text{'red'}, s) \wedge \neg(\exists t [\text{Reserves}(v, y, t)])])]\}$$

BadSids: sailors who have not reserved all red boats.

## Non-recursive Datalog with negation

```
ReserveOne(y,z) :- Reserves(y,z,_)  
BadSid(y) :- Sailor(y,_,_,_), Boat(z,_,\text{'red'},_), not ReserveOne(y,z)  
Q(x) :- Sailor(y,x,_,_), not BadSid(y)
```

Datalog requires another Sailor relation!

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - \pi_{\text{sid}}((\pi_{\text{sid}} S \times \pi_{\text{bid}} \sigma_{\text{color}=\text{'red'}} B) - \pi_{\text{sid,bid}} R)))$$
$$\pi_{\text{sname}}(S \bar{\bowtie} \pi_{\text{sid}}((S \times \sigma_{\text{color}=\text{'red'}} B) \bar{\bowtie} \pi_{\text{sid,bid}} R)))$$

Notice the cross product!

# Query 5

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

## TRC (Tuple Relational Calculus)

$$\{q(\text{bid}, \text{bname}) \mid \exists b \in \text{RedBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}] \vee \exists b \in \text{BlueBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}]\}$$

## DRC (Domain Relational Calculus)

$$\{(x, y) \mid \exists z [\text{RedBoat}(x, y, z) \vee \text{BlueBoat}(x, y, z)]\}$$

## Non-recursive Datalog with negation

$$Q(x, y) \text{ :- RedBoat}(x, y, \_)$$
$$Q(x, y) \text{ :- BlueBoat}(x, y, \_)$$

## Relational Algebra

$$\pi_{\text{bid}, \text{bname}}(\text{RedBoat} \cup \text{BlueBoat})$$

← Algebra requires the union operator

## Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

# Part 3: Logical Foundations of Relational Query Languages

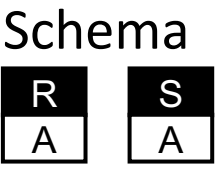
Sailor queries (for Part 5)

- 1 practical database schema (sailors-reserve-boats)
- 5 queries (with variants) in 5 slides
- Each query in 5 Query Languages (QLs)

Monadic predicate calculus = unary predicates (for Part 4)

- 1 abstract schema (R, S)
- 4 queries in 4 slides
- Each statement in 5 textual and 3 visual QLs

# Statement 6: Monadic FOL (= only unary predicates)



*S6: "Some R is not S."*

```
select exists
(select *
from R
where not exists
(select *
from S
where R.A = S.A))
```

TRC (Tuple Relational Calculus)

$\exists r \in R [\neg(\exists s \in S [r.A = s.A])]$

DRC (Domain Relational Calculus)

$\exists x [R(x) \wedge \neg S(x)]$

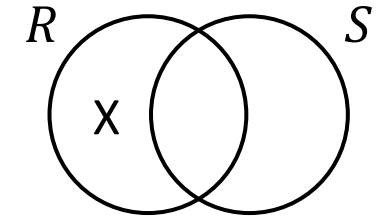
Datalog w/ inequalities

$Q() :- R(x), \text{not } S(x)$

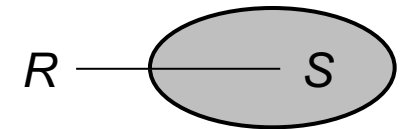
Relational Algebra

$\pi_{\emptyset}(R - S)$

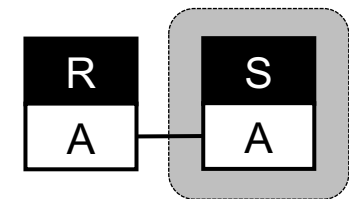
Venn-Peirce diagram



Beta Existential Graph



Relational Diagram

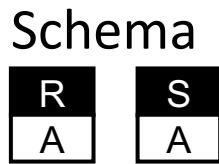


We will discuss  
these visual  
formalisms in  
detail later

"Statements" are Boolean  
queries (the answer is  
true or false).

"Monadic" means that all  
predicates are unary

# Statement 7: Monadic FOL with equalities



S7: "There is exactly one R."

```
select exists
(select *
from R
where not exists
(select *
from R R2
where R.A <> R2.A))
```

TRC (Tuple Relational Calculus)

$$\exists r \in R [\neg(\exists r2 \in R [r.A \neq r2.A])]$$

DRC (Domain Relational Calculus)

$$\begin{aligned} \exists x [R(x) \wedge \neg(\exists x [R(y) \wedge x \neq y])] \\ \exists x [R(x) \wedge \forall x [R(y) \rightarrow x = y]] \end{aligned}$$

Datalog w/ inequalities

$$I(x) :- R(x), R(y), x \neq y$$

$$Q() :- R(x), \text{not } I(x)$$

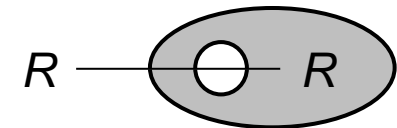
Relational Algebra

$$\pi_{\emptyset}(R - \pi_A(\sigma_{A \neq B}(R \times \rho_{A \rightarrow B}(R))))$$

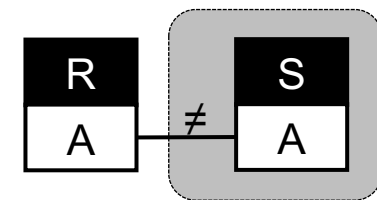
Venn-Peirce diagram

Venn diagrams can't  
handle (in)equalities

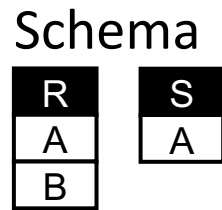
Beta Existential Graph



Relational Diagram



# Statement 8: Polyadic FOL



*S8: "There is some R.B that occurs with some R.A that is not in S."*

```
select exists
(select *
from R
where not exists
(select *
from S
where R.A = S.A))
```

TRC (Tuple Relational Calculus)  
 $\exists r \in R [\neg(\exists s \in S [r.A = s.A])]$

DRC (Domain Relational Calculus)  
 $\exists x, y [R(y, x) \wedge \neg S(x)]$

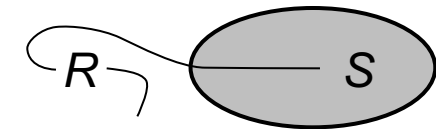
Datalog w/ inequalities  
 $Q() :- R(y, x), \text{ not } S(x)$

Relational Algebra  
 $\pi_{\emptyset}(\pi_A(R) - S)$

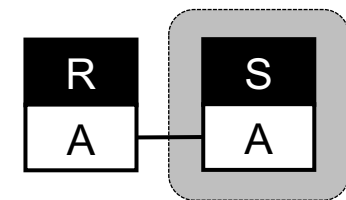
Venn-Peirce diagram

Venn diagrams can't  
handle polyadic logic

Beta Existential Graph



Relational Diagram



# Query 9: Polyadic FOL w/ free variables (= queries)

Schema

R	S
A	A
B	

Q9: "Find R.B that has some R.A that is not in S."

```
select distinct R.B
from R
where not exists
  (select *
   from S
   where R.A = S.A)
```

TRC (Tuple Relational Calculus)

$\{q(B) \mid \exists r \in R [q.B = r.B \wedge \neg(\exists s \in S [r.A = s.A])]\}$

DRC (Domain Relational Calculus)

$\{(y) \mid \exists x [R(x,y) \wedge \neg S(x)]\}$

Datalog w/ inequalities

$Q(y) :- R(y, x), \text{ not } S(x)$

Relational Algebra

$R - (S \times \pi_B R)$

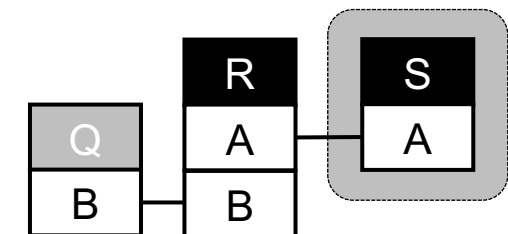
Venn-Peirce diagram

Venn diagrams can't  
handle polyadic logic,  
nor free variables

Beta Existential Graph

Beta EGs can't handle  
free variables

Relational Diagram



# Intended Agenda today

Please leave  
feedback 😊



1. Why visualizing queries and why now?
2. Principles of Query Visualization
3. Logical foundations of relational query languages
4. (Early) Diagrammatic representations
5. Visual Query Representations (from DB community)
6. Lessons Learned and Open Challenges



## Part 4: (Early) diagrammatic representations

- We next look at various visual representations for logical statements that were proposed from \*outside\* the database community, sometimes referred to as the "diagrammatic reasoning" community.
- The attempt to express simple statements (a famous example: "All men are mortal") and to reason based on visual representations predates the database community (and even the formal development of first-order logic) by centuries. But we are trying to bring a "database perspective."

# Part 4: Early Diagrammatic Representations

Monadic predicate calculus (Boolean queries & unary predicates)

1. Euler Circles (1768)
2. Venn Diagrams (1880)
3. Venn-Peirce Diagrams (~1896)
4. Venn-Peirce-Shin Diagrams (1995)

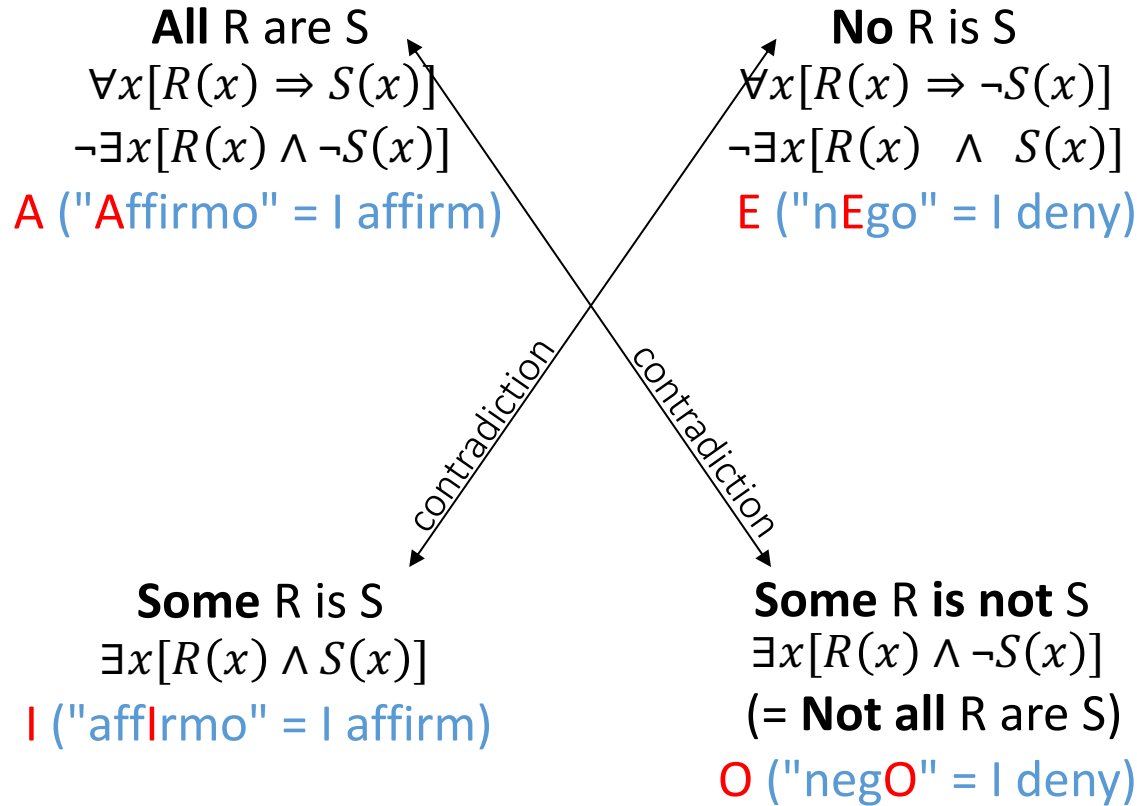
Polyadic predicate calculus (allowing predicates with arities  $\geq 2$ )

7. Peirce Beta Existential Graphs (~1909)
8. Conceptual graphs (1976)
9. String diagrams (2024)

# 4 categorical propositions / square of opposition

S... subject  
P... predicate

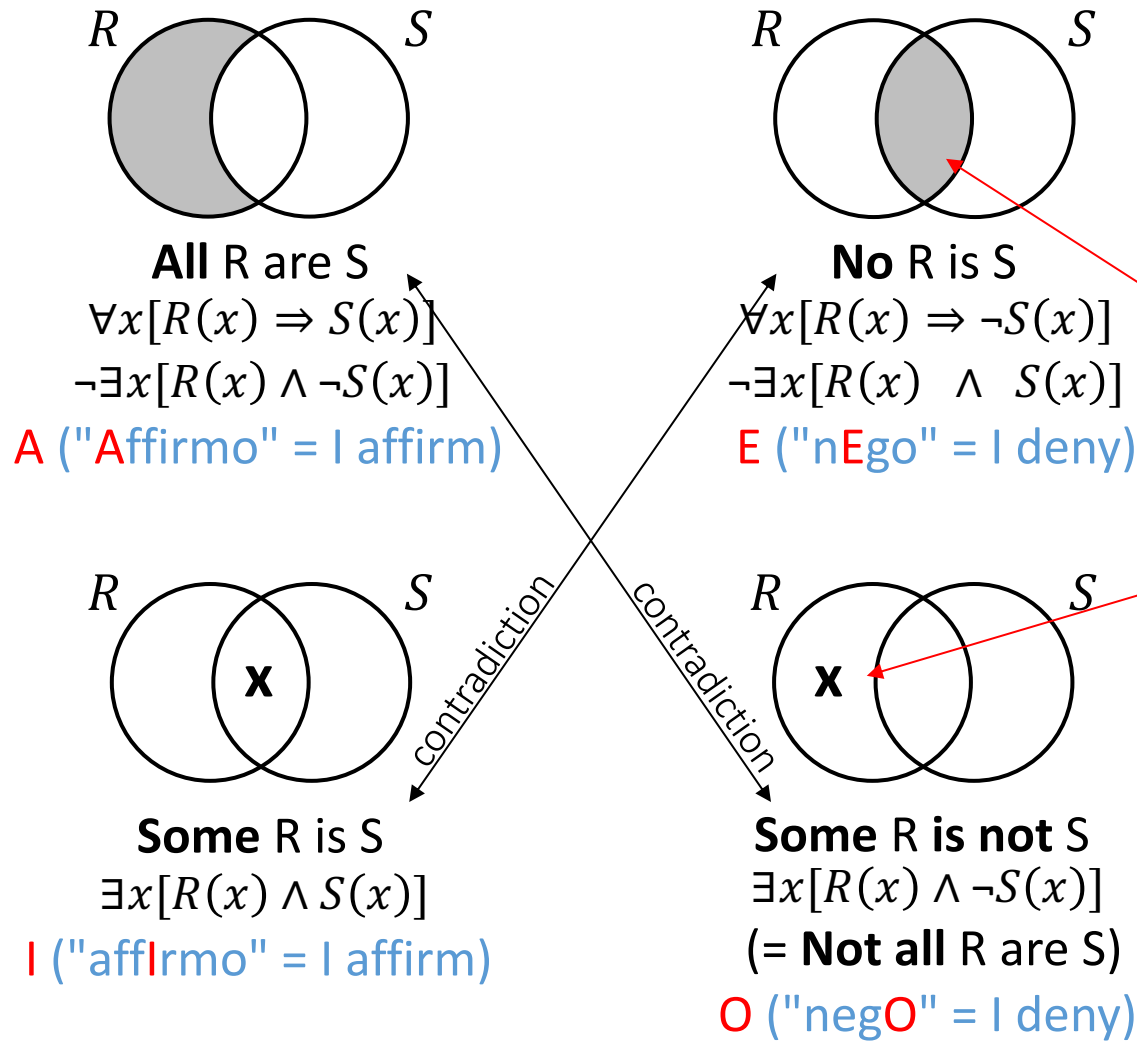
Universal  
propositions



Particular  
propositions

# 4 categorical propositions / square of opposition

S... subject  
P... predicate



Universal  
propositions

Venn-Peirce-Shin: shaded areas are empty, "x" shows that something exists

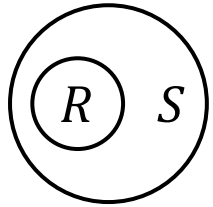
Particular  
propositions

# Euler Circles (1768)

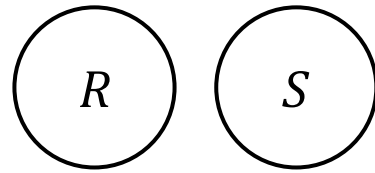
## Sources used:

- Euler, Lettres à une princesse d'Allemagne sur divers sujets de physique et de philosophie, 1770. <https://www.e-rara.ch/zut/content/zoom/2380256>, <https://doi.org/10.3931/e-rara-8642>
  - "Letters to a German Princess, On Different Subjects in Physics and Philosophy (French: Lettres à une princesse d'Allemagne sur divers sujets de physique et de philosophie) were a series of 234 letters written by the mathematician Leonhard Euler between 1760 and 1762 addressed to Friederike Charlotte of Brandenburg-Schwedt and her younger sister Louise ... The first two volumes of the 234 letters originally written in French appeared in print in Saint Petersburg in 1768 and the third in Frankfurt in 1774. The letters were later reprinted in Paris with the first volume in 1787, the second in 1788 and the third in 1789" [https://en.wikipedia.org/wiki/Letters\\_to\\_a\\_German\\_Princess](https://en.wikipedia.org/wiki/Letters_to_a_German_Princess)
  - Shin. The logical status of diagrams. 1995. <https://doi.org/10.1017/CBO9780511574696>
- Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Euler: 4 categorical sentences

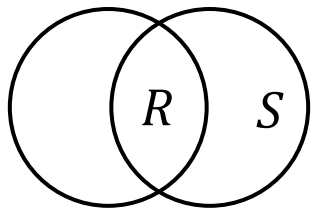


**A All R are S**  
 $\forall x[R(x) \Rightarrow S(x)]$



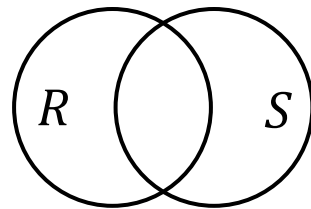
**O No R is S**  
 $\forall x[R(x) \Rightarrow \neg S(x)]$

Euler's 1<sup>st</sup> problem: A and O are contradictory.  
But that contradiction is not visible in an obvious way



**I Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

ambiguous!

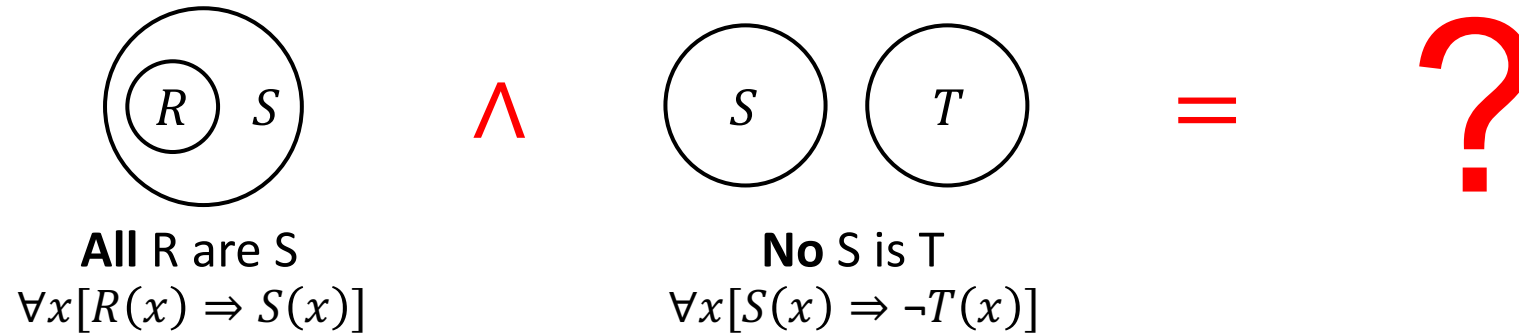


**O Some R is not S**  
 $\exists x[R(x) \wedge \neg S(x)]$

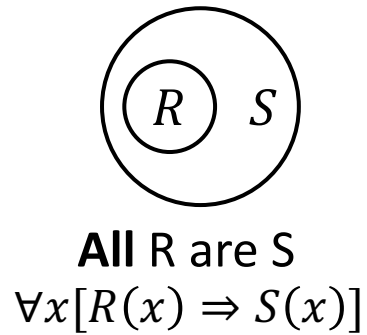
Euler's 2<sup>nd</sup> problem: "unclear representation of existential statements": A part of concept R is located outside of concept S (but also the other way around)

contradiction

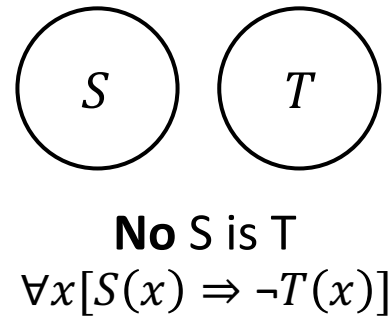
# Euler: Application for syllogistic reasoning



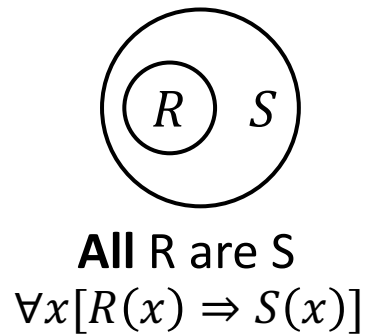
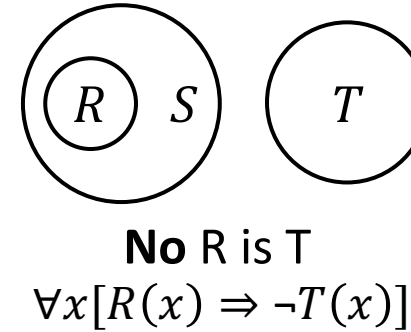
# Euler: Application for syllogistic reasoning



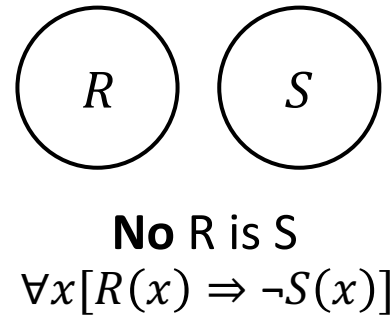
$\wedge$



$=$



$\wedge$

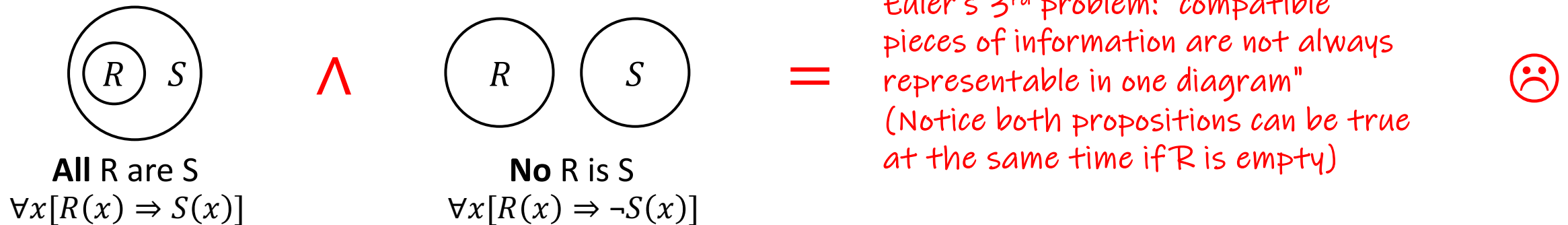
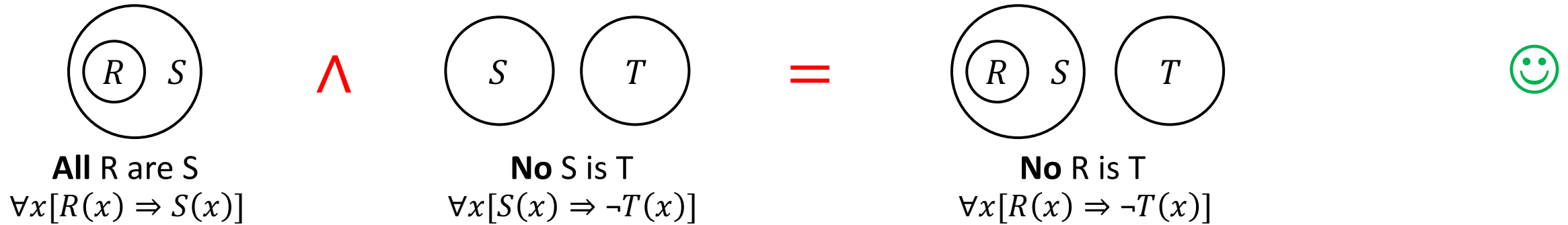


$=$





# Euler: Application for syllogistic reasoning



# Euler (1770)

Some  $A$  is not  $B$

IV. Pour les propositions négatives particulières, comme quelque  $A$  n'est pas  $B$ , une partie de l'espace  $A$  doit se trouver hors de l'espace  $B$ , comme



qui convient bien avec la précédente; mais on remarque ici principalement, qu'il y a quelque chose dans la notion  $A$ , qui n'est pas compris dans la notion  $B$ , ou qui se trouve hors de cette notion.

le 14 *Fevrier* 1761.

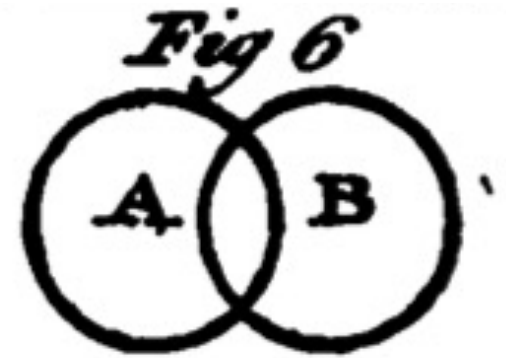
# Euler, Hunter (1802)



Let, then, the first proposition, affirmative, and particular, be expressed in this general form.

*Some A is B. (Plate I. fig. 5.)*

in which a part of the notion A is contained in the notion B.



Let us finally suppose, that the first proposition is negative and particular, namely,

*Some A is not B.*

It is represented in *plate II. fig. 8.* in which part of notion A is out of notion B.

Fig 6 / Fig 8: there seems to be an indexing error (?)

# Venn Diagrams (1880)

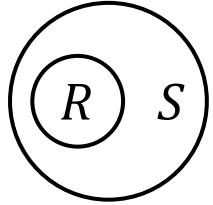
Sources used:

- Venn. On the diagrammatic and mechanical representation of propositions and reasonings, 1880. <https://doi.org/10.1080/14786448008626877>
- Venn. Symbolic logic, Macmillan, 1881. <https://archive.org/details/symboliclogic00vennia/>
- Shin. The logical status of diagrams. 1995. <https://doi.org/10.1017/CBO9780511574696>

# Venn

**All R are S**

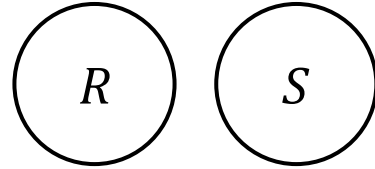
$$\forall x[R(x) \Rightarrow S(x)]$$



Euler

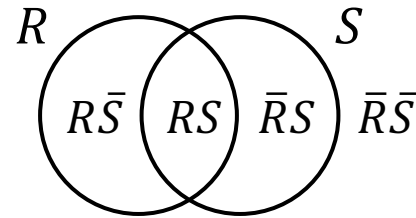
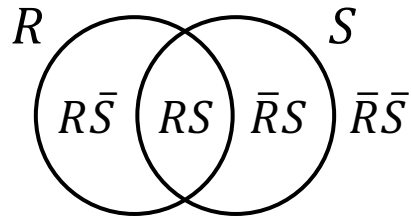
**No R is S**

$$\forall x[R(x) \Rightarrow \neg S(x)]$$

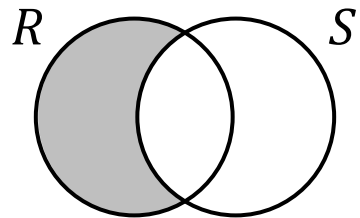


VENN mainly concerned with representing multiple pieces of information conjunctively in one diagram (Euler's 3<sup>rd</sup> problem)

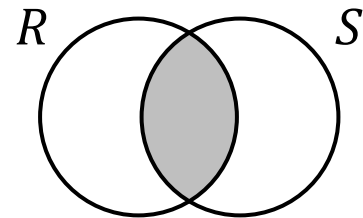
Key problem with Euler: does not allow partial information / uncertainty of information



Idea Venn: start with primary diagram



Venn

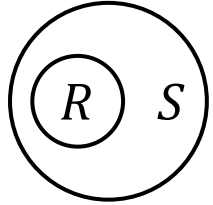


Shading as new syntactic device:  
"All, then, that we have to do is to scratch out that subdivision (that is not possible)"

# Venn: showing concurrent information

**All** R are S

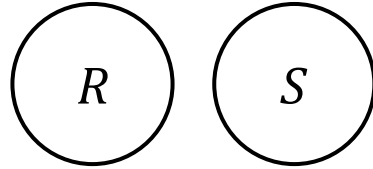
$$\forall x[R(x) \Rightarrow S(x)]$$



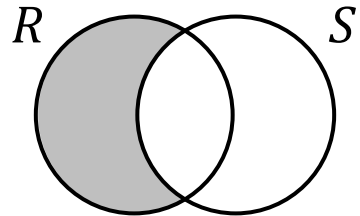
$\wedge$

**No** R is S

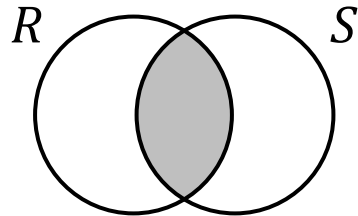
$$\forall x[R(x) \Rightarrow \neg S(x)]$$



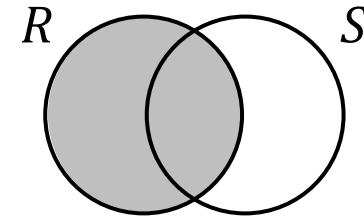
$=$



$\wedge$



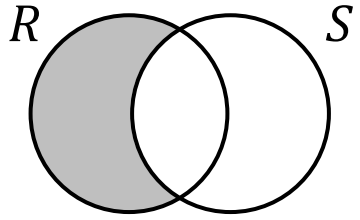
$=$



$$\neg \exists x[R(x)]$$

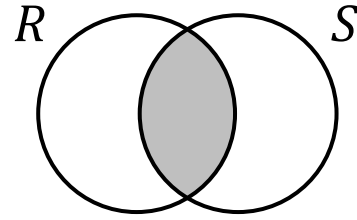


# Venn: 4 categorical sentences



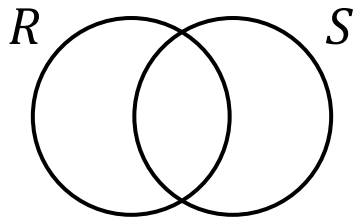
**All R are S**

$$\forall x[R(x) \Rightarrow S(x)]$$



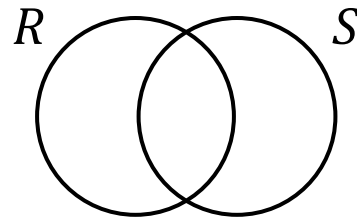
**No R is S**

$$\forall x[R(x) \Rightarrow \neg S(x)]$$



**Some R is S**

$$\exists x[R(x) \wedge S(x)]$$



**Some R is not S**

$$\exists x[R(x) \wedge \neg S(x)]$$

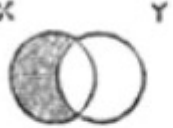
VENN overcame Euler's 3<sup>rd</sup> problem: representing multiple pieces of non-contradicting information conjunctively in one diagram

However, VENN did not overcome Euler's 1<sup>st</sup> problem: ambiguous representation of existential statements


(next: how Pierce solved that)

# Venn (1880)

The method of employing the diagrams in order to express propositions will readily be understood. It is merely this:— Ascertain what each given proposition denies, and then put some kind of mark upon the corresponding partition in the figure. The most effective means of doing this is just to shade it out. For instance, the proposition “All X is Y” is interpreted to mean that there is no such class of things in existence as “X that is not-Y” or  $X\bar{Y}$ . All, then, that we have to do is to scratch out that subdivision in the two-circle figure,

thus, . If we want to represent “All X is all Y,”

we take this as adding on another denial, viz. that of  $\bar{X}Y$ , and

we proceed to scratch out that division also, thus, 




# Venn (1880)

The main characteristic of this scheme, viz. the facility with which it enables us to express each separate accretion of knowledge, and so to break up any complicated group of data, and attack them in detail, will begin to show itself even in such a simple instance as this. On the common plan we should have to begin again with a new figure in each case respectively, viz. for “All X is Y,” and “All X is all Y;” whereas here we use the same figure each time, merely modifying it in accordance with the new information. Or take the disjunctive “All X is either Y or Z.” It is very seldom even attempted to represent this diagrammatically (and then, so far as I have seen, only if the alternatives are mutually exclusive); but it is readily enough exhibited when we regard it as merely extin-

guishing any X that is neither Y nor Z—thus,



If to this were added the statement that “none but the X's are either Y or Z,” we should then abolish the XY and the XZ,

and have . Scratch out, again, the XYZ compart-

ment, and we have made our alternatives exclusive; *i. e.* the X is then Y or Z *only*.

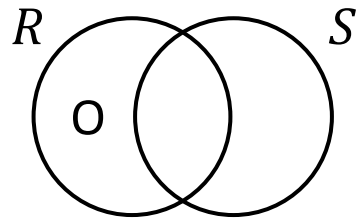
Of course the same plan is easy to adopt with any number of premises. Our first data abolish, say, such and such classes. This is final; for, as already intimated, all the resultant elementary denials which our propositions yield must be regarded as absolute and unconditional. This first step then leaves the field open to any similar accession of knowledge from the next data; and so more classes are swept away. Thus we go on till all the data have had their fire; and the muster-roll at the end will show what classes may be taken as surviving. If, therefore, we simply shade out the compartments in our figure which have thus been successively proved to be empty, nothing is easier than to go on doing this till all the information yielded by the data is exhausted.

# Venn-Peirce (~1896)

Sources used:

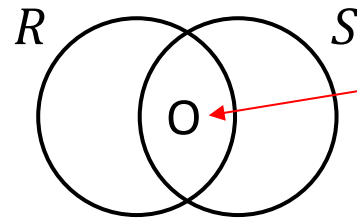
- Peirce. Collected Papers of Charles Sanders Peirce. Volumes 3 and 4. 1933. Paragraphs 4.350 – 4.371. [https://archive.org/details/collectedpaperso0000unse\\_r5j9/](https://archive.org/details/collectedpaperso0000unse_r5j9/)
- Shin. The logical status of diagrams. 1995. <https://doi.org/10.1017/CBO9780511574696>

# Venn-Peirce: 4 categorical sentences



**All R are S**

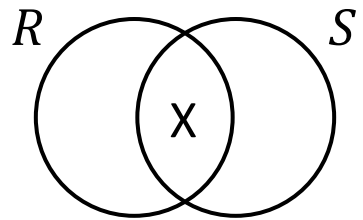
$$\forall x[R(x) \Rightarrow S(x)]$$



**No R is S**

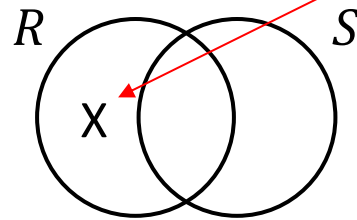
$$\forall x[R(x) \Rightarrow \neg S(x)]$$

1) "O" instead of shading: This change gives an "anchor" to the symbol "O", which becomes important later for disjunctive information ("O" stands for zero)



**Some R is S**

$$\exists x[R(x) \wedge S(x)]$$



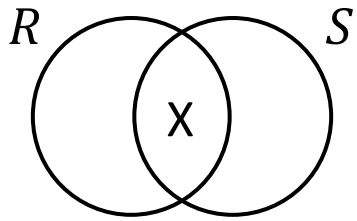
**Some R is not S**

$$\exists x[R(x) \wedge \neg S(x)]$$

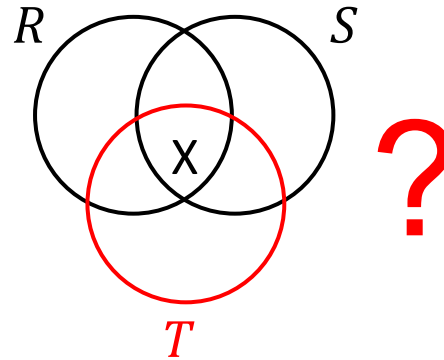
2) "X" for exists: This visual device overcomes Euler's and Venn's unclear representation of existential statements ("X" stands for there is something)

# Venn-Peirce: adding predicates

How can we express the same information from the left (not more and not less) if we just add an additional predicate T?

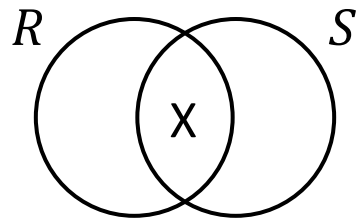


**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$



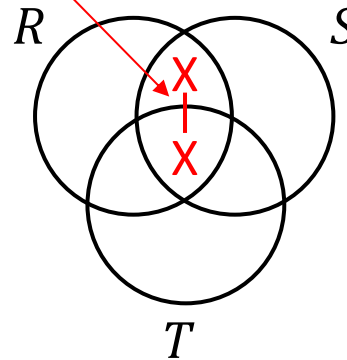
**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

# Venn-Peirce: adding predicates via disjunctions



**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

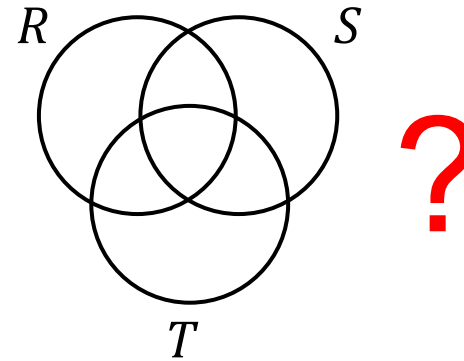
*A line connecting anchors as syntactic device to express disjunctive information. Thus connected assertions are made alternatively.*



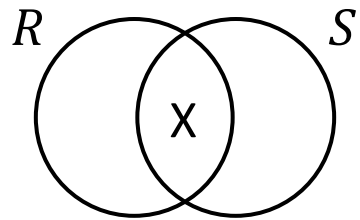
**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

$\exists x[R(x) \wedge S(x) \wedge \neg T(x)]$   
 $\vee \exists y[R(y) \wedge S(y) \wedge T(y)]$

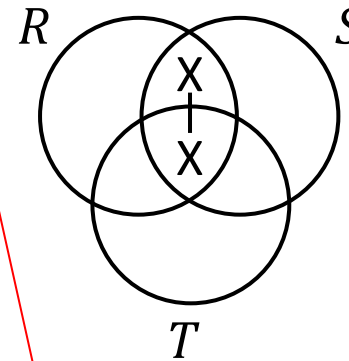
# Venn-Peirce: conjunctions



**Some R is S, and some R is T**  
 $\exists x[R(x) \wedge S(x)] \wedge \exists z[R(z) \wedge T(z)]$



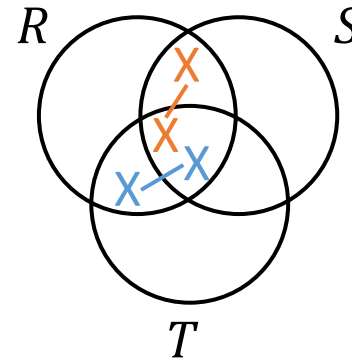
**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$



**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

# Venn-Peirce: conjunctions = juxtaposition

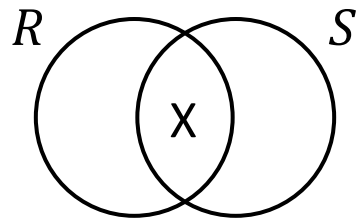
$$\begin{aligned} &\exists x[R(x) \wedge S(x) \wedge \neg T(x)] \\ \vee &\exists y[R(y) \wedge S(y) \wedge T(y)] \end{aligned}$$



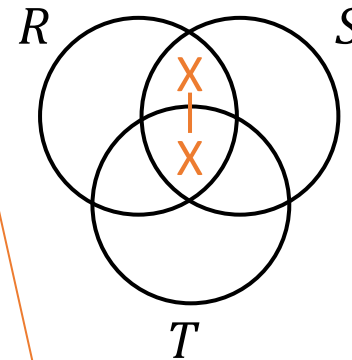
$$\begin{aligned} &\exists z[R(z) \wedge S(z) \wedge \neg T(z)] \\ \vee &\exists v[R(v) \wedge S(v) \wedge T(v)] \end{aligned}$$

**Some R is S, and some R is T**  
 $\underbrace{\exists x[R(x) \wedge S(x)]}_{\text{orange}} \wedge \exists z[R(z) \wedge T(z)]_{\text{blue}}$

*Conjunction is just juxtaposition!*

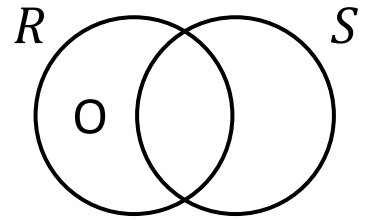


**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$



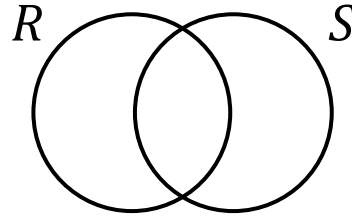
**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

# Venn-Peirce: disjunction



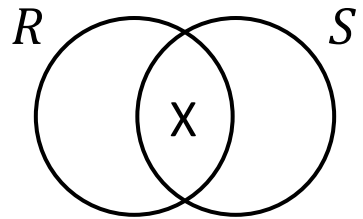
**All R are S**  
 $\forall x[R(x) \Rightarrow S(x)]$

*disjunction*



?

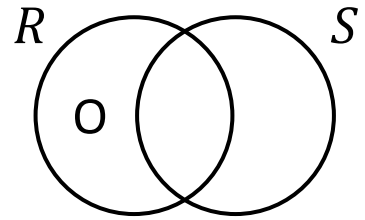
**All R are S, or some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \vee \exists x[R(x) \wedge S(x)]$



**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

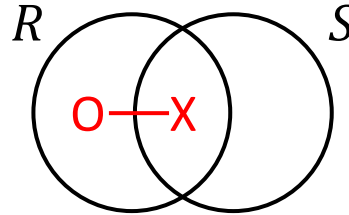


# Venn-Peirce: disjunction

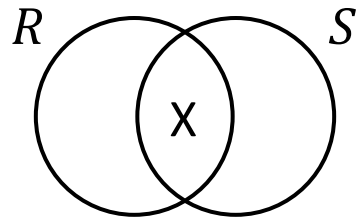


**All R are S**  
 $\forall x[R(x) \Rightarrow S(x)]$

disjunction



**All R are S, or some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \vee \exists x[R(x) \wedge S(x)]$

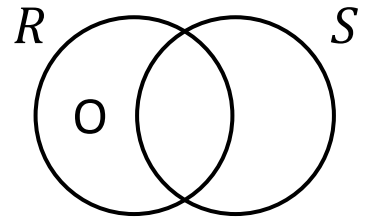


**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

What about conjunction instead of disjunction

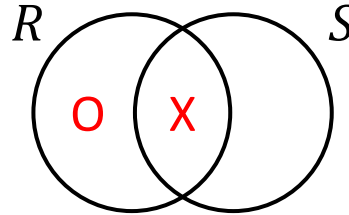
?

# Venn-Peirce: conjunction

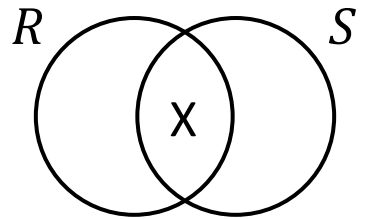


**All R are S**  
 $\forall x[R(x) \Rightarrow S(x)]$

*conjunction*

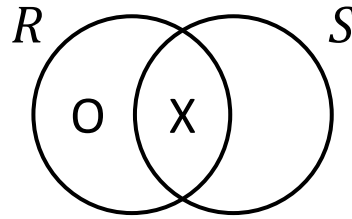


**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$

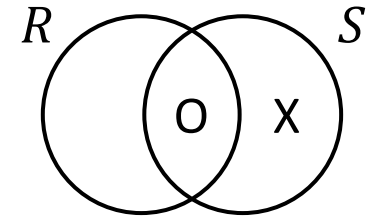


**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

# Venn-Peirce: disjunction of conjunctions



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$

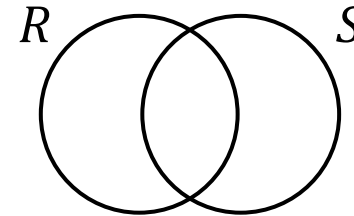


**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

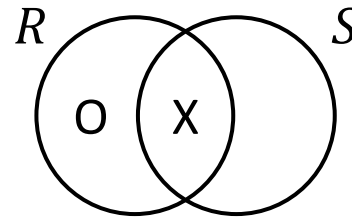
$(\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]) \vee$   
 $(\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)])$

disjunction

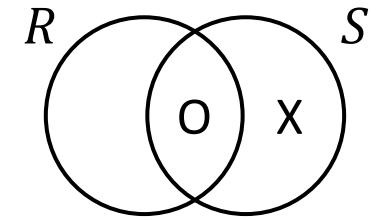
?



# Venn-Peirce: disjunction of conjunctions



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$



**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

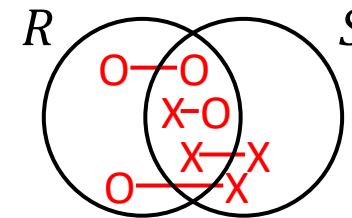
~~DNF~~

$(\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]) \vee$   
 $(\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)])$

disjunction

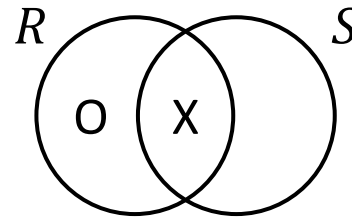
CNF

$(\forall x[R(x) \Rightarrow S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$   
 $(\forall x[R(x) \Rightarrow S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$

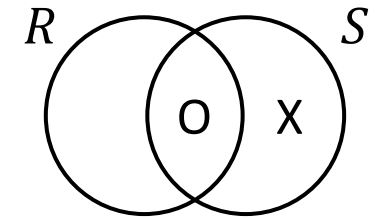


"It is only disjunctions of conjunctions that cause some inconvenience" (Peirce [~1896])

# Venn-Peirce: disjunction of conjunctions



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$



**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

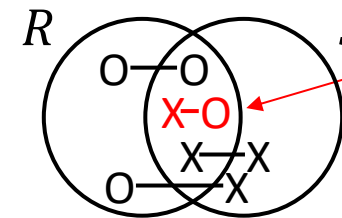
~~DNF~~

$(\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]) \vee$   
 $(\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)])$

CNF

$(\forall x[R(x) \Rightarrow S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$   
 $(\forall x[R(x) \Rightarrow S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$

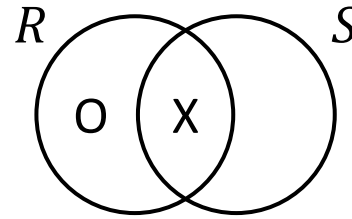
disjunction



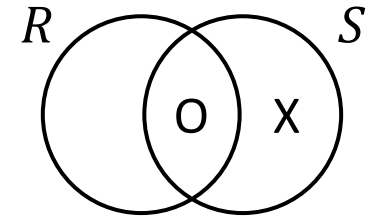
Next we can directly  
manipulate the diagram  
("diagrammatic reasoning")

"It is only disjunctions of conjunctions that cause some inconvenience" (Peirce [~1896])

# Venn-Peirce: disjunction of conjunctions



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$



**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

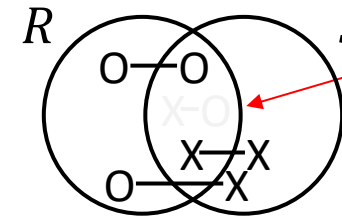
~~DNF~~

$(\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]) \vee$   
 $(\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)])$

disjunction

CNF

$(\forall x[R(x) \Rightarrow S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \forall x[R(x) \Rightarrow \neg S(x)]) \wedge$   
 $(\exists x[R(x) \wedge S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$   
 $(\forall x[R(x) \Rightarrow S(x)] \vee \exists x[S(x) \wedge \neg R(x)]) \wedge$



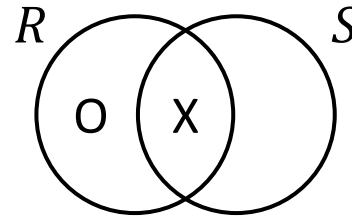
Next we can directly  
manipulate the diagram  
("diagrammatic reasoning")

"It is only disjunctions of conjunctions that cause some inconvenience" (Peirce [~1896])

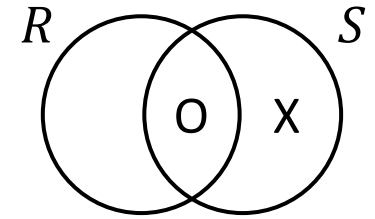
"There is, however, a very easy and very useful way of avoiding this" (Peirce [~1896])



# Venn-Peirce: disjunction of conjunctions in compartments



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$

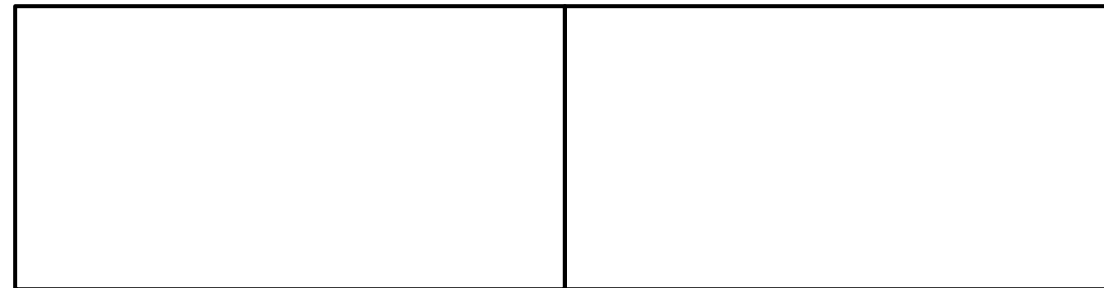


**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

DNF

- Each "compartment" represents conjunctive information.

disjunction

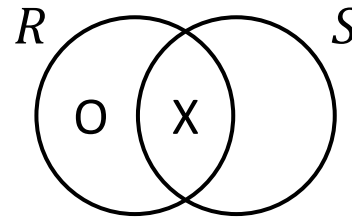


~~CNF~~

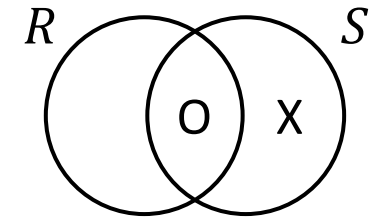
"It is only disjunctions of conjunctions that cause some inconvenience" (Peirce [~1896])

"There is, however, a very easy and very useful way of avoiding this"

# Venn-Peirce: disjunction of conjunctions in compartments



**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$



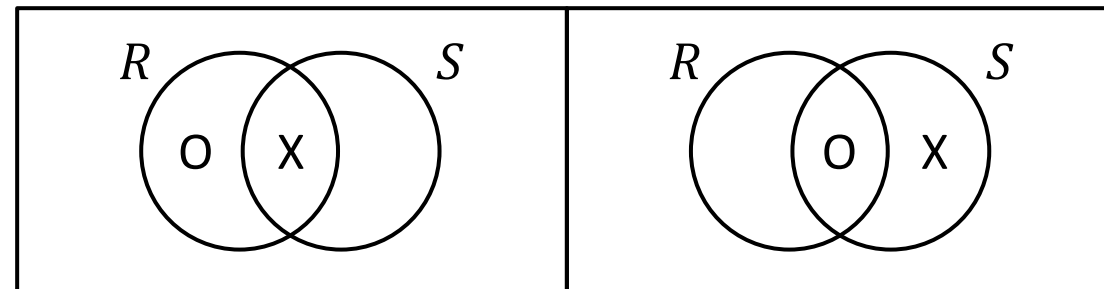
**No R is S, and some S is not R**  
 $\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)]$

DNF

- Each "compartment" represents conjunctive information.
- Different "compartments" represent different cases (disjunctions)

disjunction

~~CNF~~



"It is only disjunctions of conjunctions that cause some inconvenience" (Peirce [~1896])

"There is, however, a very easy and very useful way of avoiding this"



# Venn-Peirce [Peirce 1896]

2<sup>nd</sup> imperfection: Euler cannot affirm the existence of objects.  
Remedied with (x)

3<sup>rd</sup> imperfection: Euler cannot express that one or another of several alternative states of things occurs.

Notice a slight inconsistency with the Euler's diagram reference: two disjoint circles would represent mutual exclusive statements (e.g. R disjoint with S means "no R is S"). Here, in contrast, compartments represent non-exclusive cases (in contrast with a "possible world semantics" in which worlds are mutually exclusive)

365. In remedying the second imperfection we have gone far to remove the third and have even done something toward a treatment of the fourth. Let us consider a moment how far it can now be said that the method is inadequate to dealing with disjunctions. If by a disjunctive proposition we mean the sort of propositions usually given in the books as examples of this form, there never was any difficulty at all in dealing with them by Euler's diagrams in their original form. But such a proposition as "Every A is either B or C" which merely declares the non-existence of an A that is at once not B and not C, is not properly a disjunctive proposition. It is only disjunctions of conjunctions that cause some inconvenience; such as "Either some A is B while everything is either A or B, or else All A is B while some B is not A." Even here there is no serious difficulty. Fig. 59 expresses this proposition. It is merely that there is a greater complexity in the expression than is essential to the meaning. There is, however, a very easy and very useful way of avoiding this. It is to draw an Euler's



Fig. 59

Diagram of Euler's Diagrams each surrounded by a circle to represent its Universe of Hypothesis. There will be no need of connecting lines in the enclosing diagram, it being understood that its compartments contain the several possible cases. Thus, Fig. 60 expresses the same proposition as Fig. 59.

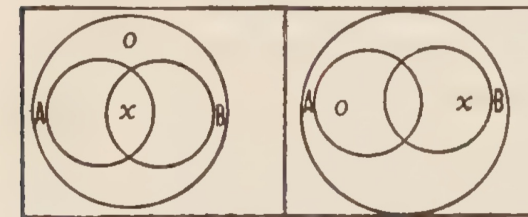


Fig. 60

# Venn-Peirce [Gardner 1958]

A word or two now about how the circles may be used for showing class propositions linked by a disjunctive (“or”) relation. Suppose we wish to say that all  $X$  is either  $Y$  or  $Z$ , taking “or” in

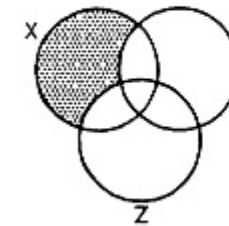


Figure 26.

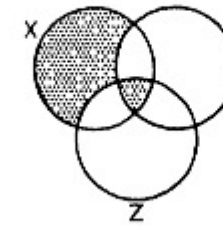


Figure 27.

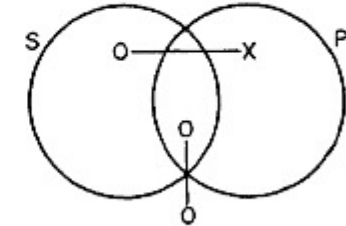
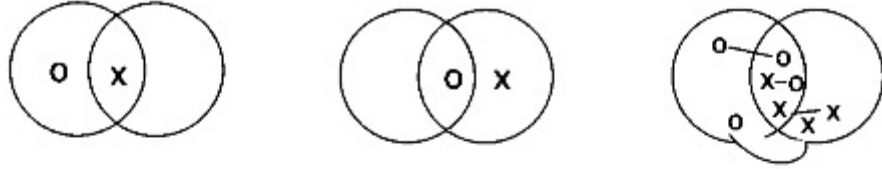


Figure 28.

the inclusive sense of “either or both.” Figure 26 shows how simply this is done. To change this to an “exclusive” disjunction (“either but not both”) we have only to shade the central area as shown in Figure 27. More complex disjunctive statements, jointly asserted, require other stratagems. Peirce suggested (*Collected Papers*, Vol. 4, pp. 307ff.) a simple way that this could be done. It involves the use of  $X$ ’s and  $O$ ’s to stand for presence or absence of members, then connecting them by a line to indicate disjunction. For example, Figure 28 shows how Peirce diagrammed the statement “Either all  $S$  is  $P$  or some  $P$  is not- $S$ , and either no  $S$  is  $P$  or no not- $S$  is not- $P$ .”

Hypothetical class statements such as “If all  $A$  is  $B$  then all  $B$  is  $C$ ,” and other types of compound statements, do not readily admit of diagramming. The best procedure seems to be, following another suggestion of Peirce’s (*op. cit.*, p. 315), to draw Venn diagrams of Venn diagrams. We shall see how this is done when we consider, later in the chapter, the use of the Venn circles for depicting truth-value statements in the propositional calculus.

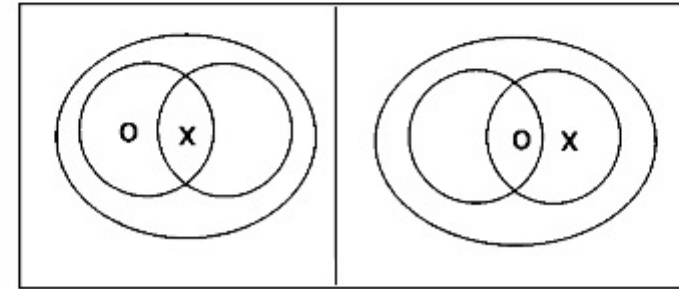
# Venn-Peirce [Shin 1995]



The rightmost diagram does not seem to have much visual power. At this point, Peirce's idea of connecting signs for disjunctive information seems to start undermining the visual effect that the original Venn method possesses. Peirce's suggestions to overcome (ii), the problem of disjunction, yield the following result: The modified system increases the power of expression, but loses the visual effects of a diagrammatic system. Peirce himself admits the complexity of his suggestion for connecting characters, and suggests an alternative way:

It is only disjunctions of conjunctions that cause some inconvenience; ... It is merely that there is a greater complexity in the expression than is essential to the meaning. There is, however, a very easy and very useful way of avoiding this. It is to draw an Euler's [Venn's] Diagram of Euler's [Venn's] Diagrams each surrounded by a circle to represent its Universe of Hypothesis. There will be no need of connecting lines in the enclosing diagrams, it being understood that its compartments contain the several possible cases.<sup>26</sup>

The basic idea behind this suggestion is very similar to the idea behind the disjunctive normal form of symbolic logic. Each compartment of a diagram conveys only conjunctive information and the relations among the compartments are disjunctive. According to this modification, the previous rightmost, complicated-looking diagram may be changed into the following diagram:



My presentation of Venn diagrams keeps to Venn's original system, and accepts only those extensions of Peirce's that may consistently be applied to the Venn system. That is, I will use a shading (not "o"), and three new syntactic devices, "x," a connecting line between x's (for Venn-I in Chapter 3), and a connecting line between diagrams (for Venn-II in Chapter 4).



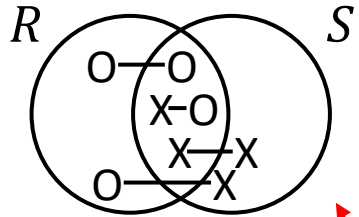
# Venn-Peirce-Shin [Venn-II] (1995)

Sources used:

- Shin. The logical status of diagrams. 1995. <https://doi.org/10.1017/CBO9780511574696>

# Venn-Peirce-Shin (Venn-II)

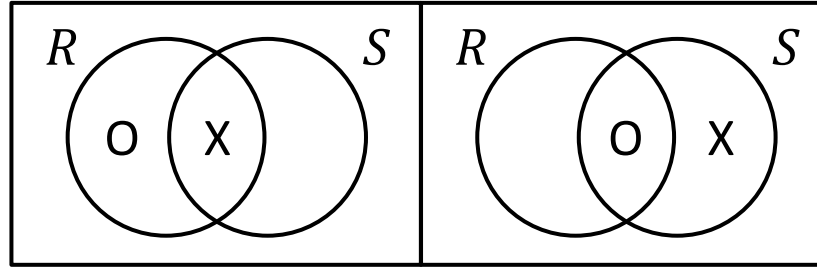
Venn-Peirce (disjunctions  
w/ lines between anchors)



(**All** R are S, and **some** R is S) or (**No** R is S, and **some** S is not R)

Notice: disjunctions  
between all anchors,  
thus both X's and O's

Venn-Peirce (disjunctions  
via compartments)



Notice: X and O anchors are  
not used for disjunctions

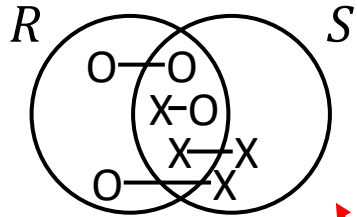
Venn-Peirce-Shin ("Venn-II")

?

Shin finds that disjunctions between universal statements (in addition to existential statements)  
"increases the power of expression, but loses the visual effect(iveness) of a diagrammatic system."  
[Shin'95]

# Venn-Peirce-Shin (Venn-II)

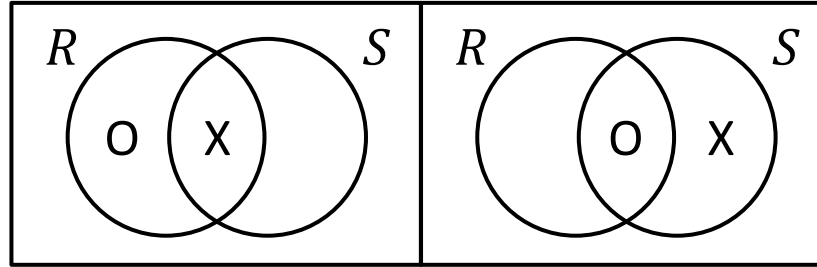
Venn-Peirce (disjunctions w/ lines between anchors)



(All R are S, and some R is S) or (No R is S, and some S is not R)

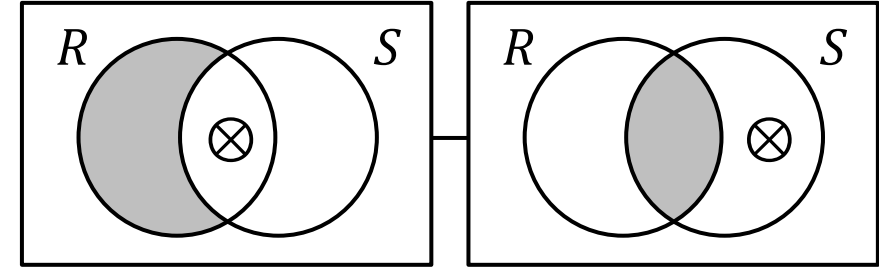
Notice: disjunctions between all anchors, thus both X's and O's

Venn-Peirce (disjunctions via compartments)



Notice: X and O anchors are not used for disjunctions

Venn-Peirce-Shin ("Venn-II")



- replaces "O" with shading
- replaces "X" with "⊗"
- allows "X-sequences" (disjunctions between existential statements "X")
- disjunctions between universal statements (now via shading, formerly via "O") are now handled via lines b/w compartments

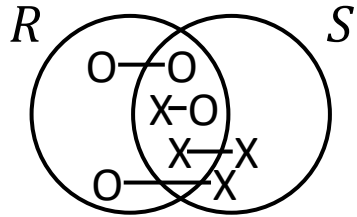
Shin finds that disjunctions between universal statements (in addition to existential statements)

"increases the power of expression, but loses the visual effect(iveness) of a diagrammatic system."  
[Shin'95]

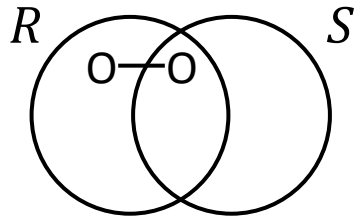
Shin proved this diagrammatic system to be equivalent in expressiveness as monadic FOL without equality. "Without equality" means it cannot express: "There is exactly one R".

# Venn-Peirce-Shin (Venn-II)

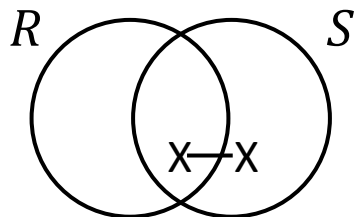
Venn-Peirce (disjunctions  
w/ lines between anchors)



(**All** R are S, and **some** R is S) or (**No** R is S, and **some** S is not R)

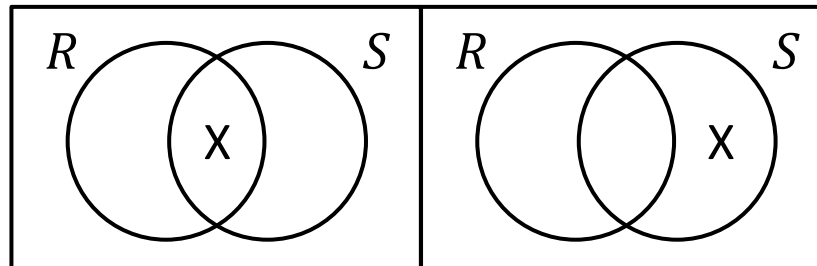
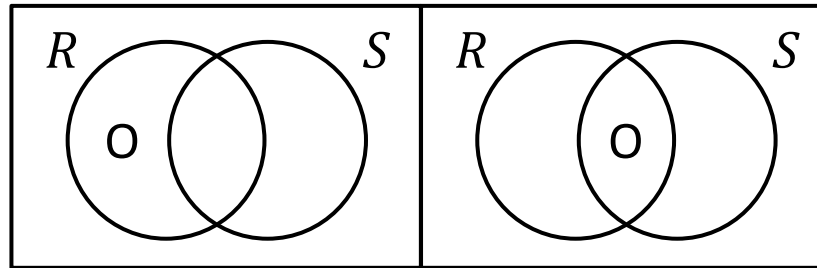
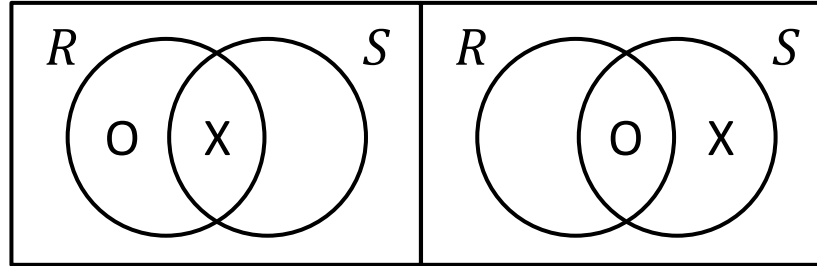


(**All** R are S) or (**no** R is S)

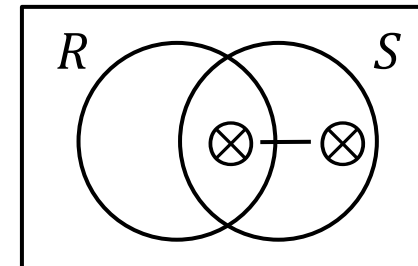
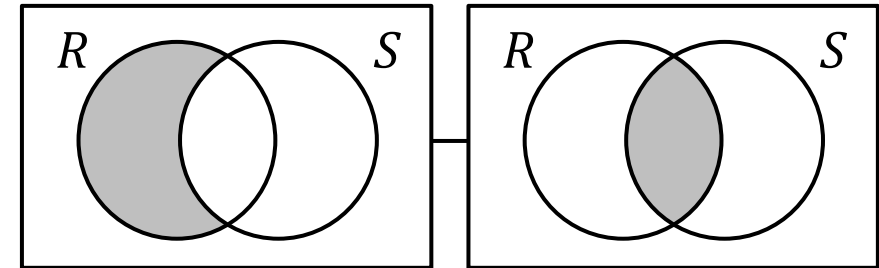
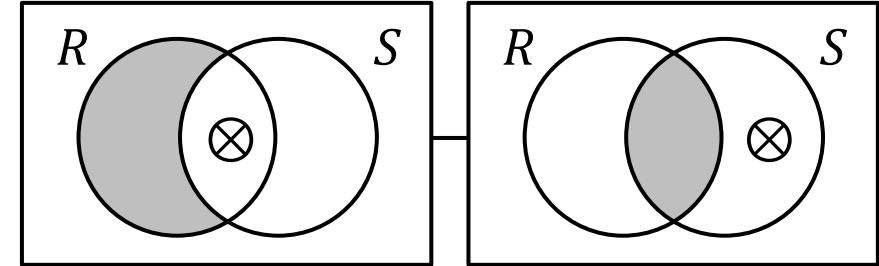


(**Some** R is S) or (**some** S is not R)

Venn-Peirce (disjunctions  
via compartments)



Venn-Peirce-Shin ("Venn-II")



Goal: both full logical  
expressiveness and  
visual effectiveness

# Venn-Peirce-Shin [Salmon 1984]

*E* sentences (including all the English variants of the standard form of *E* sentence) can be represented by the Venn diagram shown in Figure 9-6.

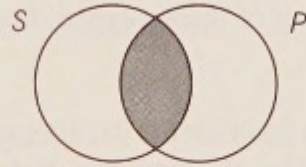


Figure 9-6

As in the Venn diagram of the *A* sentence, the two circles represent the classes *S* and *P*. The shading in the overlapping area indicates that this region is empty (that there are no things belonging to both classes).

In constructing the Venn diagram for the *I* sentence, two overlapping circles are again used to represent the classes *S* and *P*. An **x** is used to represent the fact that a class has a member. Since the *I* sentence says that the classes *S* and *P* share at least one member, an **x** is placed in the overlapping region, as shown in Figure 9-7.

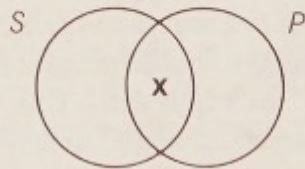


Figure 9-7

In Figure 9-14, the information contained in the second premiss, “Some *M* are *P*” is added to the diagram of the first premiss. The overlapping region between the *P* circle and the *M* circle is itself divided into two parts. One of these parts lies within the *S* circle; the other part lies outside the *S* circle. Since the information in the premiss tells us only that there is a member somewhere in this overlap, we cannot locate an **x** definitely in one region or the other. Instead, we use the “floating **x**” (two **x**s connected by a dashed line) to indicate that a member lies somewhere in that region.

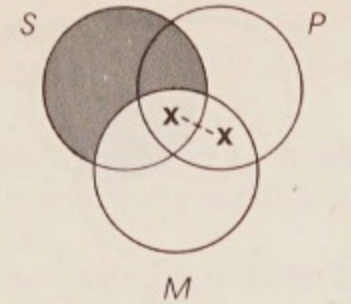


Figure 9-14

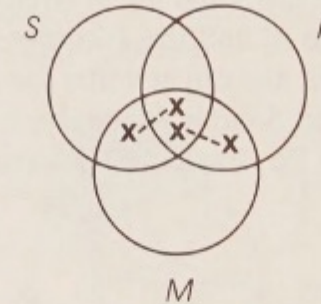


Figure 9-17

To diagram the first premiss, we place an **x** in the overlap between *S* and *M*. There are two parts to this overlap—one within the *P* circle and one outside the *P* circle (see Figure 9-17). The premiss does not tell us where to place the **x**, so we must use a floating **x**. The second premiss tells us that there is a member of both *P* and *M* but does not tell us whether or not this member belongs to *S*. Therefore, we must use another floating **x**. The conclusion requires that an **x** be in the overlapping region between *S* and *P*. But since both **x**s are floating, we cannot tell whether or not either **x** lies in that region. Thus, the conclusion cannot be “read off” the diagram, and the syllogism is invalid.



# Part 4: Early Diagrammatic Representations

Monadic predicate calculus (Boolean queries & unary predicates)

1. Euler Circles (1768)
2. Venn Diagrams (1880)
3. Venn-Peirce Diagrams (~1896)
4. Venn-Peirce-Shin Diagrams (1995)

Polyadic predicate calculus (allowing predicates with arities  $\geq 2$ )

7. Peirce Beta Existential Graphs (~1909)
8. Conceptual graphs (1976)
9. String diagrams (2024)

# Beta Existential Graphs (Beta EGs) by Peirce (~1909)

## Sources used:

- Peirce. Collected Papers of Charles Sanders Peirce. Volumes 3 and 4. 1933. Paragraph 4.621. [https://archive.org/details/collectedpaperso0000unse\\_r5j9/](https://archive.org/details/collectedpaperso0000unse_r5j9/)
- Zeman. The Graphical Logic of Charles S. Peirce, Ph.D. dissertation, University of Chicago. 1964. [https://isidore.co/CalibreLibrary/Zeman,%20Joseph%20Jay/The%20Graphical%20Logic%20of%20C.%20S.%20Peirce%20\(4481\)/](https://isidore.co/CalibreLibrary/Zeman,%20Joseph%20Jay/The%20Graphical%20Logic%20of%20C.%20S.%20Peirce%20(4481)/)
- Roberts. The existential graphs of Charles S. Peirce. De Gruyter Mouton. 1973. <https://doi.org/10.1515/9783110226225>
- Roberts. The existential graphs. Computers & Mathematics with Applications. 1992. [https://doi.org/10.1016/0898-1221\(92\)90127-4](https://doi.org/10.1016/0898-1221(92)90127-4)
- Sun-Joo Shin. The Iconic Logic of Peirce's Graphs. The MIT Press. 2002. <https://doi.org/10.7551/mitpress/3633.001.0001>

# Beta Existential Graphs (EGs)

*S: "There is a boat."*

1. Supports sentence (no free variables), no queries

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$

?

2. Quantified variables from DRC are represented by "lines of identities" on the "sheet of assertion"

Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

# Beta Existential Graphs (EGs)

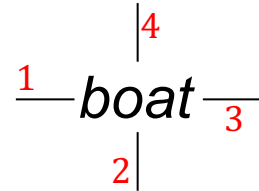
Schema

Boat	
1	<u>bid</u>
2	bname
3	color
4	pdate

*S: "There is a boat."*

1. Supports sentence (no free variables), no queries

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$



2. Quantified variables from DRC are represented by "lines of identities" on the "sheet of assertion"

3. Requires an order on the attributes of each predicate (we use counter-clockwise)

*S: "There is a red boat."*

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)] = \exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \text{Red}(z)]$



4. EGs do not support constants, we thus use unary predicates. As alternative, we could have used:

$\exists x,y,u [\text{Boat}(x,y,u) \wedge \text{Red}(x)]$

# Beta Existential Graphs (EGs)

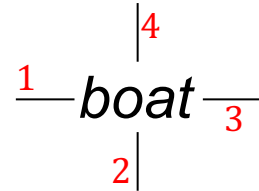
## Schema

Boat	
1	<u>bid</u>
2	bname
3	color
4	pdate

*S: "There is a boat."*

1. Supports sentence (no free variables), no queries

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$



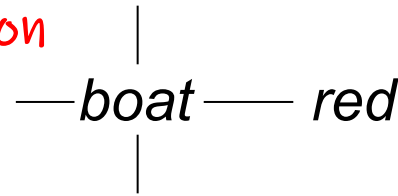
2. Quantified variables from DRC are represented by "lines of identities" on the "sheet of assertion"

3. Requires an order on the attributes of each predicate (we use counter-clockwise)

*S: "There is a red boat."*

5. juxtaposition = conjunction

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)] = \exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \text{Red}(z)]$



4. EGs do not support constants, we thus use unary predicates. As alternative, we could have used:

$\exists x,y,u [\text{Boat}(x,y,u) \wedge \text{Red}(x)]$

*S: "There is a boat that is not red."*

$\exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \neg(\exists w [\text{Red}(w) \wedge z=w])]$



6. A statement is denied by enclosing it in closed curve, called a "cut"

# Beta Existential Graphs (EGs)

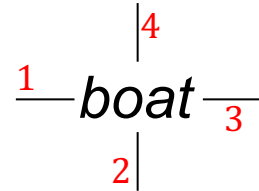
Schema

Boat	
1	<u>bid</u>
2	bname
3	color
4	pdate

*S: "There is a boat."*

1. Supports sentence (no free variables), no queries

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$



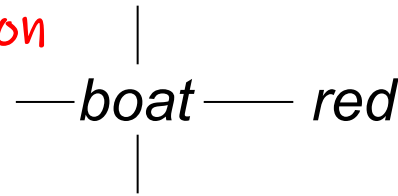
2. Quantified variables from DRC are represented by "lines of identities" on the "sheet of assertion"

3. Requires an order on the attributes of each predicate (we use counter-clockwise)

*S: "There is a red boat."*

5. juxtaposition = conjunction

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)] = \exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \text{Red}(z)]$

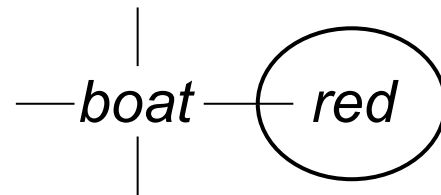


4. EGs do not support constants, we thus use unary predicates. As alternative, we could have used:

$\exists x,y,u [\text{Boat}(x,y,u) \wedge \text{Red}(x)]$

*S: "There is a boat that is not red."*

$\exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \neg(\exists w [\text{Red}(w) \wedge z=w])]$



6. A statement is denied by enclosing it in closed curve, called a "cut"

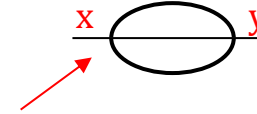
# Beta Existential Graphs (EGs)

*S: "There is exactly one boat."*

$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \neg(\exists s,t,u,v [\text{Boat}(s,t,u,v) \wedge x \neq s])]$

$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \forall s,t,u,v [\text{Boat}(s,t,u,v) \rightarrow x=s]]$

?



7. EGs can express equality.  
"There exist two things (x and y) and they are different" (the line between them is negated)

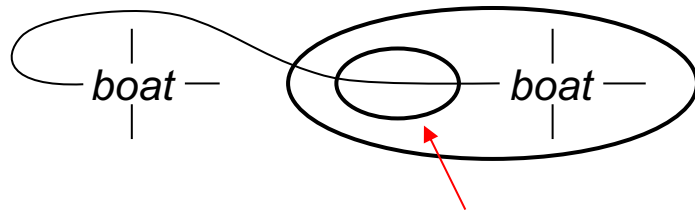
Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

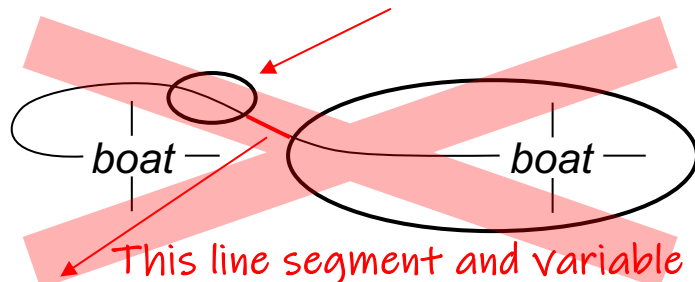
# Beta Existential Graphs (EGs)

*S: "There is exactly one boat."*

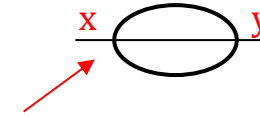
$$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \neg(\exists s,t,u,v [\text{Boat}(s,t,u,v) \wedge x \neq s])]$$

$$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \forall s,t,u,v [\text{Boat}(s,t,u,v) \rightarrow x=s]]$$


8. The placement of the cuts matters! The EG below could erroneously be seen as equivalent way to write above statement (I got this wrong myself earlier). But a more careful analysis shows that it has a different semantic interpretation.



This line segment and variable  $s$  are not guarded

$$\exists x,y,z,w,s [\text{Boat}(x,y,z,w) \wedge x \neq s \wedge \neg(\exists t,u,v [\text{Boat}(s,t,u,v)])]$$


7. EGs can express equality.  
"There exist two things ( $x$  and  $y$ ) and they are different" (the line between them is negated)

Schema

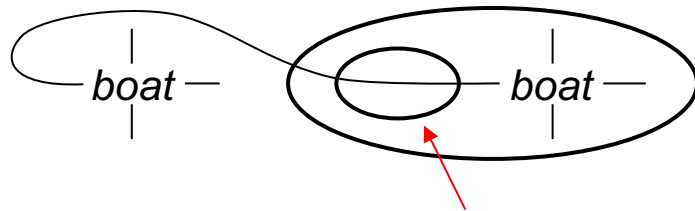
	Boat
1	bid
2	bname
3	color
4	pdate



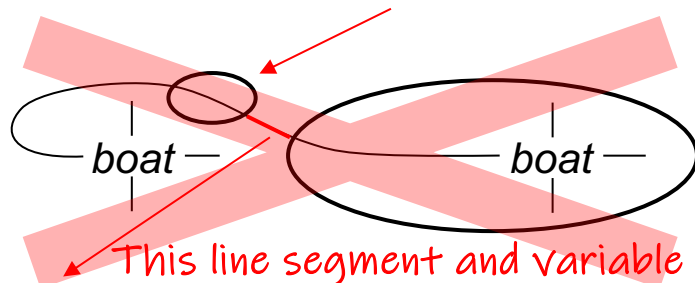
# Beta Existential Graphs (EGs)

*S: "There is exactly one boat."*

$$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \neg(\exists s,t,u,v [\text{Boat}(s,t,u,v) \wedge x \neq s])]$$

$$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \forall s,t,u,v [\text{Boat}(s,t,u,v) \rightarrow x=s]]$$


8. The placement of the cuts matters! The EG below could erroneously be seen as equivalent way to write above statement (I got this wrong myself earlier). But a more careful analysis shows that it has a different semantic interpretation.



This line segment and variable  $s$  are not guarded

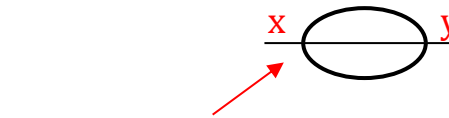
$$\exists x,y,z,w,s [\text{Boat}(x,y,z,w) \wedge x \neq s \wedge \neg(\exists t,u,v [\text{Boat}(s,t,u,v)])]$$

Beta EG example adapted from "Sowa. Peirce's tutorial on existential graphs, Semiotica, 2011. <https://doi.org/10.1515/semi.2011.060> "

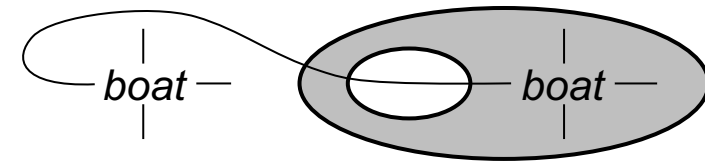
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

Schema

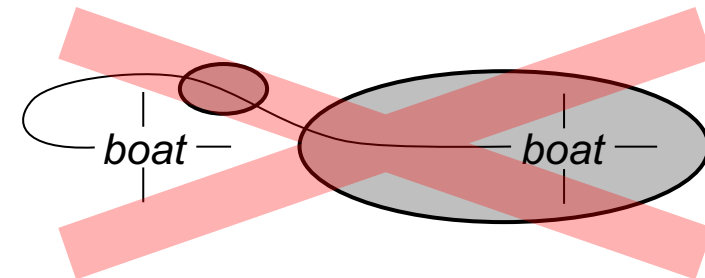
	Boat
1	bid
2	bname
3	color
4	pdate



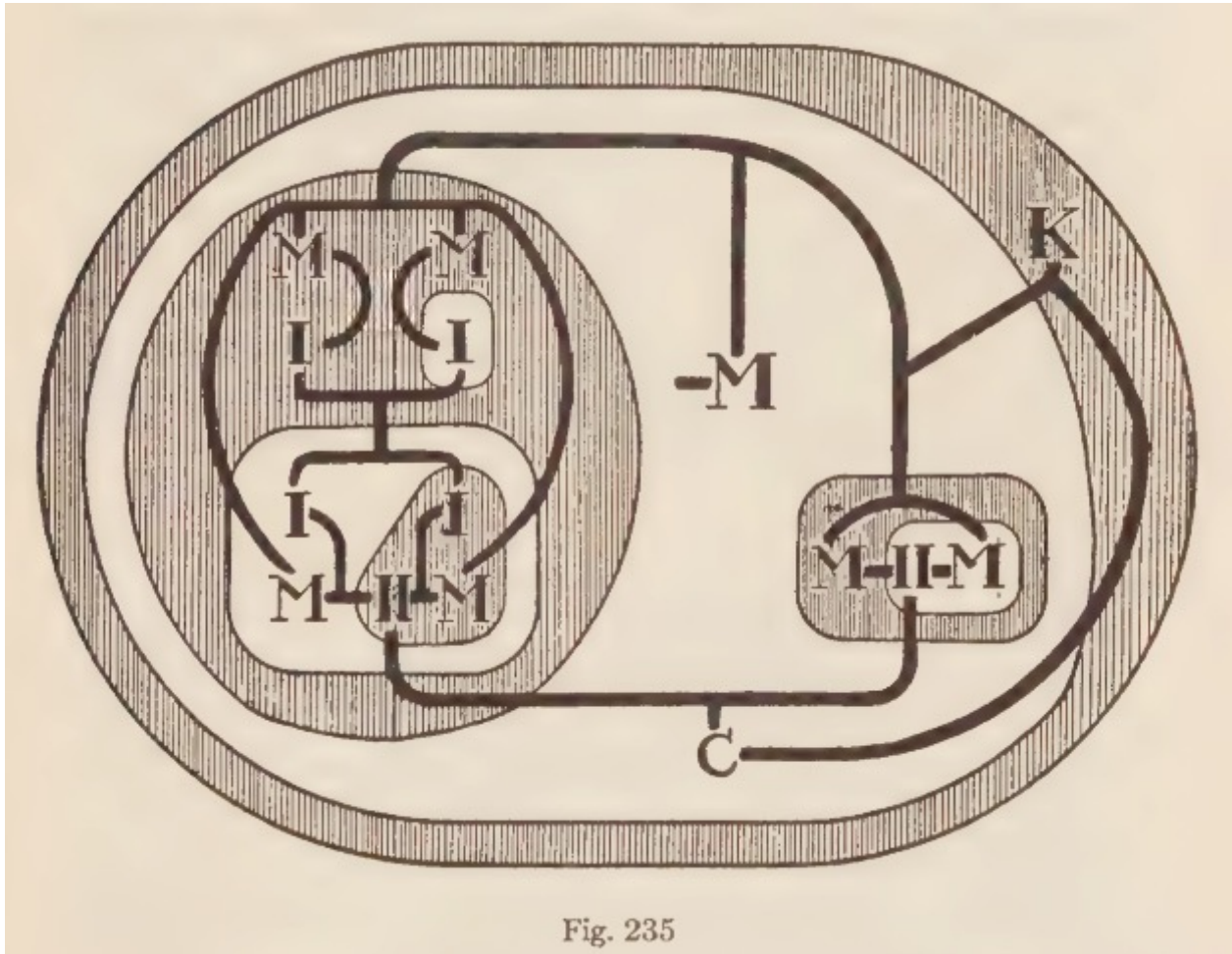
7. EGs can express equality.  
"There exist two things ( $x$  and  $y$ ) and they are different" (the line between them is negated)



9. "Peirce shading": shade the oddly enclosed areas. Makes it often easier to read these diagrams.



# "Peirce shading": Alternating shaded areas



on each side a higher peg to precede a lower one. With this understanding, the graph of Fig. 235, where for the sake of perspicuity the oddly enclosed, or negating areas are shaded, may be translated into the language of speech in either of the two following equivalent forms (besides many others):

It is false that

there is a cyclic system while it is false that  
this system has a member  
and involves a relation ("being A to," the bottom peg of II),  
and that it is false that  
the system has a member of which it is false that  
it is in that relation, A, to a member of the system,  
while it is false that  
there is a definite predicate, P (the top or bottom peg of  
I), that is true of a member of  
the system and is false of a member of the system,  
and that it is false that  
this predicate is true of a member of the system of which  
it is false that  
it is A to a member of the system of which P is true.

Reading from the outside inward also called "endoporeutic" reading by Peirce

# Beta Existential Graphs (EGs)

*S: "There are exactly two boats."*

$$\exists x,y,z,s,t,p,r [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,p,r) \wedge x \neq s \wedge \neg(\exists u,v,w, [\text{Boat}(u,v,\text{'red'},w) \wedge u \neq x \wedge u \neq s])]$$
$$\exists x,y,z,s,t,p,r [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,p,r) \wedge x \neq s \wedge \forall u,v,w, [\text{Boat}(u,v,\text{'red'},w) \rightarrow (u=x \vee u=s)]]$$

Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate



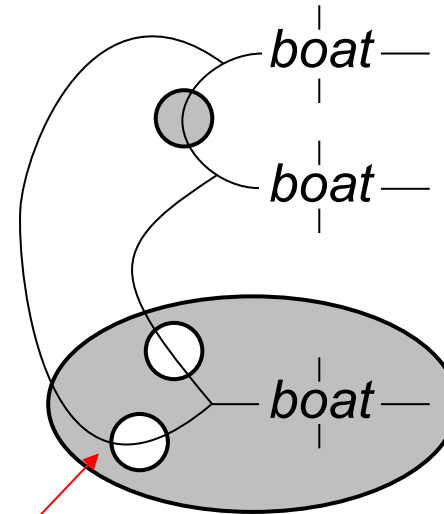
# Beta Existential Graphs (EGs)

*S: "There are exactly two boats."*

$$\exists x,y,z,s,t,p,r [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,p,r) \wedge x \neq s \wedge \neg(\exists u,v,w, [\text{Boat}(u,v,\text{'red'},w) \wedge u \neq x \wedge u \neq s])]$$
$$\exists x,y,z,s,t,p,r [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,p,r) \wedge x \neq s \wedge \forall u,v,w, [\text{Boat}(u,v,\text{'red'},w) \rightarrow (u=x \vee u=s)]]$$

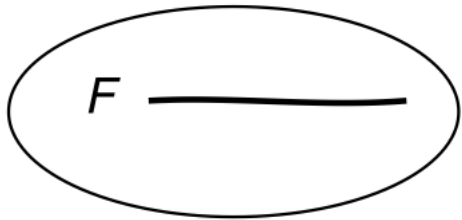
Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

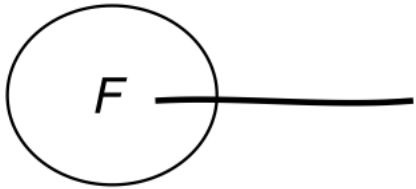


The placement of the two cuts *\*inside\** the larger one is important; placing them outside instead would give an incorrect semantics.

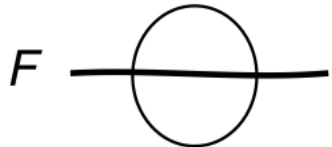
# Beta EGs: Lines of Identity & "Loose ends"



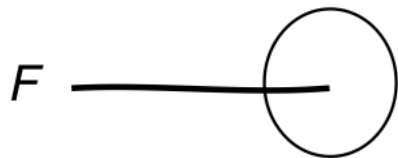
"It is not the case that something is F"



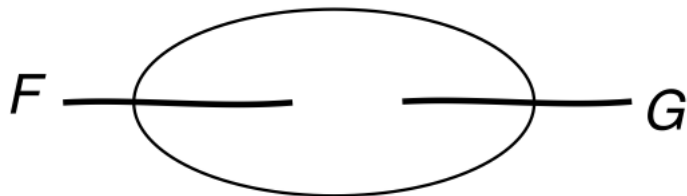
"Something is not F"



"Something is F, and there is at least one more thing"

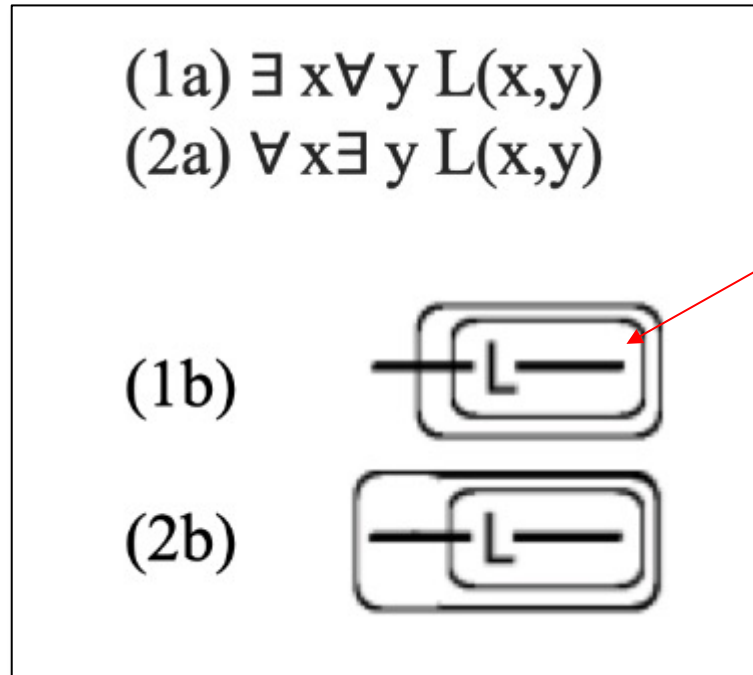


"Some F is not identical with itself."



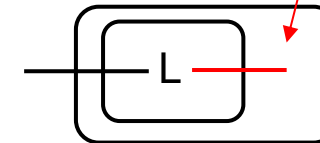
"Some F or some G is not identical with itself."

# Beta EGs: Lines of Identity & "Loose ends"



The end point of these lines matters a lot. One appears in the wrong enclosure.

It should rather end in nesting depth 1, instead of 2



# The "lines of identity" are complicated to interpret



Figure 65.

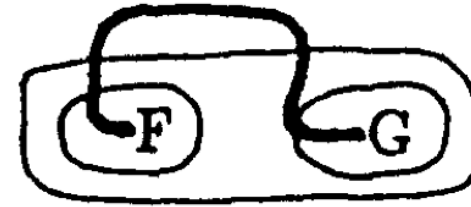


Figure 66.

Here is a more complex proof. The graphs of Figures 65 and 66 can each be derived from the other. This equivalence is the theorem  $[(\exists x) Fx \vee (\exists x) Gx] \equiv (\exists x) [Fx \vee Gx]$ .

There is extensive secondary literature that elaborates on how routing the lines affects the semantics. These interpretations rely on visual inference rules (= diagrammatic reasoning) and are pretty hairy.



# The "lines of identity" are complicated to interpret



Figure 65.

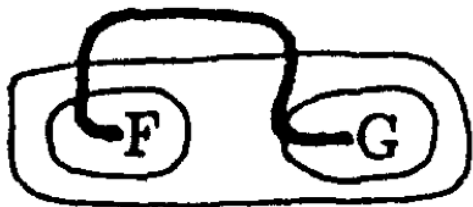
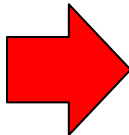
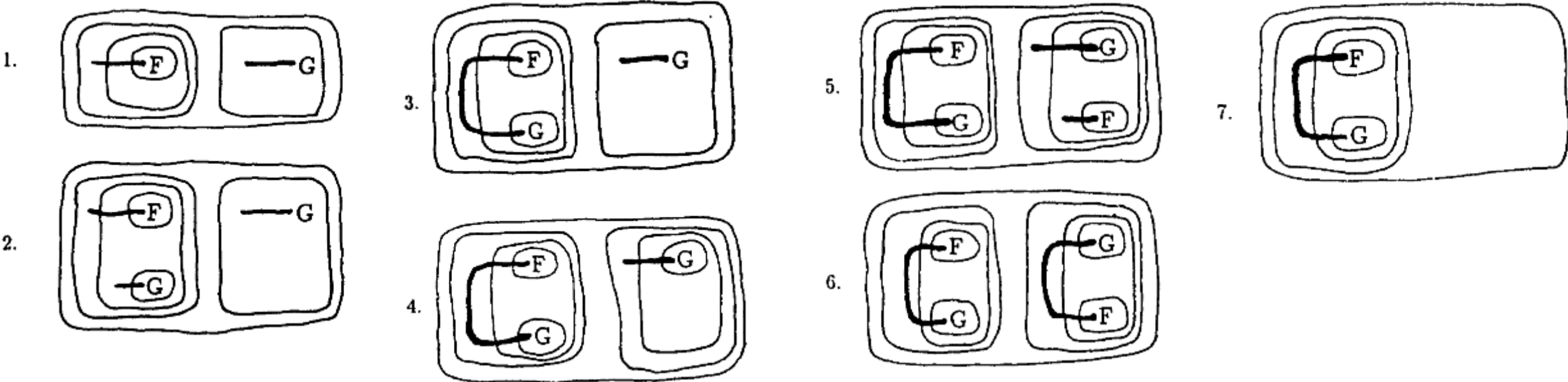


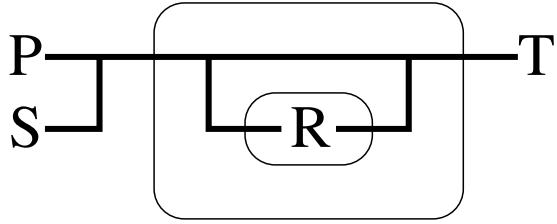
Figure 66.

The inference from Figure 66 to Figure 65 is straightforward, but the converse inference requires subtlety.





# How to interpret more complicated graphs?



?

# How to interpret more complicated graphs?

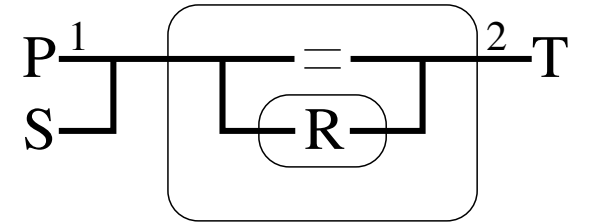
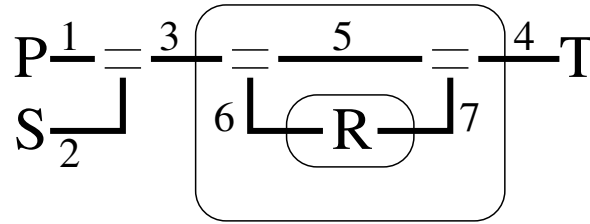
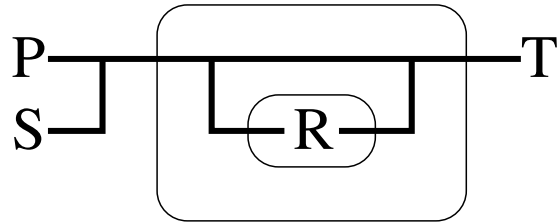


Figure from Dau [2006] discussing an example beta-EG whose interpretation provided by Shin [2002] is incorrect, together with two alternative interpretations of splitting the Lines of Identity (LI's) in order to interpret this beta-EGs correctly. The details of the arguments are not important here, only that there is a lot of disagreement as to how interpret LI's correctly. Take-away: Beta EGs are complicated to read and interpret correctly, mainly because of the use of lines for existential quantification.

# Beta Existential Graphs

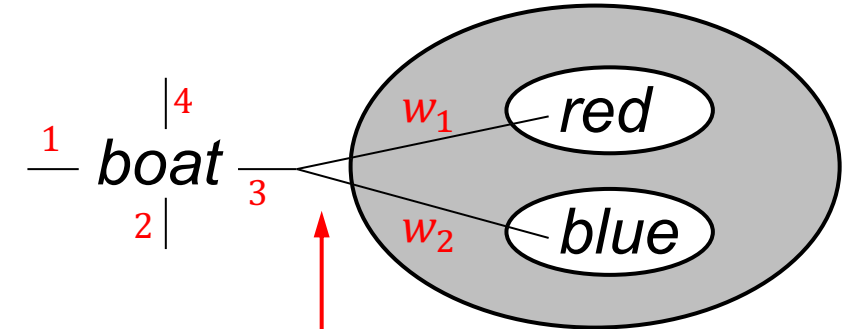
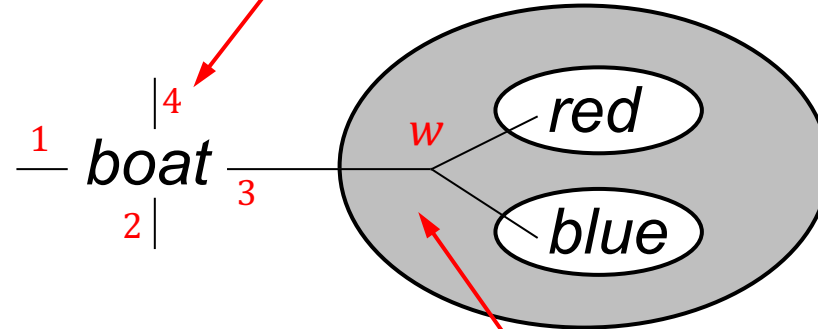
Schema

	Boat
1	bid
2	bname
3	color
4	pdate

~Q1: "There is a boat that is red or blue."

```
select exists
(select *
from Boat
where color = 'red'
or color = 'blue')
```

The literature is not explicit about how to determine the order of the attributes. My convention here is a counter-clockwise order.



Comparison predicates such as "pdate < 1980" are not supported

Disjunction of selection predicates can be represented via De Morgan (double-negation and conjunction)

The exact placement of this fork (inside the shaded area) makes a slight difference in the interpretation of the line segments. Yet both turn out to be logically equivalent.

left:  $\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w [w=y \wedge \neg(w='red') \wedge \neg(w='blue')])]\}$

right:  $\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w_1,w_2 [w_1=y \wedge w_2=y \wedge \neg(w_1='red') \wedge \neg(w_2='blue')])]\}$

## DRC (Domain Relational Calculus)

$$\begin{aligned} &\exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge (z='red' \vee z='blue')] \\ &\exists x,y,z,u [\text{Boat}(x,y,z,u) \wedge \neg(\neg(z='red') \wedge \neg(z='blue'))] \end{aligned}$$

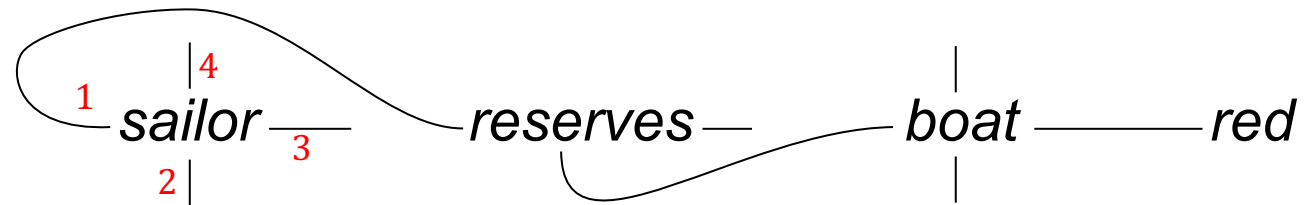
# Beta Existential Graphs

*~Q2: "There is a sailor who reserved a red boat."*

```
select exists
(select S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red')
```

Schema

Sailor	Reserves	Boat
1 <u>sid</u>	<u>sid</u>	<u>bid</u>
2 sname	<u>bid</u>	bname
3 rating	<u>day</u>	color
4 bdate		pdate

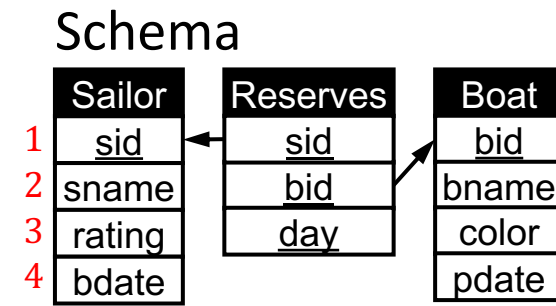


## DRC (Domain Relational Calculus)

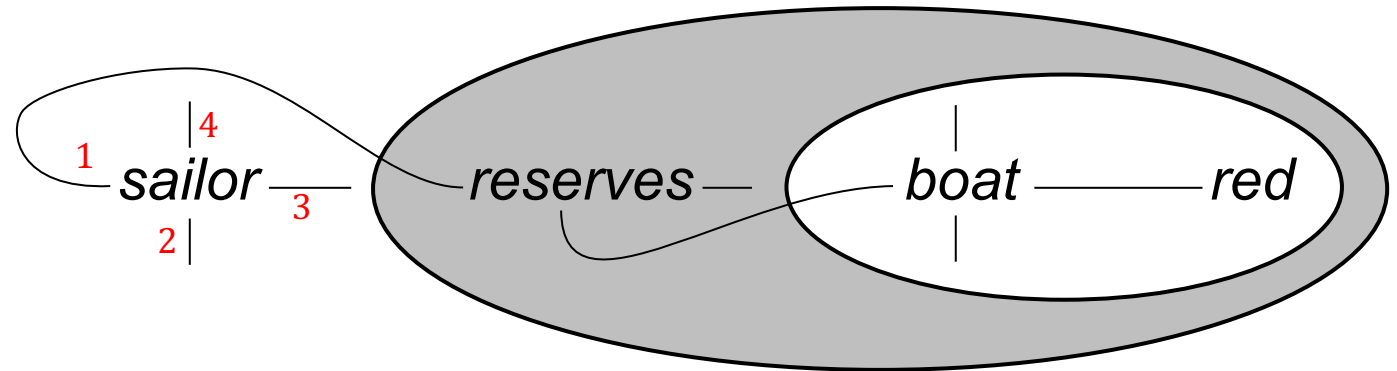
$\exists x,v,z,w,y,t,u,s [Sailor(v,x,z,w) \wedge \exists y,t [Reserves(v,y,t) \wedge \exists u,s [Boat(y,u,'red',s)]]]$

# Beta Existential Graphs

~Q3: "There is a sailor who reserved only red boats."



```
select exists
(select S.sname
from Sailor S
where not exists
(select *
from Reserves R
where S.sid=R.sid
and not exists
(select *
from Boat B
where R.bid=B.bid
and color = 'red')))
```



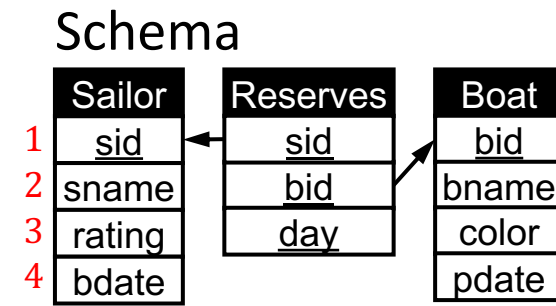
## DRC (Domain Relational Calculus)

$$\exists x,v,z,w [\text{Sailor}(v,x,z,w) \wedge \neg(\exists y,t [\text{Reserves}(v,y,t) \wedge \neg(\exists u,s [\text{Boat}(y,u,\text{'red'},s)])])]$$

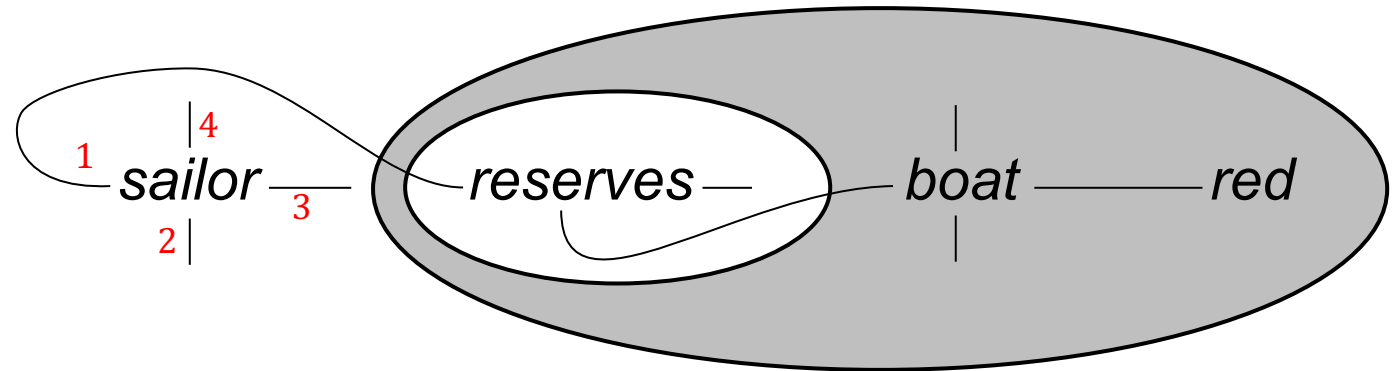
$$\exists x,v,z,w [\text{Sailor}(v,x,z,w) \wedge \forall y,t [\text{Reserves}(v,y,t) \rightarrow (\exists u,s [\text{Boat}(y,u,\text{'red'},s)])]]$$

# Beta Existential Graphs

~Q4: "There is a sailor who reserved all red boats."



```
select exists
( select S.sname
  from Sailor S
  where not exists
    (select *
     from Boat B
     where color = 'red'
     and not exists
       (select *
        from Reserves R
        where S.sid=R.sid
        and B.bid=R.bid))
```



## DRC (Domain Relational Calculus)

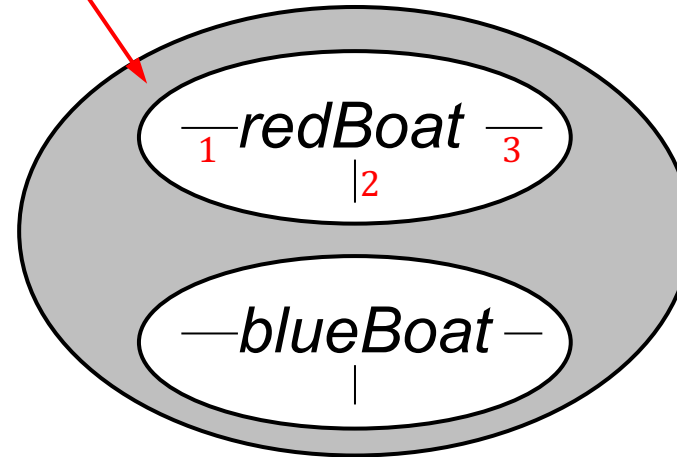
$$\exists x,v,z,w [Sailor(v,x,z,w) \wedge \neg(\exists y,u,s [Boat(y,u,'red',s) \wedge \neg(\exists t [Reserves(v,y,t)])])]$$
$$\exists x,v,z,w [Sailor(v,x,z,w) \wedge \forall y,u,s [Boat(y,u,'red',s) \rightarrow (\exists t [Reserves(v,y,t)])]]$$

# Beta Existential Graphs

$\sim Q5$ : "There is a boat that is red or blue."

```
select exists
(select *
 from RedBoat R
 union
 select *
 from BlueBoat B)
```

Union of table can be represented via De Morgan (double-negation and conjunction). However, notice that the resulting expression is not safe (free variables  $x, y, z$  are not "guarded", i.e. not bound to an element from the active domain)



Schema

RedBoat	
1	<u>bid</u>
2	bname
3	pdate

BlueBoat	
	<u>bid</u>
	bname
	pdate

## DRC (Domain Relational Calculus)

$$\exists x \exists y \exists z [\text{RedBoat}(x, y, z) \vee \text{BlueBoat}(x, y, z)]$$
$$\neg(\neg(\exists x \exists y \exists z [\text{RedBoat}(x, y, z)]) \wedge \neg(\exists z [\text{BlueBoat}(x, y, z)]))$$

An accessible overview of issues involving safety is: Topor, Safety and Domain Independence, Encyclopedia of Database Systems. 2009 [https://doi.org/10.1007/978-0-387-39940-9\\_1255](https://doi.org/10.1007/978-0-387-39940-9_1255)

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Conceptual graphs (1976)

## Sources used:

- Sowa. "Conceptual graphs for a data base interface," IBM Journal of Research and Development, 1976. <https://doi.org/10.1147/rd.204.0336>
- Sowa. "Conceptual Structures: Information Processing in Mind and Machine," Addison-Wesley, 1984. <https://dl.acm.org/doi/book/10.5555/4569>
- Sowa. "Knowledge Representation: Logical, Philosophical, and Computational Foundations," Brooks/Cole, 2000. <https://dl.acm.org/doi/book/10.5555/318183>
- Sowa. "Conceptual graphs," in Handbook of Knowledge Representation," 2008. [https://doi.org/10.1016/S1574-6526\(07\)03005-2](https://doi.org/10.1016/S1574-6526(07)03005-2)
- Sowa. "From existential graphs to conceptual graphs," IJCSA, 2013. <https://doi.org/10.4018/ijcssa.2013010103>
- Sowa. "Reasoning with diagrams and images," Journal of Applied Logics. 2018. <https://www.collegepublications.co.uk/ifcolog/?00025>
- Dau. "The Logic System of Concept Graphs with Negation And Its Relationship to Predicate Logic," 2003. <https://doi.org/10.1007/b94030>
- Chein, Mugnier. "Graph-based knowledge representation," 2009. <https://doi.org/10.1007/978-1-84800-286-9>

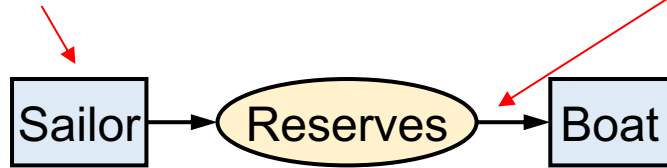


# Conceptual Graphs and their translation to calculus

Conceptual graphs have 2 types of nodes (similar to ER diagrams):

- **concept** nodes (rectangular): **represent quantification** (instead of line), entities (and attributes)
- **relation** nodes (oval): show relationships (of arbitrary arity) between entities

entities of type "Sailor"



arcs link concepts and relations (arcs "belong" to concepts, arrowhead marks first argument for binary relation, sequence numbers are added for higher arity relations)



Can think of binary relations in a relational database with typed columns

Translation to predicate calculus:

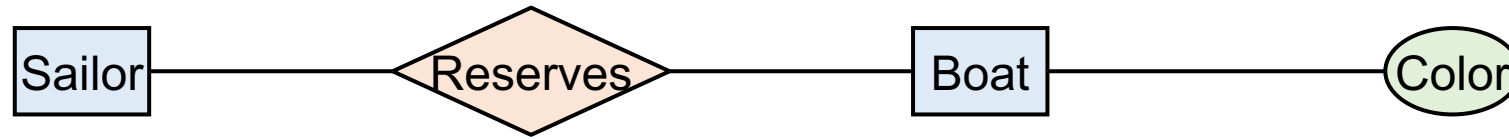
$$\exists x, \exists y [\text{Sailor}(x) \wedge \text{Boat}(y) \wedge \text{Reserves}(x, y)]$$

Concepts are existentially quantified variables

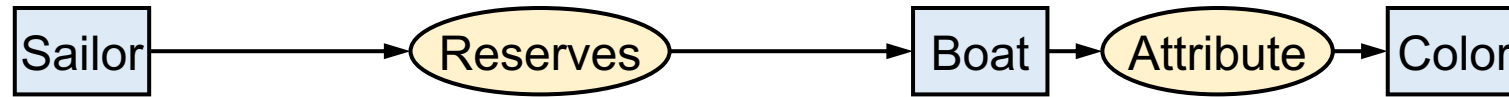
$$\exists x: \text{Sailor}, \exists y: \text{Boat} [\text{Reserves}(x, y)]$$

Concepts are typed variables in "Typed predicate calculus"

# Conceptual Graphs vs. ERD attributes and relations

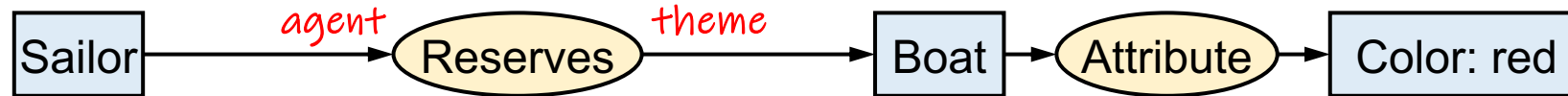


ER diagrams show "entity sets" and may include attributes



$\exists x: \text{Sailor}, \exists y: \text{Boat}, \exists z: \text{Color} [\text{Reserves}(x, y) \wedge \text{Attribute}(y, z)]$

CGs show statements about "entities" (no attributes)



$\exists x: \text{Sailor}, \exists y: \text{Boat} [\text{Reserves}(x, y) \wedge \text{Color}(\text{red}) \wedge \text{Attribute}(y, \text{red})]$

"Individual" concept (instead of "generic")

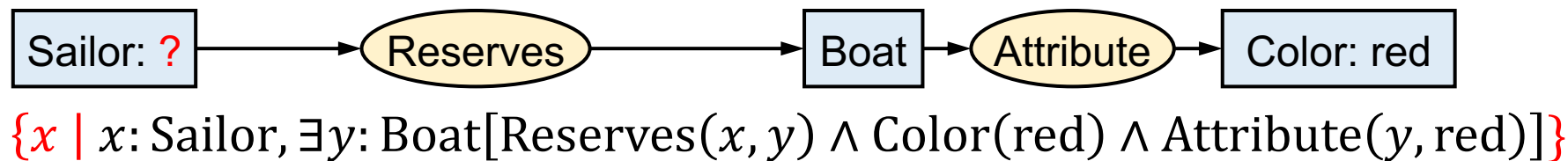
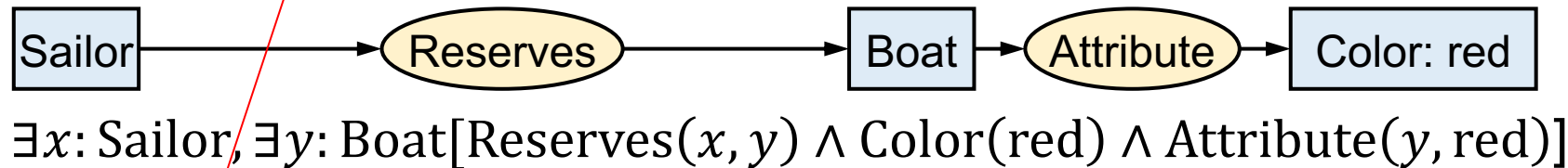


$\exists x: \text{Sailor}, \exists y: \text{Boat}, \exists z: \text{Reservation} [\text{Agent}(z, x) \wedge \text{Theme}(z, y) \wedge \text{Color}(\text{red}) \wedge \text{Attribute}(x, \text{red})]$

Former relation now represented as a concept, linked to its participants by "case relations"

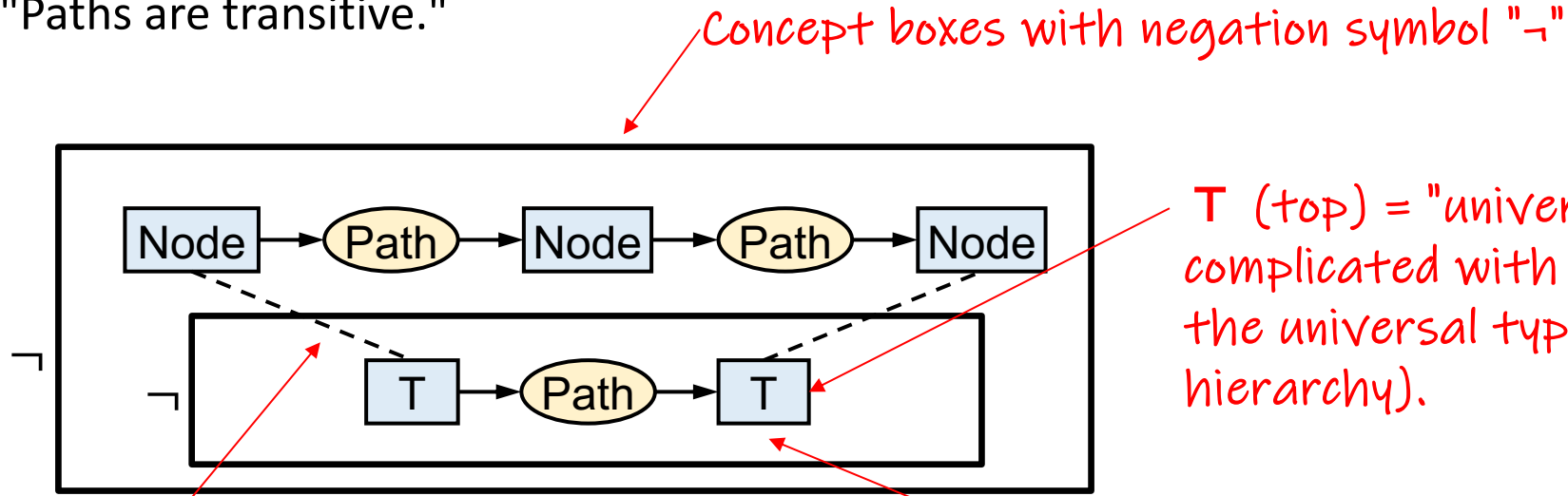
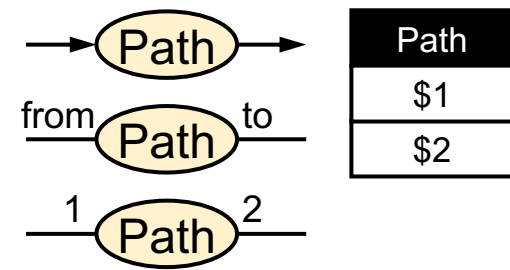
# Conceptual Graphs vs. ERD attributes and relations

A query graph is a conceptual graph that contains one or more concepts with a question mark in the referent field, as in [Sailor: ?]



# Conceptual Graphs: negation

"Paths are transitive."



**T** (top) = "universal type" (details a bit complicated with minor errors even in [Sowa'84], the universal type is the greatest type in a type hierarchy).

1. "Coreference" link (dotted line): both endpoints refer to same entity

2. Relations cannot be shown without concepts (concepts provide the required quantification). CGs within each "context" need to be a valid proposition (also within negated context). Thus the required quantification by **T** in the nesting

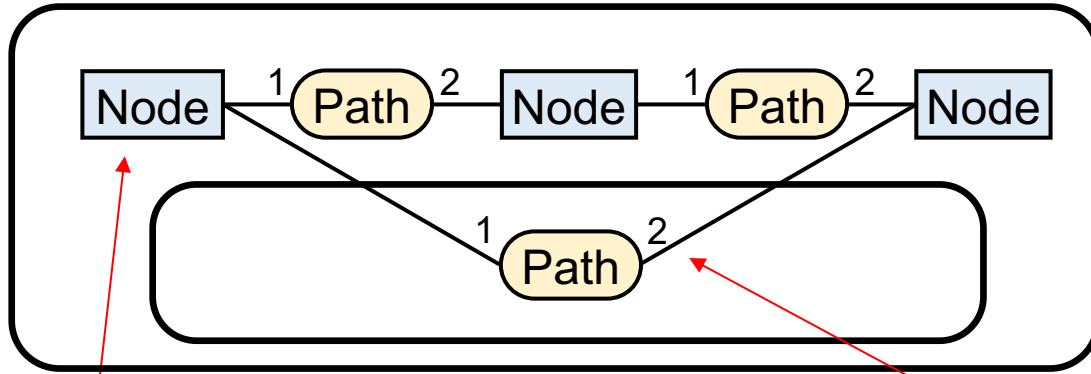
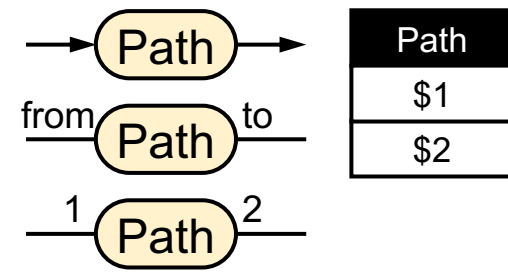
Translation to (domain relational) calculus:

$\neg(\exists x: \text{Node}, \exists y: \text{Node}, \exists z: \text{Node}[\text{Path}(x, y) \wedge \text{Path}(y, z) \wedge \neg(\text{Path}(x, z))])$

Meaning: "The relation 'Path' is transitive on entities of type 'Node'."

# Conceptual Graphs (Dau variant)

"Paths are transitive."



Dau's variant still requires concept nodes \*in addition\* to relation nodes

"The definition of Sowa does not suffice to derive a mathematical definition from it." [Dau'03]  
Dau streamlines various details for the purpose of FOL, leading to a more precise and simpler notation, called "concept graphs w/ cuts". We instead call them "conceptual graphs (Dau variant)"

1. Does not require any coreference links anymore.
2. Neither do graphs inside "cuts" (instead of "negative contexts") need to valid and thus locally quantified concepts for all relations

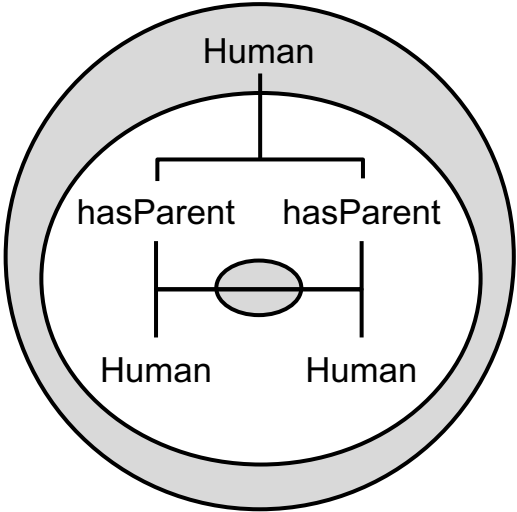
Translation to (domain relational) calculus:

$\neg(\exists x: \text{Node}, \exists y: \text{Node}, \exists z: \text{Node}[\text{Path}(x, y) \wedge \text{Path}(y, z) \wedge \neg(\text{Path}(x, z))])$

Meaning: "The relation 'Path' is transitive on entities of type 'Node'."

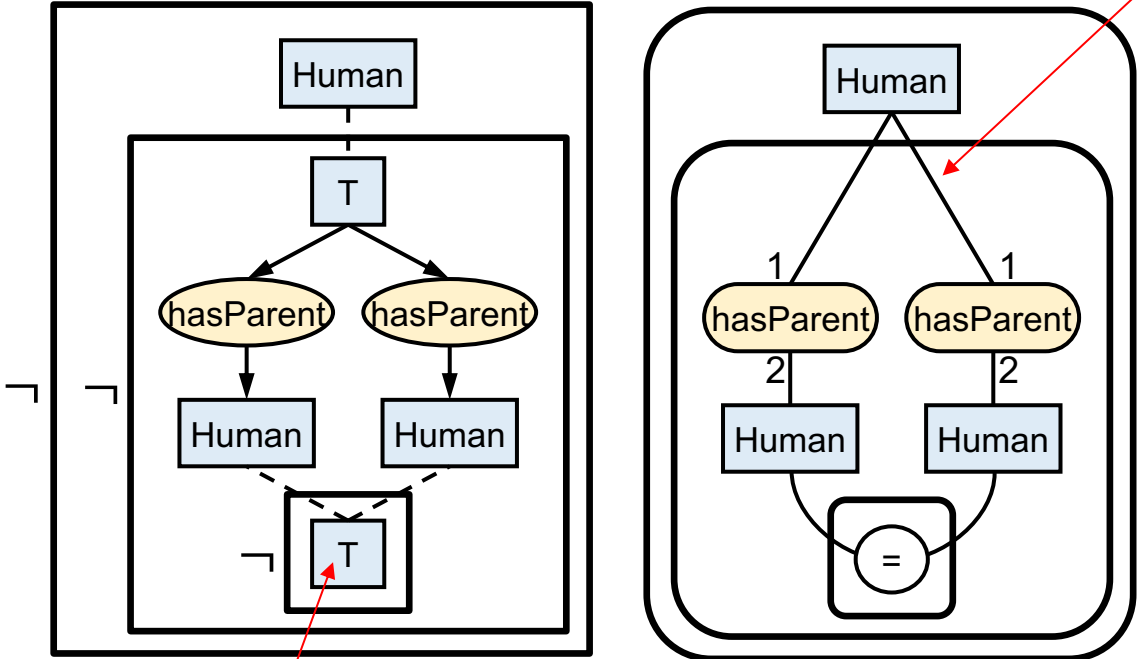
# Beta Existential Graph

"Every Human has at least two parents who are Human."



# Conceptual Graph

## Conceptual Graphs (Dau variant)



To express that  $y \neq z$ , we have to say "No entity exists that is equal to both  $y$  and  $z$ ."

## Translation:

DRC:  $\neg(\exists x[\text{Human}(x) \wedge \neg(\exists y, \exists z[\text{hasParent}(x, y) \wedge \text{Human}(y) \wedge \text{hasParent}(x, z) \wedge \text{Human}(z) \wedge \neg(y = z)])])$

# String Diagrams $\text{NPR}_\Sigma$ (2024)

Neo-Peircean Relations w/ signature  $\Sigma$

Sources used:

- Bonchi, Haydon, Di Giorgio, Sobocinski. Diagrammatic Algebra of First Order Logic, 2024. <https://arxiv.org/abs/2401.07055>
- Haydon, Sobocinski. Compositional Diagrammatic First-Order Logic, Diagrams 2020. [https://doi.org/10.1007/978-3-030-54249-8\\_32](https://doi.org/10.1007/978-3-030-54249-8_32)
- Bonchi, Seeber, Sobocinski. Graphical Conjunctive Queries, CSL 2018. <https://doi.org/10.4230/LIPIcs.CSL.2018.13>
- Personal communication with the authors

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# String Diagrams $\text{NPR}_\Sigma$

- "Neo-Peircean Relations" ( $\text{NPR}_\Sigma$ ) is variant of "string diagrams" that redefines Peirce's  $\beta$  Existential Graphs (EGs) in "category theory" (the details of which are hard to follow)  
String diagrams, formally arrows of a freely generated symmetric (strict) monoidal category, combine the rigour of traditional terms with a visual and intuitive graphical representation. Like traditional terms, they can be equipped with a compositional semantics.
- In contrast to Peirce's  $\beta$ -EGs, they can express queries due to an elegant visual distinction between 1) **free variables** (a line w/o marker) and 2) **bound variables** (a line with a **bullet as marker**), which seems graphically inspired by the "free hooks" notation of [Burch'91]
- They are 3) interpreted left-to-right, 4) use bullets also whenever a line splits into segments, and 5) use "photographic negatives" (alternatively shaded areas that also change foreground colors) for negation

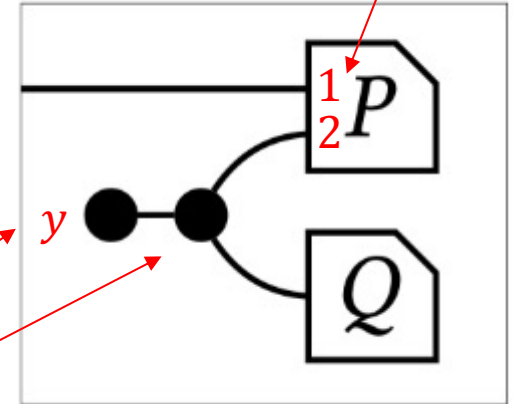
For all practical purposes, the arguments for predicates can be thought of as on the side only, and their order top-down.

The default for a line without marker, reaching the end of the bordered Canvas, is that it is free

A bullet at the end of a line means the variable is bound

The outer box (the limits of Peirce's "sheet of assertion") seems not strictly necessary, but simplifies the reading

$$\{(x) \mid \exists y[P(x, y) \wedge Q(y)]\}$$





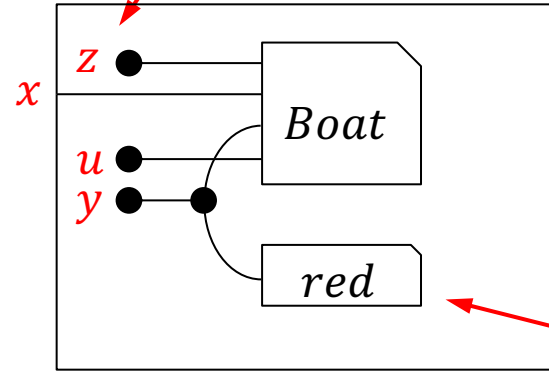
# String Diagrams $\text{NPR}_\Sigma$

Q1a: "Find boats that are red."

```
select distinct bname
from Boat
where color = 'red'
```

Schema

Boat
<u>bid</u>
bname
color
pdate



Marking bounded variables with bullet markers (and free variables without) allows a visual distinction necessary to represent relational queries

Constants (like 'red') are treated as unary predicates

## DRC (Domain Relational Calculus)

$\{(x) \mid \exists y, z, u [\text{Boat}(z, x, y, u) \wedge y = \text{'red'}]\}$

Comparison predicates ("before 1980", "pdate < 1980") are not supported.

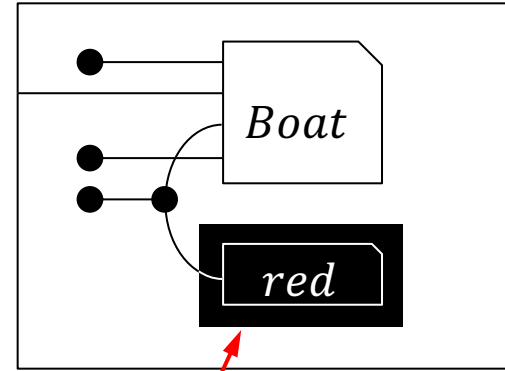
# String Diagrams $\text{NPR}_\Sigma$

Schema

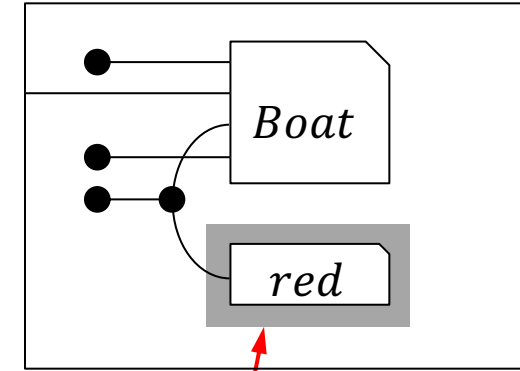
Boat
<u>bid</u>
bname
color
pdate

Q1b: "Find boats  
that are not red."

```
select distinct bname  
from Boat  
where color != 'red'
```



Negation is shown by switching  
colors black / white (notably both  
background and foreground) called  
"photograph negative"



This is the closest visual alternative  
had we applied Peirce's originally  
suggested "shading" of the  
background for negation, yet not  
changing the foreground.

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists y, z, u [\text{Boat}(z, x, y, u) \wedge y \neq \text{'red'}]\}$$

# String Diagrams $\text{NPR}_\Sigma$

Q1: "Find boats  
that are red or blue."

```
select distinct bname
from Boat
where color = 'red'
or color = 'blue'
```

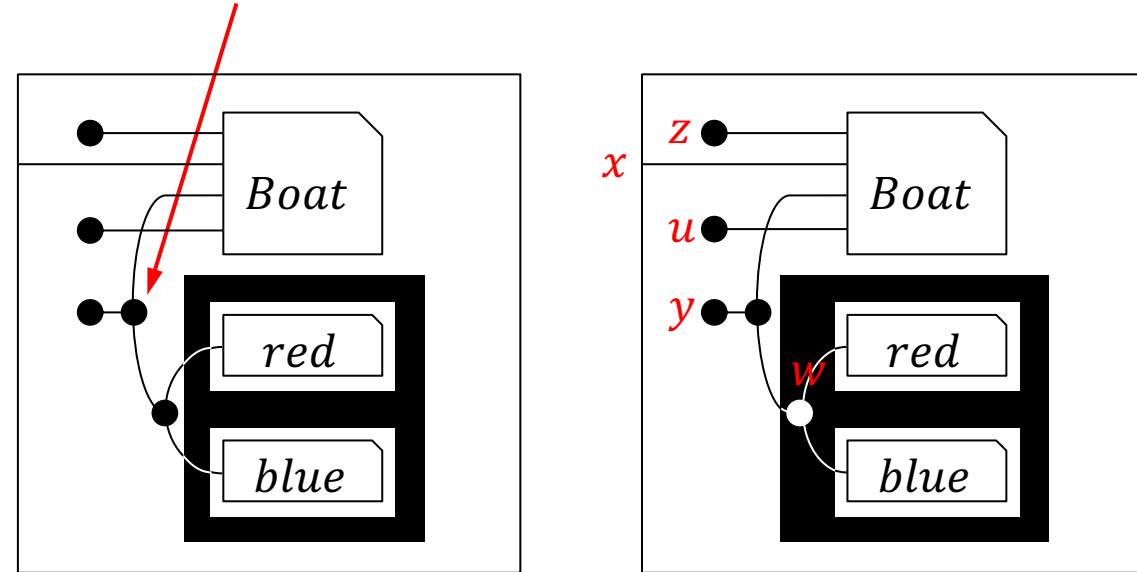
Comparison predicates such as  
" $\text{pdate} < 1980$ " are not supported

Disjunction of selection predicates  
can be represented via De Morgan  
(double-negation and conjunction)

## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge (y=\text{'red'} \vee y=\text{'blue'})]\}$$
$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\neg(y=\text{'red'}) \wedge \neg(y=\text{'blue'}))]\}$$

Because of considerations from category theory, every internal bullet can have maximally 3 outgoing lines in a strict syntactical sense (e.g. 1 incoming left and 2 outgoing right, but not 1 incoming left and 3 outgoing right). For practical visual purposes, this enforcement would not matter.



These two diagrams are logically identical, but have a slightly different "literal" interpretation. The right can be read as:

$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w [w=y \wedge \neg(w=\text{'red'}) \wedge \neg(w=\text{'blue'})])]\}$$

Schema

Boat
bid
bname
color
pdate

# String Diagrams $\text{NPR}_\Sigma$

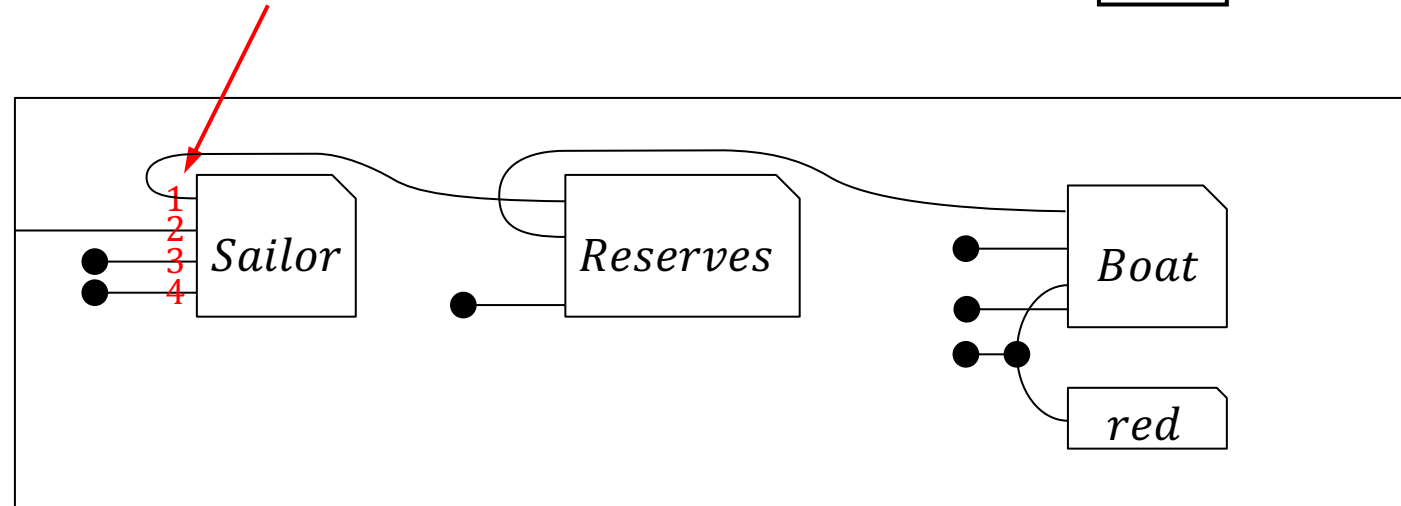
Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate

Lines from arguments of predicates follow the order from the relational schema



## DRC (Domain Relational Calculus)

$\{(x) \mid \exists v,z,w,y,t,u,s [\text{Sailor}(v,x,z,w) \wedge \text{Reserves}(v,y,t) \wedge \text{Boat}(y,u,\text{'red'},s)]\}$

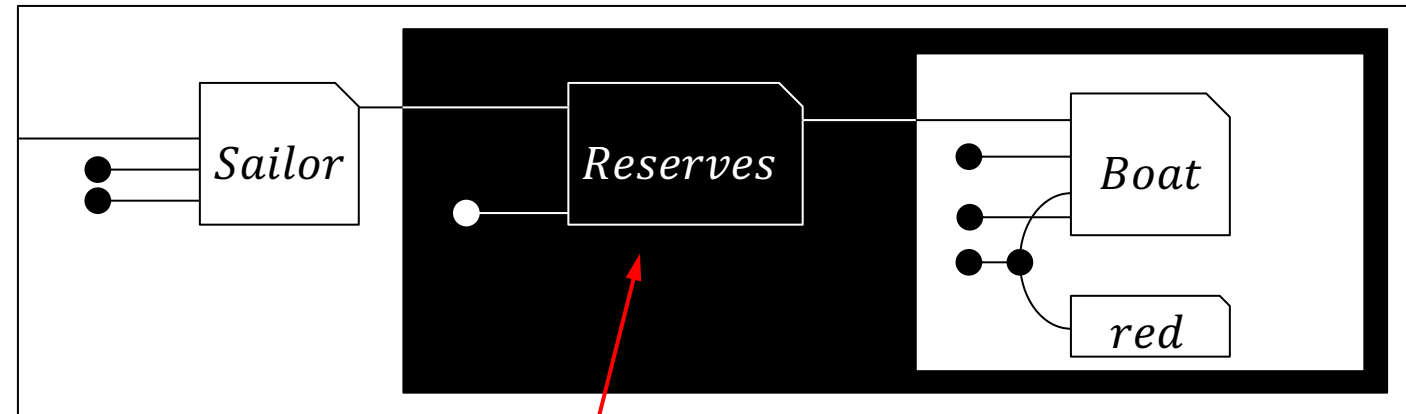
# String Diagrams $\text{NPR}_\Sigma$

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate



Negation is shown by using Peirce's "cuts" and switching colors between black / white (notably both background and foreground)

## DRC (Domain Relational Calculus)

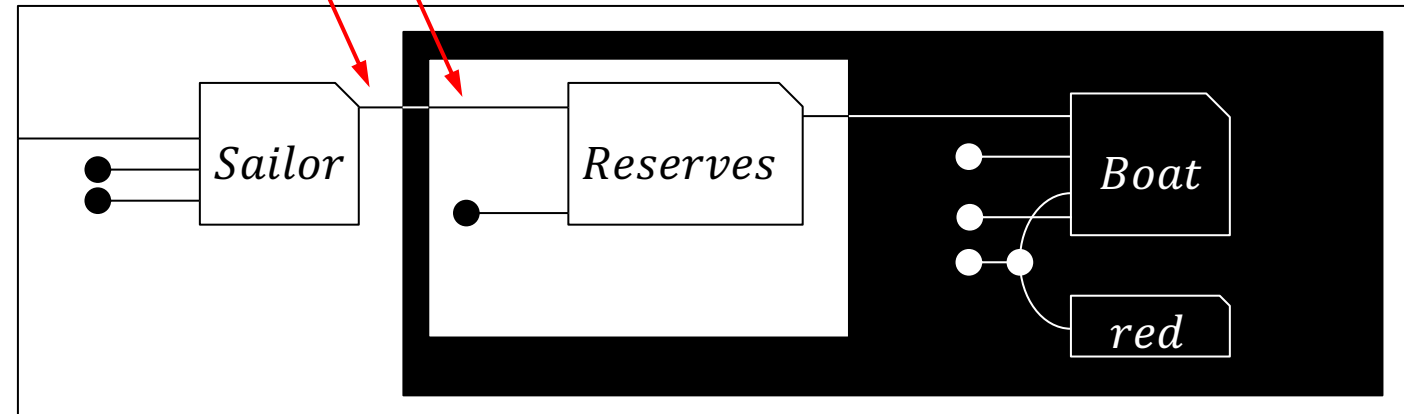
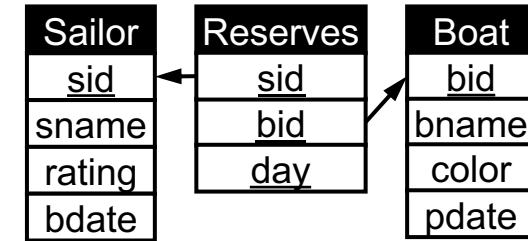
$$\{(\mathbf{x}) \mid \exists \mathbf{v}, \mathbf{z}, \mathbf{w} [\text{Sailor}(\mathbf{v}, \mathbf{x}, \mathbf{z}, \mathbf{w}) \wedge \neg(\exists \mathbf{y}, \mathbf{t} [\text{Reserves}(\mathbf{v}, \mathbf{y}, \mathbf{t}) \wedge \neg(\exists \mathbf{u}, \mathbf{s} [\text{Boat}(\mathbf{y}, \mathbf{u}, \text{'red'}, \mathbf{s})])])]\}]$$

# String Diagrams $\text{NPR}_\Sigma$

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

## Schema



## DRC (Domain Relational Calculus)

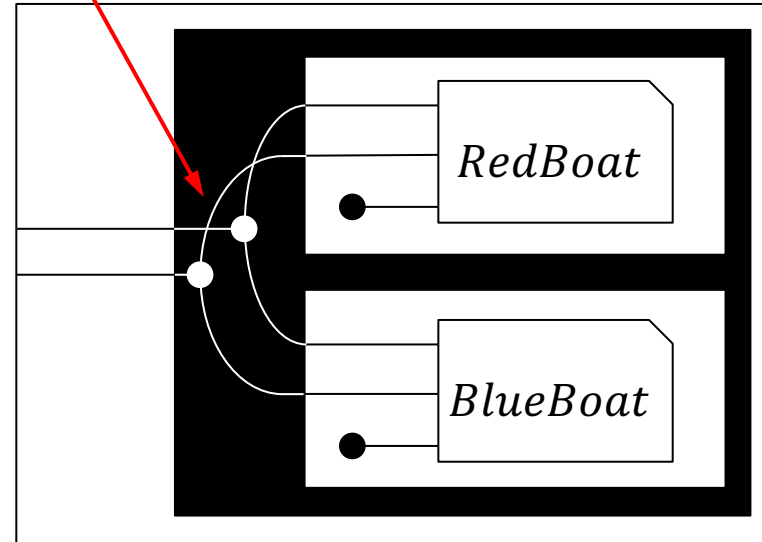
$$\{(\mathbf{x}) \mid \exists \mathbf{v}, \mathbf{z}, \mathbf{w} [\text{Sailor}(\mathbf{v}, \mathbf{x}, \mathbf{z}, \mathbf{w}) \wedge \neg(\exists \mathbf{y}, \mathbf{u}, \mathbf{s} [\text{Boat}(\mathbf{y}, \mathbf{u}, \text{'red'}, \mathbf{s}) \wedge \neg(\exists t [\text{Reserves}(\mathbf{v}, \mathbf{y}, t)])])]\}]$$

# String Diagrams $\text{NPR}_\Sigma$

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

Union of table can be represented via De Morgan (double-negation and conjunction). However, notice that the resulting expression is not safe (free variables  $x$  and  $y$  are not "guarded", i.e. not bound to an element from the active domain)



Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

## DRC (Domain Relational Calculus)

$\{(x,y) \mid \exists z [\text{RedBoat}(x,y,z) \vee \text{BlueBoat}(x,y,z)]\}$

$\{(x,y) \mid \neg(\neg(\exists z [\text{RedBoat}(x,y,z)]) \wedge \neg(\exists z [\text{BlueBoat}(x,y,z)]))\}$

An accessible overview of issues involving safety is: Topor, Safety and Domain Independence, Encyclopedia of Database Systems. 2009 [https://doi.org/10.1007/978-0-387-39940-9\\_1255](https://doi.org/10.1007/978-0-387-39940-9_1255)

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# BACKUP

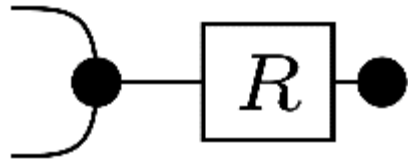
# String Diagrams



# String Diagrams $\text{NPR}_\Sigma$

In contrast to Peirce's  $\beta$ -EGs, the default for a line without bullet is to be free

The left side of predicates have "arities", the right side has "co-arities", a notion from category theory that appears to depend on the actual query, not just the schema. Here,  $R.2$  is the co-arity



$$\phi = \exists z_0 : (x_0 = x_1) \wedge R(x_0, z_0)$$

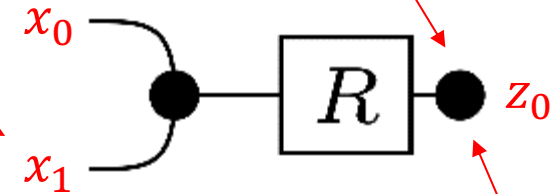
notation of paper

$$\{(x_0, x_1) \mid \exists z_0 [R(x_0, z_0) \wedge x_0 = x_1]\}$$

free

bound

notation of this survey

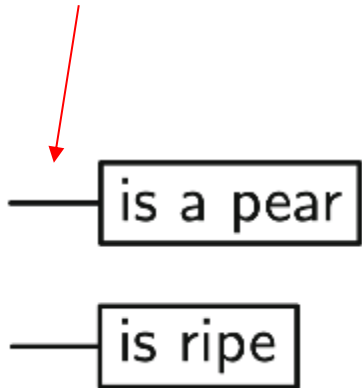


A bullet as arrowhead of a line binds a variable

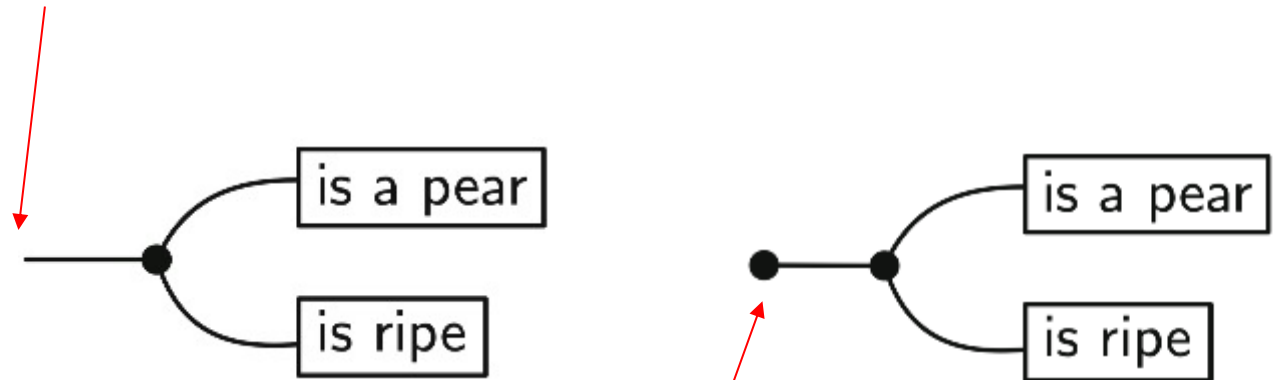
# String Diagrams $\text{NPR}_\Sigma$

Free variables: lines are dangling ("hooks are unfilled")

$\{(x, y) \mid \text{is\_a\_pear}(x) \wedge \text{is\_ripe}(y)\}$



$\{x \mid \text{is\_a\_pear}(x) \wedge \text{is\_ripe}(x)\}$

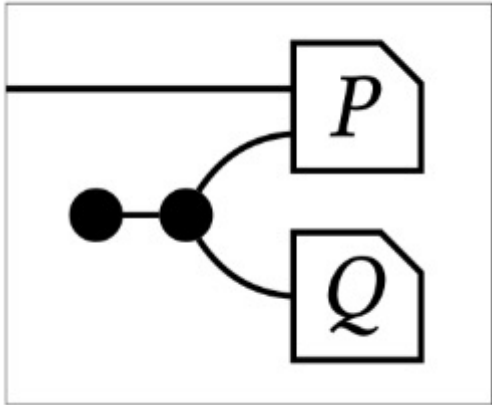


$\exists x [\text{is\_a\_pear}(x)] \wedge \exists y [\text{is\_ripe}(y)]$

Bound variables: lines are capped off with a bullet as arrowhead

$\exists x [\text{is\_a\_pear}(x) \wedge \text{is\_ripe}(x)]$

# String Diagrams $\text{NPR}_\Sigma$



FOL formula  $\exists x_2. P(x_1, x_2) \wedge Q(x_2)$

notation of paper

Outer bounding box appears not necessary

The order of arguments for predicates seems top down.

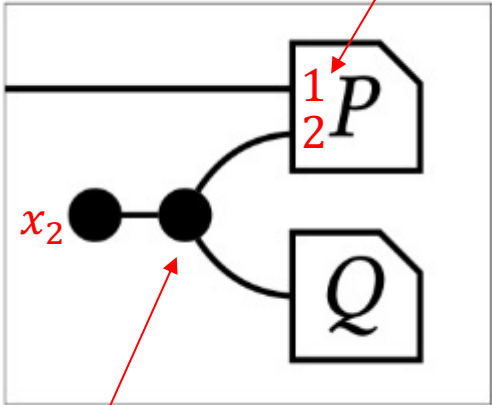
Free variable

Bound variable w/ bullets at line end

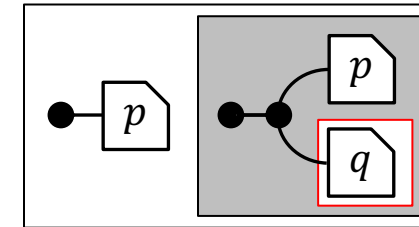
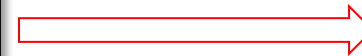
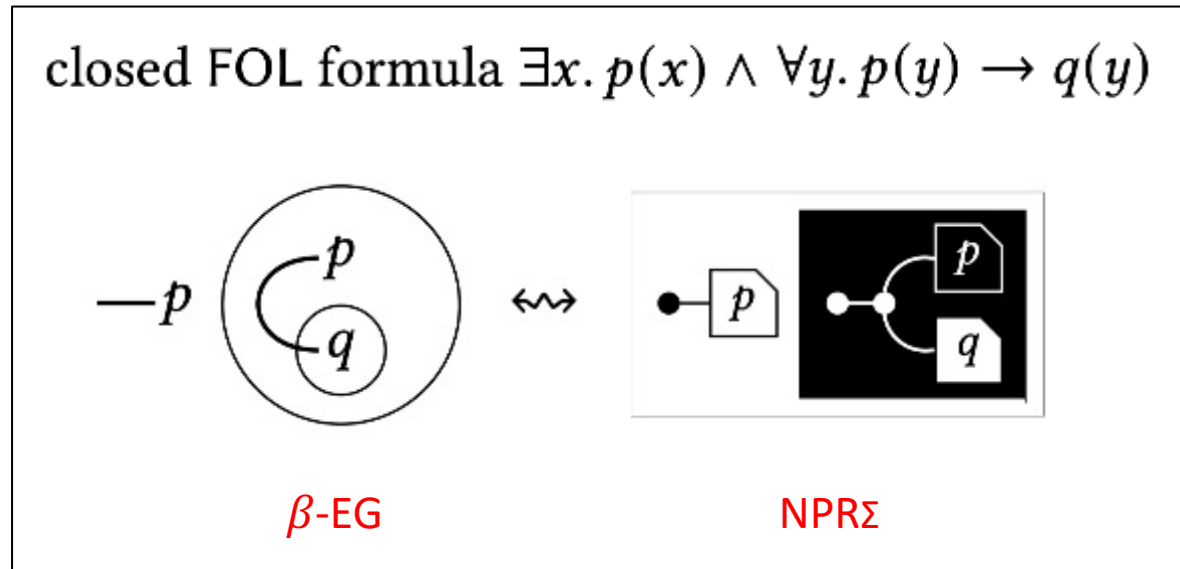
Bullets are also used for splitting / connecting line segments

$\{(x_1) \mid \exists x_2 [P(x_1, x_2) \wedge Q(x_2)]\}$

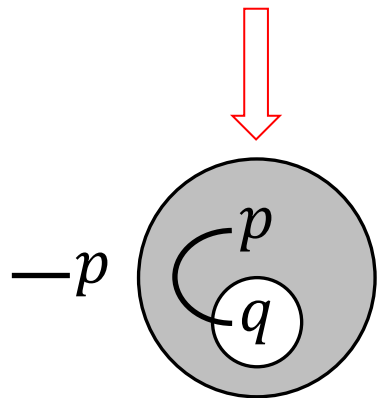
notation of this survey



# Connection of String Diagrams $\text{NPR}_\Sigma$ to Peirce's $\beta$ -EGs



$\text{NPR}_\Sigma$  with "Peirce shading" which would separates the depiction of the predicates and variables (the foreground is always in black) from the alternatively shaded and nested bounding boxes (notice here the red bounding box missing on the left)



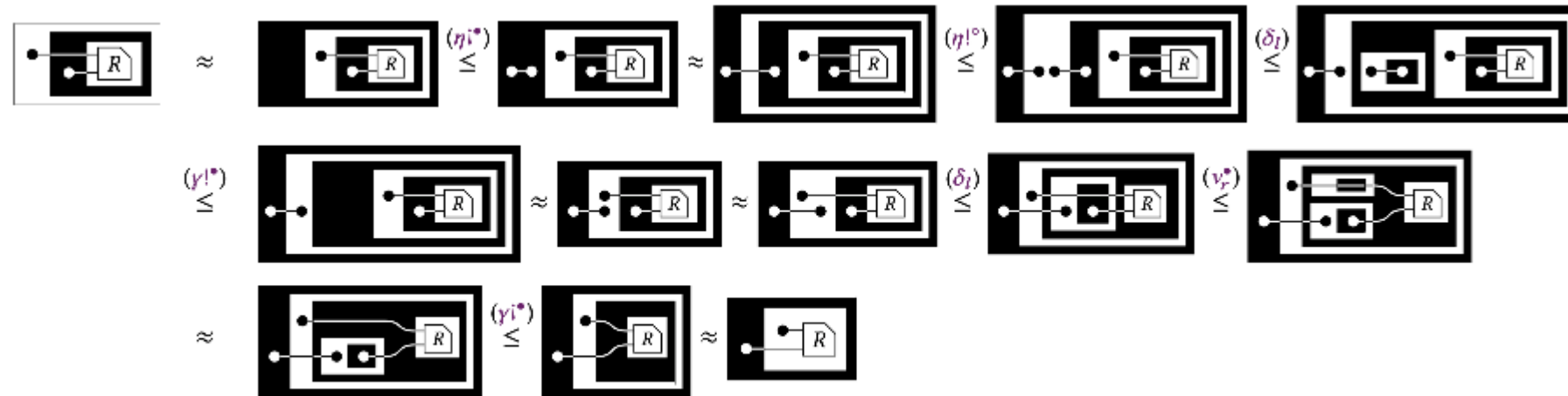
$\beta$ -EG with shading proposed by Peirce

# Contrast "Diagrammatic representation" from "Diagrammatic reasoning"

Our main focus in "diagrammatic representation (of relational queries)" is to help users quickly and unambiguously understand the semantics of a query. In contrast, the focus in "diagrammatic reasoning" is to support proofs in a visual formalism.

Example:  $\exists x. \forall y. R(x, y) \models \forall y. \exists x. R(x, y)$

$$\exists x. \forall y. R(x, y) \quad \leq \quad \forall y. \exists x. R(x, y)$$



**Figure 10: Completely axiomatic proof of (1).**

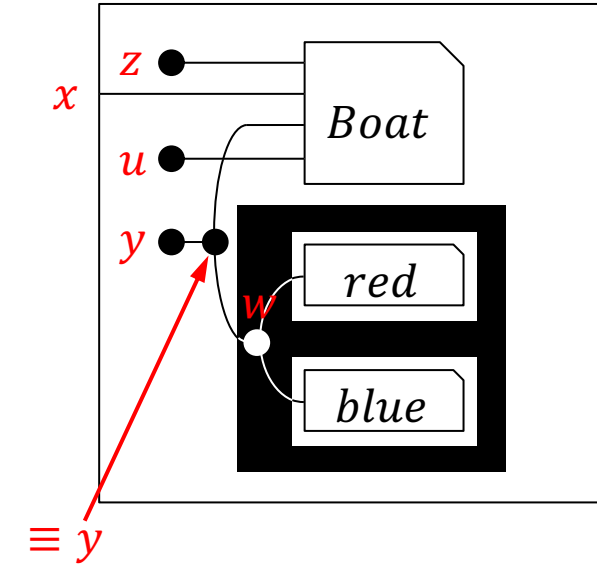
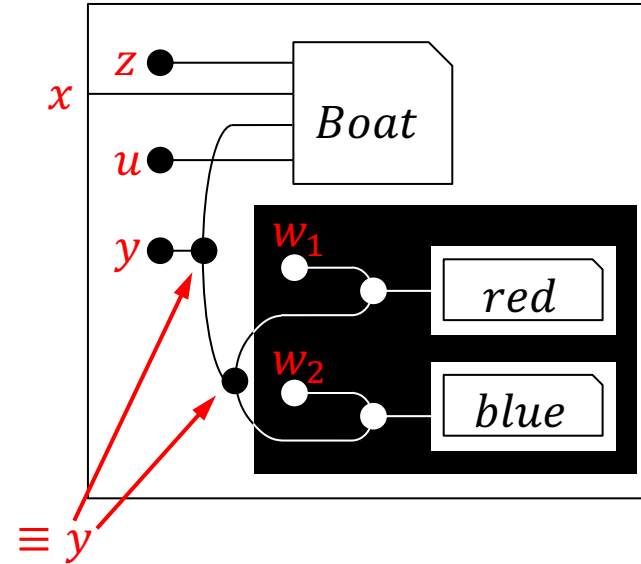
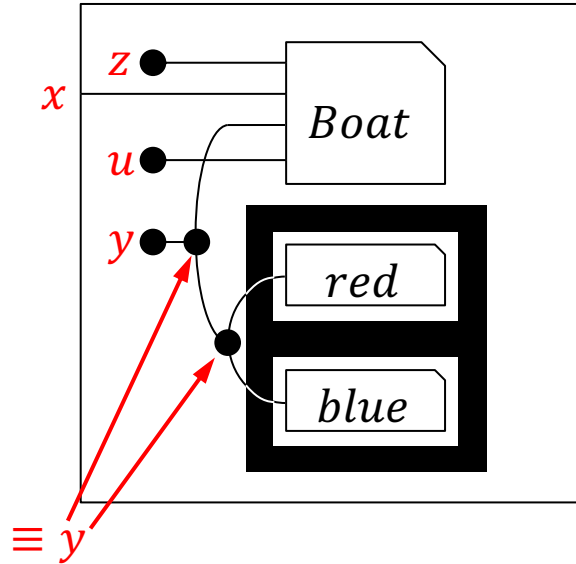
# String Diagrams $\text{NPR}_\Sigma$

Q1: "Find boats that are red or blue."

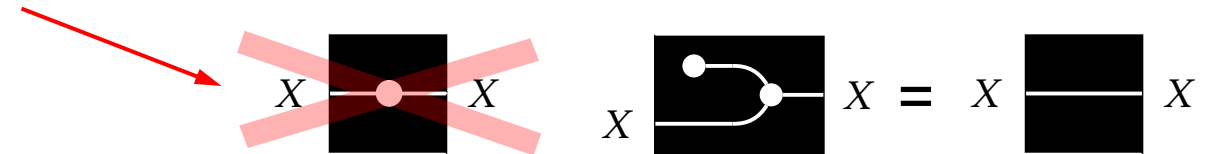
Three equivalent representations with slightly different "literal" interpretation

Schema

Boat
bid
bname
color
pdate



The strict syntax does not allow to have a dot attached to a line on the left and a line on the right (but intuitively, that's the interpretation):



## DRC (Domain Relational Calculus)

left:  $\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\neg(y=\text{'red'}) \wedge \neg(y=\text{'blue'}))]\}$

middle:  $\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w_1,w_2 [w_1=y \wedge w_2=y \wedge \neg(w_1=\text{'red'}) \wedge \neg(w_2=\text{'blue'})])]\}$

right:  $\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w [w=y \wedge \neg(w=\text{'red'}) \wedge \neg(w=\text{'blue'})])]\}$

Based on personal communication with the authors

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Intended Agenda today

Please leave  
feedback 😊



1. Why visualizing queries and why now?
2. Principles of Query Visualization
3. Logical foundations of relational query languages
4. (Early) Diagrammatic representations
5. Visual Query Representations (from DB community)
6. Lessons Learned and Open Challenges

## Part 5: Visual query representations (from DB community)

- We next look at various visual representations for relational queries that were proposed from \*inside\* the database community.
- Many of these formalisms were proposed as "Visual Query Language" and thus as alternative to SQL for specifying queries.
- Our perspective is thus often different from the original authors' goals: here, we are only interested the visual formalisms.



# Part 5: Visual query representations (from DB community)

How the selection of work was made:

- 1) if highly cited or influential, or
  - 2a) it represents a didactically interesting type of visualizations, and
  - 2b) documentation was easy enough to find and use

Please leave feedback  
on the tutorial page 😊



DISCLAIMER 1: I may be missing relevant work. If you think I did, please let me know.

DISCLAIMER 2: It's my best effort to understand the visual representation implied by an approach, based on available information (it's surprisingly hard to create visualizations for new queries, based on paper write-ups). I may have gotten things wrong. If you spot an error, let me know where, and how I can fix.

DISCLAIMER 3: query composition has its own challenges separate from visualization. Thus the focus of some tools may not have been on the "visual alphabet", and the tools have other interesting contributions (like the interactive exploration, or spreadsheet-type interface). Our focus today is uniquely on the visual representation.

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# QBE (1977)

## (Query-By-Example)

Sources used:

- Zloof. Query-by-Example: A Data Base Language. IBM Systems Journal 16(4). 1977. <https://doi.org/10.1147/sj.164.0324>
- Ramakrishnan, Gehrke. Database management systems, 2nd ed, 2000. Section 6. <https://pages.cs.wisc.edu/~dbbook/openAccess/thirdEdition/qbe.pdf>
- Elmasri, Navathe. Fundamentals of Database Systems, 7th ed, 2015. Appendix C. <https://dl.acm.org/doi/10.5555/2842853>

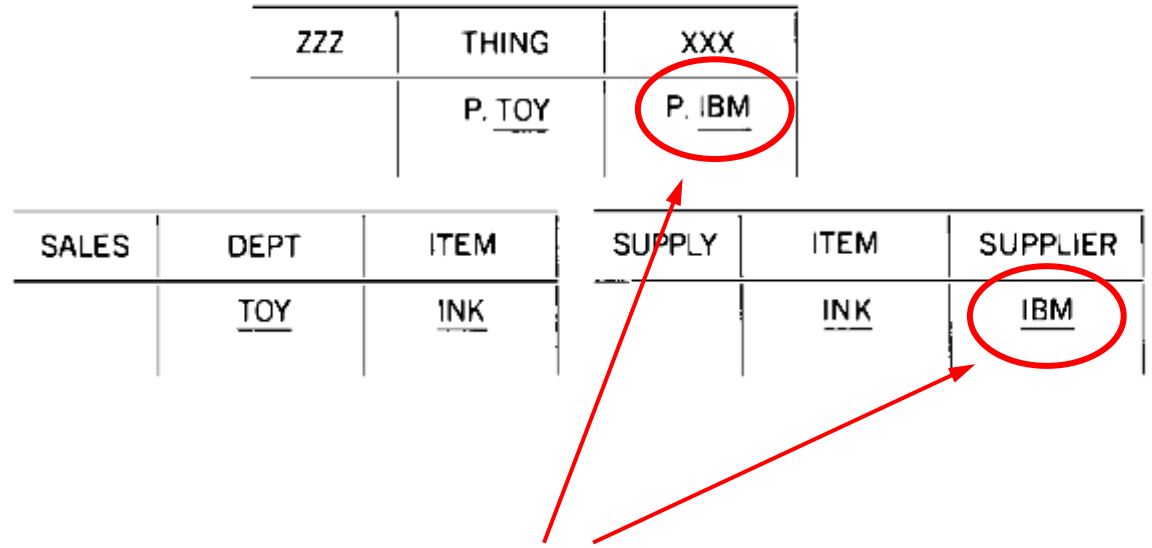
A nice comparison of various extensions is "Ozsoyoglu, Wang. Example-Based Graphical Database Query Languages. Computer, 1993. <https://doi.org/10.1109/2.211893> "

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# QBE (Query-By-Example)

- Developed in 1970s and thus one of the first "**graphical**" query languages developed for database systems.
- Influential for later interactive query composition tools, in particular "Example-Based Graphical Database Query Languages"

Figure 19 Retrieval of collected output from multiple tables



- User specify queries using **two-dimensional forms**. The "examples" are actually variables, motivated from DRC (domain relational calculus).
- "**Query-By-Form**" would be more appropriate than "Query-By-Example"
- Described by the creator Zloof as "the first visual programming language". But is QBE really "visual", i.e. is it diagrammatic? (I would rather call it a 2D variant of Datalog)

# QBE (Query-By-Example)

Q1b: "Find boats that are not red."

```
select distinct bname
from Boat
where color != 'red'
```

Boat	bid	bname	color	pdate
		P	!=red	
	101	Interlake	blue	4/10/13
	103	Clipper	green	4/10/13

Original visualization in 1977 paper, inspired by the way relations were written out. Also used by [Gehrke Ramakrishnan'00]

Actual database table

Schema

Boat
<u>bid</u>
bname
color
pdate

Relational schema provides a template

Influenced by DRC and similar to Datalog

Datalog

$P(x) :- \text{Boat}(\_x, y, \_), y \neq \text{'red'}$

**Boat**

bid	bname	color	pdate
	P.	!=red	

More modern variant, based on UML notations. Also used by [Elmasri Navathe'15]

P. = "Print" = part of output

# QBE (Query-By-Example)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```

**Boat**

bid	bname	color	pdate
	P.	red	
	P.	blue	

← Conditions in distinct rows  
are connected by "OR"

## Datalog

$P(x) :- \text{Boat}(\_, x, \text{'red'}, \_)$

$P(x) :- \text{Boat}(\_, x, \text{'blue'}, \_)$

# QBE (Query-By-Example)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Intuitively, QBE represents  
the selection predicates in DNF

```
... where (color = 'red' and pdate < 1980)
or (color = 'blue' and pdate < 1980)
```

**Boat**

bid	bname	color	pdate
	P.	red	<1980
	P.	blue	<1980

← Conditions in the same row  
are connected by "AND"

← Conditions in distinct rows  
are connected by "OR"

## Datalog

$P(x) :- \text{Boat}(\_,x,\text{'red'},z), z < 1980$

$P(x) :- \text{Boat}(\_,x,\text{'blue'},z), z < 1980$

# QBE (Query-By-Example)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

**Boat**

bid	bname	color	pdate
	P.	<u>c</u>	<u>d</u>

**Conditions**

d<1980 and (c=red or c=blue)

Variables (of arbitrary name) are expressed with underscores

A "conditions box" allows to express more complicated conditions in a strictly linguistic way

## Datalog

$P(x) :- \text{Boat}(\_,x,\text{'red'},z), z < 1980$

$P(x) :- \text{Boat}(\_,x,\text{'blue'},z), z < 1980$



# QBE (Query-By-Example)

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Question to the audience:  
which of those two query expressions  
is "visual", which one is not?



Schema

Boat
<u>bid</u>
bname
color
pdate

Disjunctions in Datalog are not  
standard but used in some Datalog  
implementations like Souffle  
(see <https://souffle-lang.github.io/rules#disjunction>)

## Datalog (Souffle syntax)

$P(x) \text{ :- Boat}(x, \_, y, z), z < 1980, (y = \text{red}; y = \text{blue})$

### Boat

bid	bname	color	pdate
	P.	_c	_d

### Conditions

$\_d < 1980 \text{ and } (\_c = \text{red or } \_c = \text{blue})$

# QBE (Query-By-Example)

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Question to the audience:  
which of those two query expressions  
is "visual", which one is not?

What about now?



Schema

Boat
<u>bid</u>
bname
color
pdate

Disjunctions in Datalog are not  
standard but used in some Datalog  
implementations like Souffle

(see <https://souffle-lang.github.io/rules#disjunction>)

We now chose more "readable" variable  
names

## Datalog (Souffle syntax)

P(bname) :- Boat(bname,\_,color,pdate), pdate<1980, (color=red; color=blue)

### Boat

bid	bname	color	pdate
	P.	_c	_d

### Conditions

\_d<1980 and (\_c=red or \_c=blue)

# QBE (Query-By-Example)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Question to the audience:  
which of those two query expressions  
is "visual", which one is not?

I believe QBE should not be called a "visual programming language" (any more than Datalog); and *\*we\** should stop continuing this historical misclassification in our undergraduate database classes!

Disjunctions in Datalog are not standard but used in some Datalog implementations like Souffle  
(see <https://souffle-lang.github.io/rules#disjunction>)  
We now chose more "readable" variable names

## Datalog (Souffle syntax)

P(bname) :- Boat(bname,\_,color,pdate), pdate<1980, (color=red; color=blue)

### Boat

bid	bname	color	pdate
	P.	_c	_d

### Conditions

\_d<1980 and (\_c=red or \_c=blue)

# QBE (Query-By-Example)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

The "join structure" is not visualized  
any different from Datalog!

**Sailor**

sid	sname	rating	bdate
_y	P.		

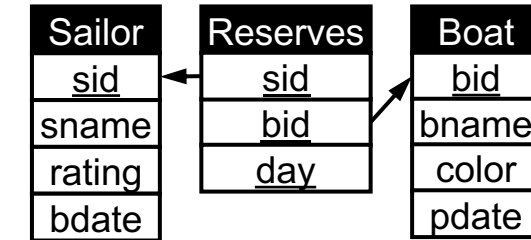
**Reserves**

sid	bid	day
_y	_x	

**Boat**

bid	bname	color	pdate
_x		red	

**Schema**



## Datalog

$Q(z) :- \text{Sailor}(y, z, \_, \_), \text{Reserves}(y, x, \_), \text{Boat}(x, \_, 'red', \_)$

# QBE (Query-By-Example)

Q2a: "Find sailors and red boats they reserved."

```
select distinct S.sname, B.bname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

The "join structure" is not visualized any different from Datalog!

## Datalog

$Q(z,w) \text{ :- } \text{Sailor}(y,z,\_,\_), \text{Reserves}(y,x,\_), \text{Boat}(x,w,\text{'red'},\_,\_)$

**Sailor**

sid	sname	rating	bdate
<u>_y</u>	<u>_z</u>		

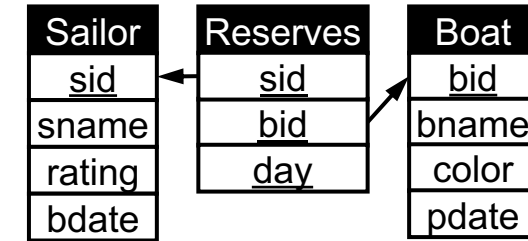
**Reserves**

sid	bid	day
<u>_y</u>	<u>_x</u>	

**Boat**

bid	bname	color	pdate
<u>_x</u>	<u>_w</u>	red	

**Schema**



**Output**

sname	bname
P._z	P._w

We need a separate output table in order to collect attributes from different input tables

# QBE (Query-By-Example)

Double negations need to create an intermediate table, just like in Datalog

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

Symbol for negation

Boat			
bid	bname	color	pdate
$\neg$ _y		red	

Reserves		
sid	bid	day
_x	_y	

BadSid	
sid	
$\neg$ _x	

Sailor			
sid	sname	rating	bdate
_z	P.		

BadSid	
sid	
$\neg$ _z	

Insert into temporary table "BadSid" sailors who reserved at least one non-red boat

## Datalog

```
RedBoat(y) :- Boat(y,_, 'red',_)
BadSid(x) :- Reserves(x,y,_), not RedBoat(y)
Q(w) :- Sailor(z,w,_,_), not BadSid(z)
```

QBE seems to allow a specification that would be unsafe in Datalog: "..., not Boat(y,\_, 'red',\_)". Datalog needs to use an extra intermediate relation "RedBoat"

# QBE (Query-By-Example)

Double negations need to create an intermediate table, just like in Datalog

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

Symbol for negation

Boat			
bid	bname	color	pdate
$\neg$ _y		red	

Reserves		
sid	bid	day
_x	_y	

BadSid	
sid	
$\neg$ _x	

Sailor			
sid	sname	rating	bdate
_z	P.		

BadSid	
sid	
$\neg$ _z	

Insert into temporary table "BadSid" sailors who reserved at least one non-red boat

Datalog's safety conditions do not allow negation of (anonymous) variables that are not guarded. Thus we need an intermediate table "RedBoat". But for anonymous variables that could be a simple syntactic extension...

## Datalog

```
RedBoat(y) :- Boat(y,_, 'red', _)
BadSid(x) :- Reserves(x,y,_), not RedBoat(y)
Q(w) :- Sailor(z,w,_,_), not BadSid(z)
```

BadSid(x) :- Reserves(x,y,\_), not Boat(y, ~~\_,~~ 'red', ~~\_,~~)

# QBE (Query-By-Example)

Double negations need to create an intermediate table, just like in Datalog

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

Boat			
bid	bname	color	pdate
$\neg$ _y		red	

Sailor			
sid	sname	rating	bdate
_z	P.		

Reserves		
sid	bid	day
_x	_y	

BadSid	
sid	
$\neg$ l. _x	
$\neg$ _z	

A possible way to make it more succinct (not 100% sure if supported in any current implementations)

## Datalog

```
RedBoat(y) :- Boat(y,_, 'red', _)
BadSid(x) :- Reserves(x, y, _), not RedBoat(y)
Q(w) :- Sailor(z, w, _, _), not BadSid(z)
```



# QBE (Query-By-Example)

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

**Sailor**

sid	sname	rating	bdate
_x			

**Reserves**

sid	bid	day
¬ _x	_y	

**Boat**

bid	bname	color	pdate
_y		red	

**BadSid**

sid
l. _x

**Sailor**

sid	sname	rating	bdate
_z	P.		

**BadSid**

sid
¬ _z

## Datalog

$I(x,y) :- \text{Reserves}(x,y,\_)$   
 $\text{BadSid}(x) :- \text{Sailor}(x,\_,\_,\_), \text{Boat}(y,\_,\text{'red'},\_), \text{not } I(x,y)$   
 $Q(w) :- \text{Sailor}(z,w,\_,\_), \text{not } \text{BadSid}(z)$

*BadSid: sailors who have not reserved at least one red boat*

# QBE (Query-By-Example)



Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

**Sailor**

sid	sname	rating	bdate
_x			
_z	P.		

**Reserves**

sid	bid	day
¬ _x	_y	

**Boat**

bid	bname	color	pdate
_y		red	

**BadSid**

sid
l. _x
¬ _z

Not clear if any currently available system supports the query in this more compact representation (using every table only once). But it looks even more complicated when reusing the tables (what is the order in which to read?)

## Datalog

$I(x,y) :- \text{Reserves}(x,y, \_)$

$\text{BadSid}(x) :- \text{Sailor}(x, \_, \_, \_), \text{Boat}(y, \_, 'red', \_), \text{not } I(x,y)$

$Q(w) :- \text{Sailor}(z, w, \_, \_), \text{not } \text{BadSid}(z)$

# QBE (Query-By-Example)

which query is "visual" and which is not ?

1:

```
I(sid,bid) :- Reserves(sid,bid,_)  
  
BadSid(sid) :- Sailor(sid,_,_,_), Boat(bid,_, 'red',_),  
               not I(sid,bid)  
  
Q(sname) :- Sailor(sid,sname,_,_),  
            not BadSid(sid)
```

2:

Sailor

sid	sname	rating	bdate
_x			

Boat

bid	bname	color	pdate
_y		red	

Sailor

sid	sname	rating	bdate
_z	P.		

Reserves

sid	bid	day
¬_x	_y	

BadSid

sid
l. _x

BadSid

sid
¬_z

# QBE (Query-By-Example)

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

[Zlopf'77] suggests that we need a separate output tuple for expressing a table union

**RedBoat**

bid	bname	pdate
_i1	_n1	

**BlueBoat**

bid	bname	pdate
_i2	_n2	

**Output**

bid	bname
P._i1	P._n1
P._i2	P._n2

**Schema**

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

## Datalog

$Q(x,y) \text{ :- RedBoat}(x,y,\_)$   
 $Q(x,y) \text{ :- BlueBoat}(x,y,\_)$

# QBE (1977) (Query-By-Example) Backup

# QBE (Query-By-Example)

*Retrieval using a negation.* Print the departments that sell an item not supplied by the Pencraft Company. This query is shown in Figure 17. Here the not ( $\neg$ ) operator is applied against the entire query expression in the SUPPLY table. This query may be paraphrased as follows. Print department names for items INK such that it is not the case that PENCRAFT supplies INK. In other words, the system is to look for (INK, PENCRAFT) throughout the entire table, and only if it does not find that entry is the corresponding department printed. This query is different from the following one.

Figure 17 Retrieval using a negation

SALES	DEPT	ITEM	SUPPLY	ITEM	SUPPLIER
	P.	<u>INK</u>	$\neg$	<u>INK</u>	PENCRAFT

*Retrieval using a negation.* Print the departments that sell items supplied by a supplier other than the Pencraft Company. This query is illustrated by Figure 18. Here the system retrieves data in the SUPPLY table with suppliers different from Pencraft, and then retrieves the relevant departments. Note that (INK, PENCRAFT) might also exist.

Figure 18 Retrieval using a negation

SALES	DEPT	ITEM	SUPPLY	ITEM	SUPPLIER
	P.	<u>INK</u>		<u>INK</u>	$\neg$ PEN CRAFT

# QBE (Query-By-Example)

*Retrieval of collected output from multiple tables.* Print out each department with its corresponding suppliers. Since the output must be a new table, the user must generate a third table skeleton, and fill it in with examples mapped from the two existing tables that satisfy the stipulation of the query. Since it is a user-created table—and, therefore, does not correspond to stored data—the user can fill in the required descriptive headings or leave them blank. This is shown in Figure 19.

**Figure 19   Retrieval of collected output from multiple tables**

ZZZ	THING	XXX
	P. <u>TOY</u>	P. <u>IBM</u>

SALES	DEPT	ITEM
	<u>TOY</u>	<u>INK</u>

SUPPLY	ITEM	SUPPLIER
	<u>INK</u>	<u>IBM</u>

# QBE (Query-By-Example)

Print the names of employees whose salary is between \$10000 and \$15000, provided it is not \$13000, as shown in Figure 22. The use of the same example element JONES in all three rows implies that these three conditions are **ANDed** on the employee JONES.

Figure 22 Implicit AND operation

EMP	NAME	SAL
	P. <u>JONES</u>	>10000
	<u>JONES</u>	<15000
	<u>JONES</u>	¬ 13000

Figure 24 AND operation using condition box

EMP	NAME	SAL
	P.	<u>S1</u>

CONDITIONS
<u>S1</u> = (>10000 & <15000 & ¬13000)

Print the names of employees whose salary is either \$10000 or \$13000 or \$16000. This is illustrated in Figure 23. Different example elements are used in each row, so that the three lines express independent queries. The output is the union of the three sets of answers. (In this example, the P.'s alone would have been sufficient.)

Figure 23 Implicit OR operation

EMP	NAME	SAL
	P. <u>JONES</u>	10000
	P. <u>LEWIS</u>	13000
	P. <u>HENRY</u>	16000

Figure 25 OR operation using condition box

EMP	NAME	SAL
	P.	<u>S1</u>

CONDITIONS
<u>S1</u> = (10000   13000   16000)



# QBE (Query-By-Example)

We can print the names of sailors who do *not* have a reservation by using the  $\neg$  command in the relation name column:

<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>	<i>Reserves</i>	<i>sid</i>	<i>bid</i>	<i>day</i>
	$\_Id$	P. $\_S$			$\neg$	$\_Id$		

The use of  $\neg$  in the relation-name column gives us a limited form of the set-difference operator of relational algebra. For example, we can easily modify the previous query to find sailors who are not (both) younger than 30 and rated higher than 4:

<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>	<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>
	$\_Id$	P. $\_S$			$\neg$	$\_Id$		$> 4$	$< 30$

# QBE (Query-By-Example)

*Q: "Print the names of sailors who are younger than 30 or older than 20."*

<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>
		P.		< 30
		P.		> 20

*Q: "Print the names of sailors who are both younger than 30 and older than 20."*

<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>
	_Id	P.		< 30
	_Id			> 20

# QBE (Query-By-Example)

*Find sailors who have reserved all boats.*

$$\{\langle I, N, T, A \rangle \mid \langle I, N, T, A \rangle \in \text{Sailors} \wedge \neg \exists \langle B, BN, C \rangle \in \text{Boats} \\ (\neg \exists \langle Ir, Br, D \rangle \in \text{Reserves} (I = Ir \wedge Br = B))\}$$

One way to achieve such control is to break the query into several parts by using temporary relations or views. As we saw in Chapter 4, we can accomplish division in two logical steps: first, identify *disqualified* candidates, and then remove this set from the set of all candidates. In the query at hand, we have to first identify the set of *sids* (called, say, BadSids) of sailors who have not reserved some boat (i.e., for each such sailor, we can find a boat not reserved by that sailor), and then we have to remove BadSids from the set of *sids* of all sailors. This process will identify the set of sailors who've reserved all boats. The view BadSids can be defined as follows:

<i>Sailors</i>	<i>sid</i>	<i>sname</i>	<i>rating</i>	<i>age</i>	<i>Reserves</i>	<i>sid</i>	<i>bid</i>	<i>day</i>
	<u>Id</u>				$\neg$	<u>Id</u>	<u>B</u>	

<i>Boats</i>	<i>bid</i>	<i>bname</i>	<i>color</i>	<i>BadSids</i>	<i>sid</i>
	<u>B</u>			I.	<u>Id</u>

Given the view BadSids, it is a simple matter to find sailors whose *sids* are not in this view.

# QBE (Query-By-Example)

(a)

Essn	Pno	Hours
P._ES	1	
P._ES	2	

(b)

Essn	Pno	Hours
P._EX	1	
P._EY	2	

CONDITIONS

_EX = _EY
-----------

**Figure C.4**

Specifying EMPLOYEES who work on both projects. (a) Incorrect specification of an AND condition. (b) Correct specification.

Now consider query Q0C: *List the social security numbers of employees who work on both project 1 and project 2*; this cannot be specified as in Figure C.4(a), which lists those who work on *either* project 1 or project 2. The example variable \_ES will bind itself to Essn values in  $\langle -, 1, - \rangle$  tuples *as well as* to those in  $\langle -, 2, - \rangle$  tuples. Figure C.4(b) shows how to specify Q0C correctly, where the condition ( $\_EX = \_EY$ ) in the box makes the \_EX and \_EY variables bind only to identical Essn values.

# QBE (Query-By-Example)

**EMPLOYEE**

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
P.		P.	_SX						

**DEPENDENT**

⌊

Essn	Dependent_name	Sex	Bdate	Relationship
_SX				

**Figure C.7**  
Illustrating negation by the query Q6.

**Query 6.** Retrieve the names of employees who have no dependents.

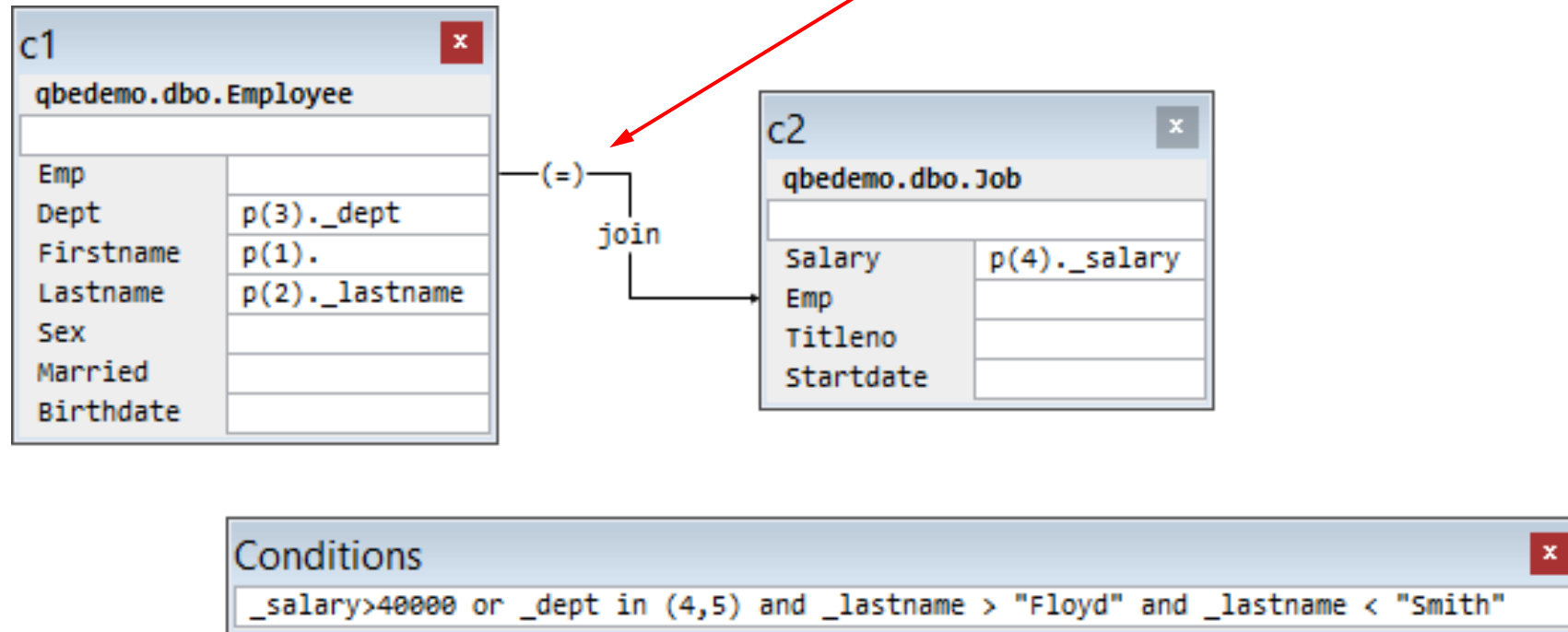
**Q6:**     **SELECT**     Fname, Lname  
          **FROM**     EMPLOYEE  
          **WHERE**    **NOT EXISTS** ( **SELECT**     \*  
                                  **FROM**     DEPENDENT  
                                  **WHERE**    Ssn = Essn );

**Q6:** {*q, s* | (∃*t*)(EMPLOYEE(*qrstuvxyz*) **AND**  
          (**NOT**(∃*l*)(DEPENDENT(*lmnop*) **AND** *t=l*)))}

# QBE variant: Catalyst One Sysdeco

Q: "List employees who earn more than 40,000. In the same list, we want to include employees who work in departments 4 and 5 and have a surname in the interval between Floyd and Smith, irrespective of how much they earn."

Using a tool called "visual query editor" which combines ideas from QBE with a visual join syntax.



# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# QBD (1990)

## (Query By Diagram)

Sources used:

- Angelaccio, Catarci, Santucci. QBD\*: a graphical query language with recursion. IEEE TSE 1990. <https://doi.org/10.1109/32.60295>
- Angelaccio, Catarci, Santucci. Query by Diagram: a fully visual query system. JVLC 1990. [https://doi.org/10.1016/S1045-926X\(05\)80009-6](https://doi.org/10.1016/S1045-926X(05)80009-6)
- Santucci, Sottile. Query by Diagram: a Visual Environment for Querying Databases. SPE 1993. <https://doi.org/10.1002/spe.4380230307>
- Catarci, Santucci. Query by diagram : a graphical environment for querying databases. SIGMOD demo 1994. <https://doi.org/10.1145/191839.191976>
- Catarci, Costabile, Levialdi, Batini. Visual query systems for databases: a survey. JVLC 1997. <https://doi.org/10.1006/jvlc.1997.0037>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>



# QBD (Query-By-Diagram)

- Based on an ER model of the data, thus separates entities and relationships
- User navigates the ERD and creates "bridges" b/w entities when specifying the query
- Describes a mapping of the RA (relational algebra) operators to labels on edges
- Filters and join conditions are specified in separate windows (like in visual query builders)
- Our focus is here just the visual metaphors as possibly applied to relations directly

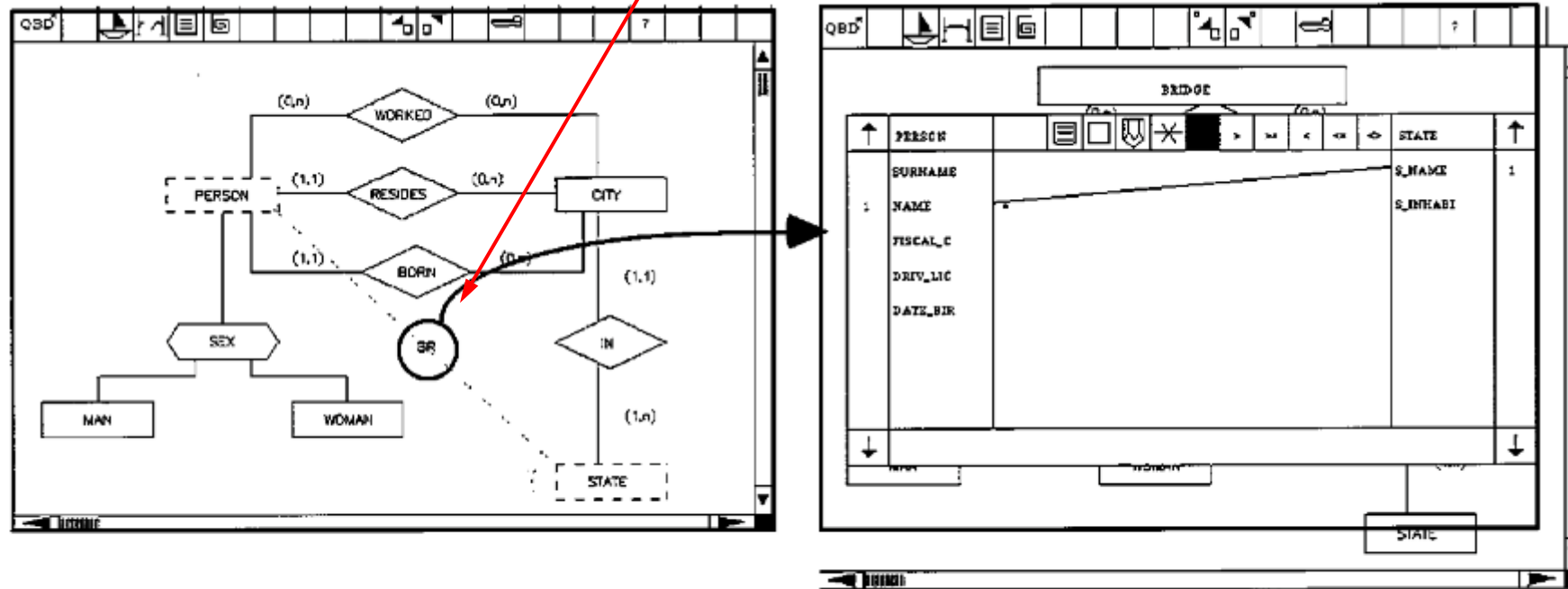


Figure source: "Catarci, Costabile, Levialdi, Batini. Visual query systems for databases: a survey. JVL 1997. <https://doi.org/10.1006/jvlc.1997.0037>"

citing "Angelaccio, Catarci, Santucci. Query by Diagram\*: a fully visual query system. JVL 1990. [https://doi.org/10.1016/S1045-926X\(05\)80009-6](https://doi.org/10.1016/S1045-926X(05)80009-6)"

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Query 1

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname
from Boat
where color = 'red'
or color = 'blue'
```

Schema

Boat
<u>bid</u>
bname
color
pdate

Boat

Selection conditions are specified in  
separate context windows (like in  
visual active query builders)

Boat	<input checked="" type="checkbox"/> = <input type="checkbox"/> > <input type="checkbox"/> >= <input type="checkbox"/> < <input type="checkbox"/> <= <input type="checkbox"/> <>	
bid bname color pdate		red

## Relational Algebra

$\sigma_{\text{color}='red' \vee \text{color}='blue'} B$

# QBD (Query-By-Diagram)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate



Returned attributes and selections are displayed in separate context menus (not the main panel)

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie R \bowtie \sigma_{\text{color}='red'} B)$$

# QBD (Query-By-Diagram)

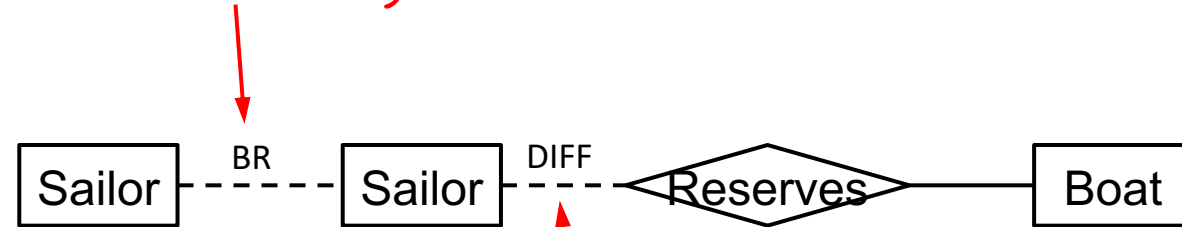
Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

## Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate

A "bridge" connects entities that are not connected in the original ERD



Set difference as algebraic operator is shown by a labeled edge

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - (\pi_{\text{sid}} (R \bowtie \sigma_{\text{color}='red'} B))))$$

# QBD (Query-By-Diagram)

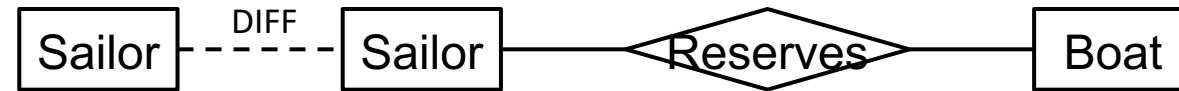
Q3: "Find sailors who reserved only red boats."

"except" assumes set semantics

```
select sname
from Sailor
except
select sname
from Sailor S, Reserves R,
      Boat B
where S.sid=R.sid
and R.bid=B.bid
and color <> 'red'
```

Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate



Appropriate selections of attributes and filters for boats that are not red are done in context menus

This is a logically equivalent way of writing the same query

## Relational Algebra

$$\pi_{\text{sname}} S - (\pi_{\text{sname}} (S \bowtie R \bowtie \sigma_{\text{color} \neq \text{'red'}} B))$$

Figure drawn based on personal communication with the authors

Database to run SQL queries is available as schema 341 at <https://github.com/northeastern-datalab/cs3200-activities/tree/master/sql/>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# QBD (Query-By-Diagram)

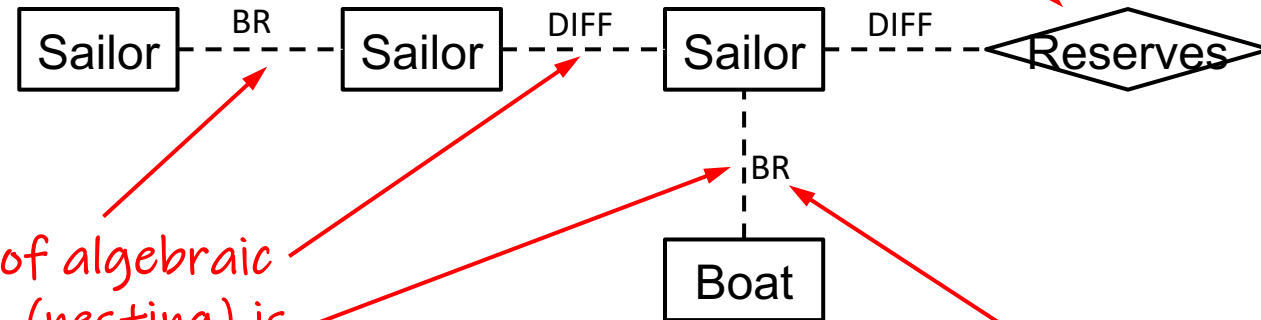
Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

## Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate

QBD is originally an ER model, thus  
"Reserves" would be a relationship.  
For RA it needs to be treated as table



Sequence of algebraic  
operators (nesting) is  
ambiguous

The Cross Product is treated as join thus  
connects two entities via a "bridge"

## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - \pi_{\text{sid}}((\pi_{\text{sid}} S \times \pi_{\text{bid}} \sigma_{\text{color}='red'} B) - \pi_{\text{sid,bid}} R)))$$

# QBD (Query-By-Diagram)

Q4: "Find sailors who reserved all red boats."

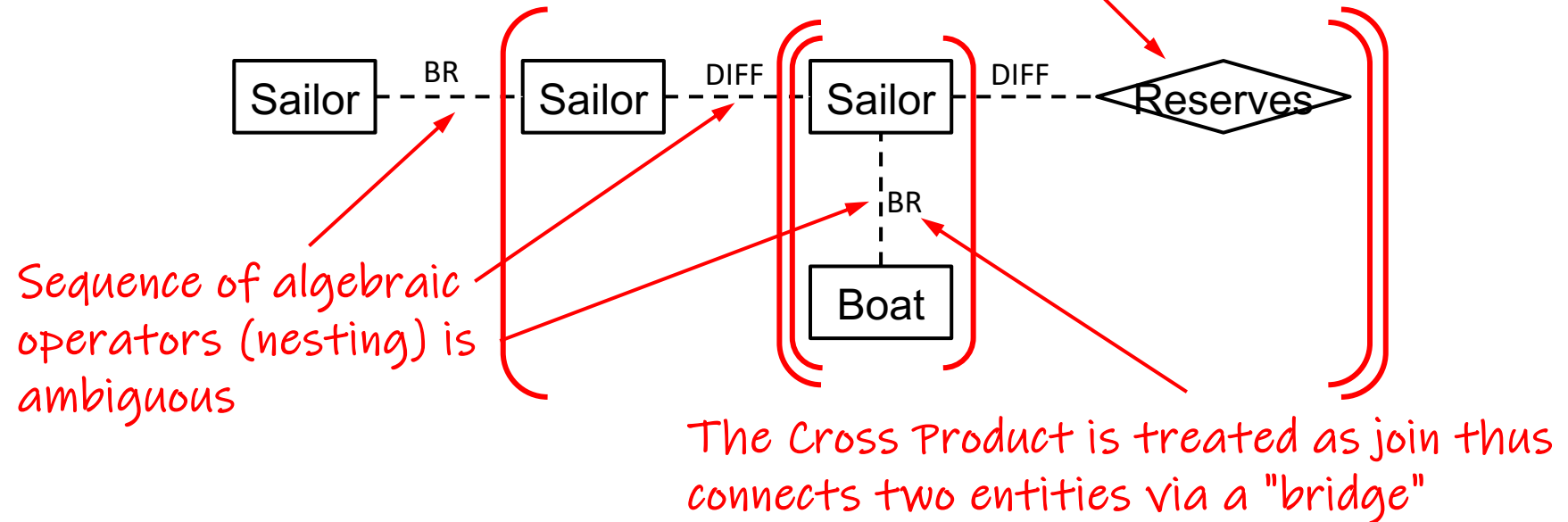
```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

## Schema

Sailor	Reserves	Boat
<u>sid</u>	<u>sid</u>	<u>bid</u>
sname	<u>bid</u>	bname
rating	<u>day</u>	color
bdate		pdate

QBD is originally an ER model, thus "Reserves" would be a relationship. For RA it needs to be treated as table

?



## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - \pi_{\text{sid}}((\pi_{\text{sid}} S \times \pi_{\text{bid}} \sigma_{\text{color}='red'} B) - \pi_{\text{sid,bid}} R)))$$

# QBD (Query-By-Diagram)

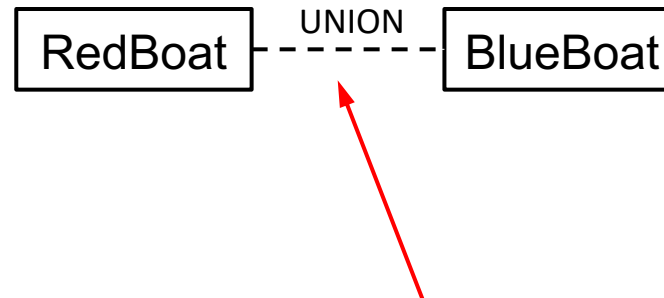
Q5: "Find boats  
that are red or blue."

```
select bid, bname  
from RedBoat R  
union  
select bid, bname  
from BlueBoat B
```

Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate



Union as algebraic operator is shown by a label on a "bridge" that connects entities that are not connected in the original ERD

## Relational Algebra

$\pi_{bid, bname}(\text{RedBoat} \cup \text{BlueBoat})$



# QBD (1990) (Query By Diagram) Backup

# QBD (Query-By-Diagram)

At this point the query session can begin. To retrieve the desired pilots the user selects in sequence the entities PILOT and PASSENG(er), creating an effective bridge with the condition `PILOT.surname=PASSENG(er).surname`. The window mechanism used to put conditions on attributes is shown in Figure 8 (the image comes from a previous version of QBD\*: the window mechanism in the Windows environment is under development).

The new relationship, represented by a dotted line and the letters BR, is shown in Figure 9.

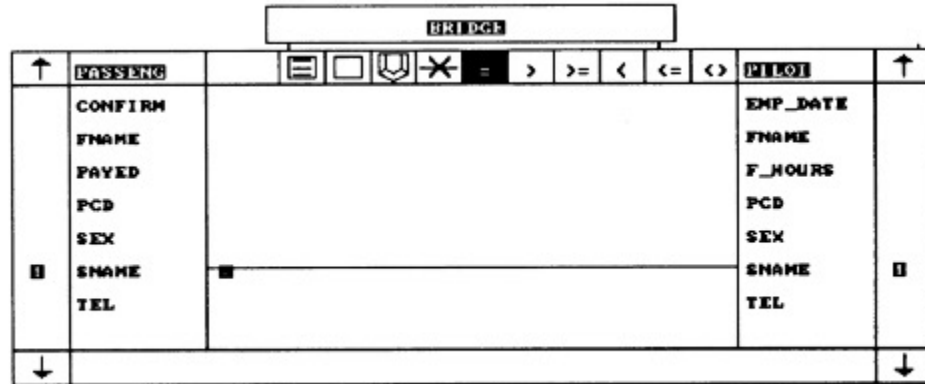


Figure 8. The windows mechanism for the 'bridge'

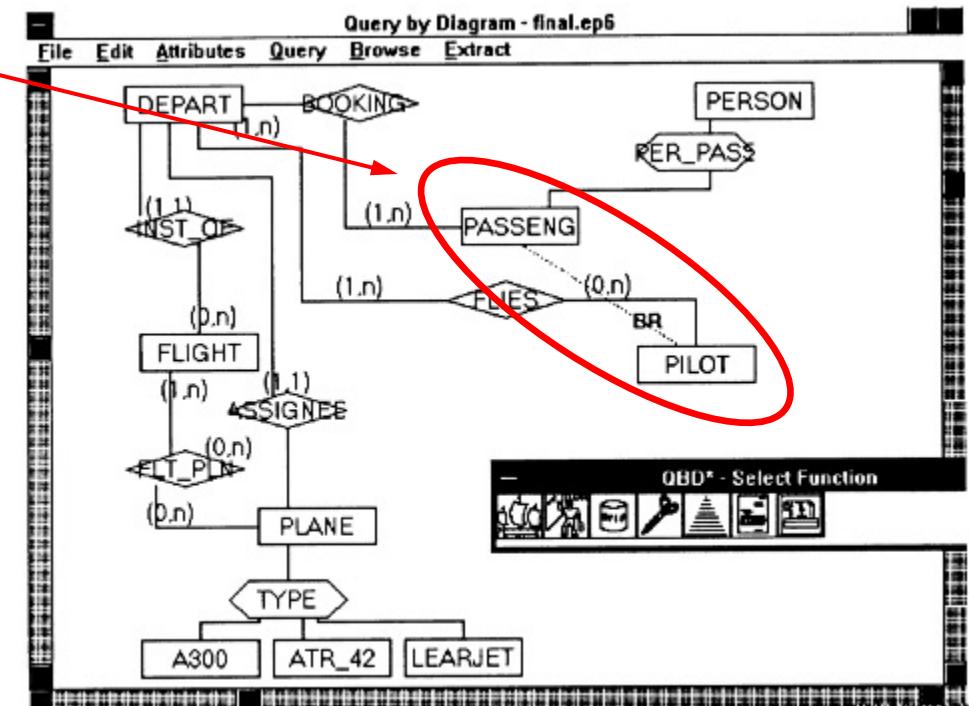


Figure 9. The new relationship

# QBD (Query-By-Diagram)

Relationship model. For example, in QBD\* a query primitive is available that allows joining entities not explicitly linked in the schema [4].

These "bridges" are also necessary for cross joins

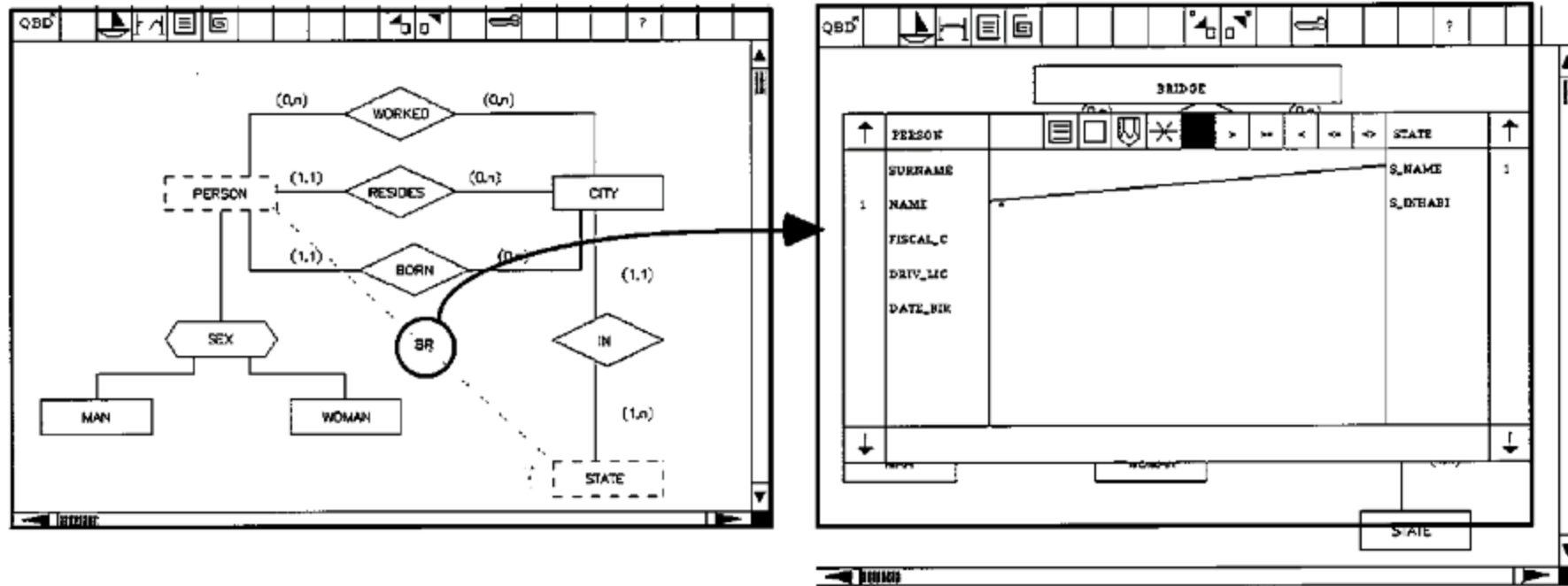


Figure 11. Unconnected path in QBD\* (from Angelaccio *et al.* [4])

Source: "Catarcì, Costabile, Levialdi, Batini. Visual query systems for databases: a survey. JVL 1997. <https://doi.org/10.1006/jvlc.1997.0037>"

citing "Angelaccio, Catarcì, Santucci. Query by Diagram\*: a fully visual query system. JVL 1990. [https://doi.org/10.1016/S1045-926X\(05\)80009-6](https://doi.org/10.1016/S1045-926X(05)80009-6)"

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# TableTalk (1991)

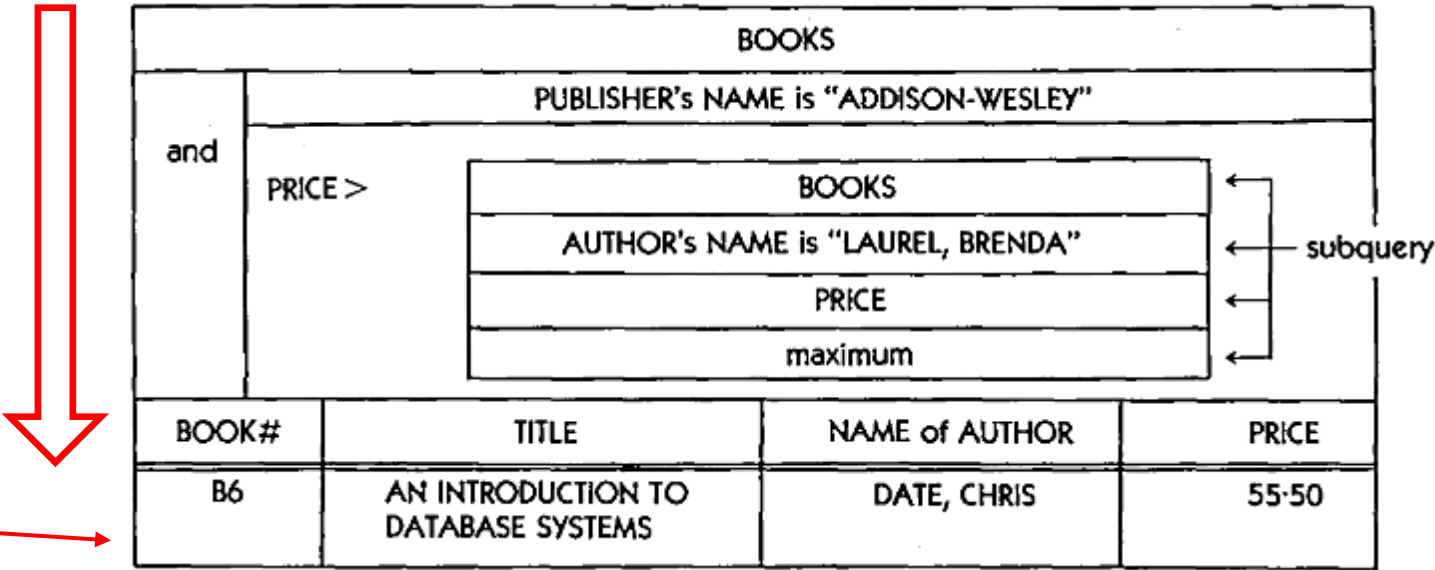
Sources used:

- Epstein. The TableTalk query language. JVLC, 1991. [https://doi.org/10.1016/S1045-926X\(05\)80026-6](https://doi.org/10.1016/S1045-926X(05)80026-6)
- Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Tabletalk

- A flowchart inspired visual representation based on blocks

The program is "run" top-down, and displays results of the query at the bottom



# Tabletalk

Q1b: "Find boats  
that are not red."

```
select distinct bname  
from Boat  
where color = 'red'
```

row #:

1  
2  
3

Boat
color = "red"
bname

class row (= table containing  
objects of interest)

predicate row: specifies a  
logical condition

scalar transformer

sequence processing language with  
rows and tiles (is read top down)

# Tabletalk

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname, color
from Boat
where color = 'red'
or color = 'blue'
```

Boat	
or	color = "red"
	color = "blue"
bname	color
Interlake	red
Interlake	blue
Marine	red

predicate row containing  
multiple tiles

multiple tiles for output

query answers



# Tabletalk

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Boat
color = "red"
Reserves
rid
Sailor
sname

"object transformer"  
(assumes FK-PK constraints)  
"transforms the primordial  
objects of the main processing  
sequence into new primordial  
objects whose class is the  
codomain class of the object  
attribute."

# Tabletalk

Q2a: "Find sailors and red boats they reserved."

```
select distinct S.sname, B.bname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

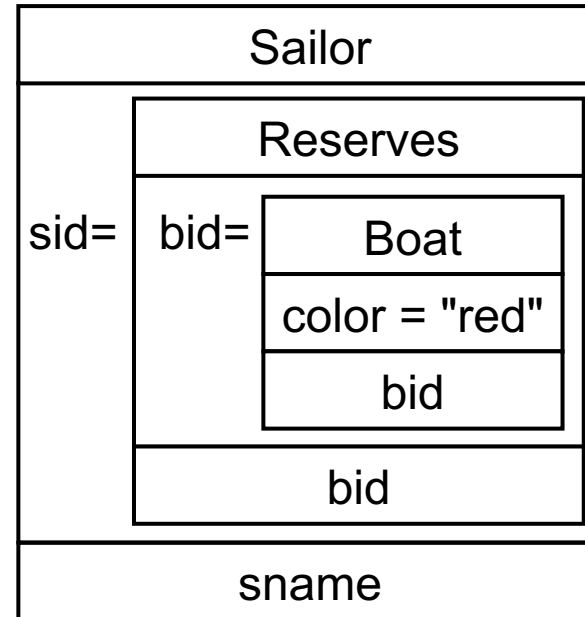
Boat	
color = "red"	
bname	Reserves
	rid
	Sailor
	sname

apply "product" to not "forget"

# Tabletalk

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
where exists
  (select *
   from Boat B
   where color = 'red'
   and exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```



*Nested queries are evaluated inside out*

# Tabletalk

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

To express nested correlated queries, we first have to unnest and then follow a dataflow strategy.

?

This requires a cross-product and difference, similar to Datalog and QBE.

But paper does not discuss a difference or other non-monotone operator...

Nor does it discuss union

?

# TableTalk (1991)

## Backup

# Tabletalk (1991)



EXAMPLE 1. Give the titles, author names and author photos for all books whose price is over \$40.00.

row #:

1




2

3

BOOKS		
PRICE > 40.0		
TITLE	AUTHOR	
	NAME	PHOTO
AN INTRODUCTION TO DATABASE SYSTEMS	DATE, CHRIS	
THE ART OF HUMAN- COMPUTER INTERFACE DESIGN	LAUREL, BRENDA	

# Tabletalk (1991)

EXAMPLE 2. Give the book numbers, titles, order numbers, and customers for those orders for books published by Addison-Wesley that are out of stock.

BOOKS			
and	IN_STOCK = 0		
	NAME of PUBLISHER = "ADDISON-WESLEY"		
BOOK#	TITLE	ORDERS	
		ORDER#	CUSTOMER
B5	A GUIDE TO DB2	ORD5	 C5
		ORD6	 C2
B6	AN INTRODUCTION TO DATABASE SYSTEMS	ORD6	 C5

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)



# "OO-VQL" (1993)

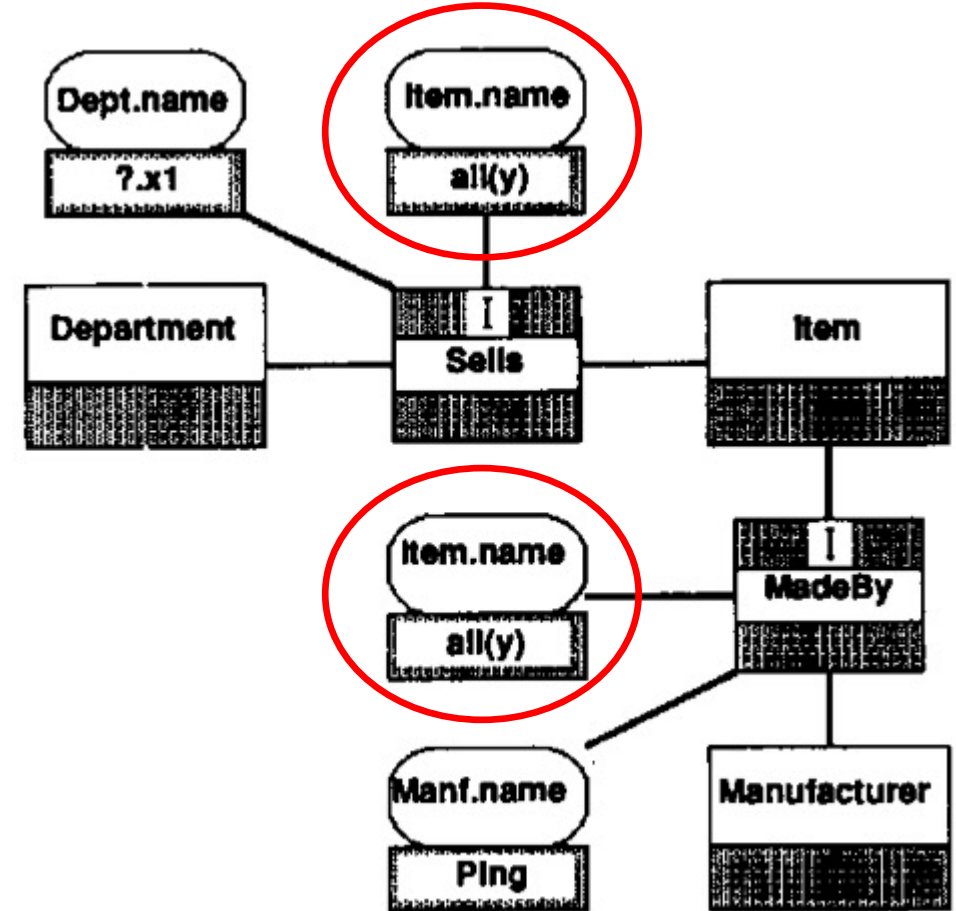
## "Object-Oriented VQL"

Sources used:

- Mohan, Kashyap. A visual query language for graphical interaction with schema-intensive databases. TKDE 1993. <https://doi.org/10.1109/69.243513>
- Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# OO-VQL (Object-oriented VQL)

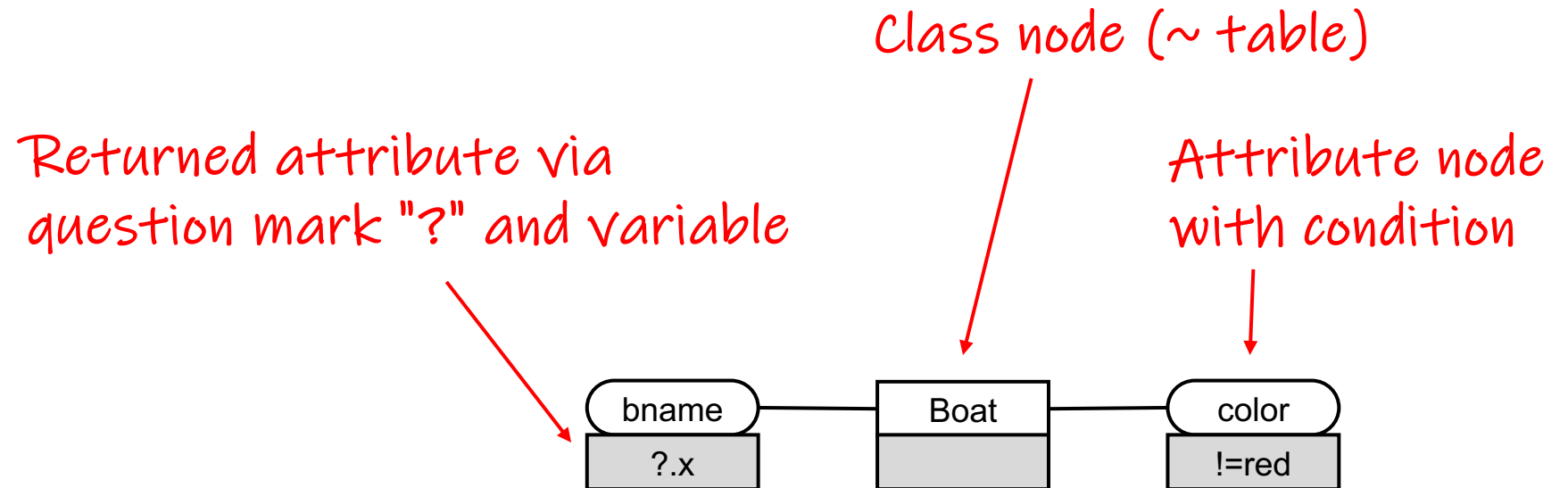
- Developed for an object-oriented data model, thus separates **entities and relationships**
- We again focus here on the visual metaphors as possibly applied to relations directly
- Notice that "VQL" is ambiguous: The term has been used multiple times in the literature for proposed visual languages, even for the term Visual Query Language. So we use here OO-VQL for "Object-Oriented VQL"



# OO-VQL (Object-oriented VQL)

Q1b: "Find boats  
that are not red."

```
select distinct bname  
from Boat  
where color != 'red'
```



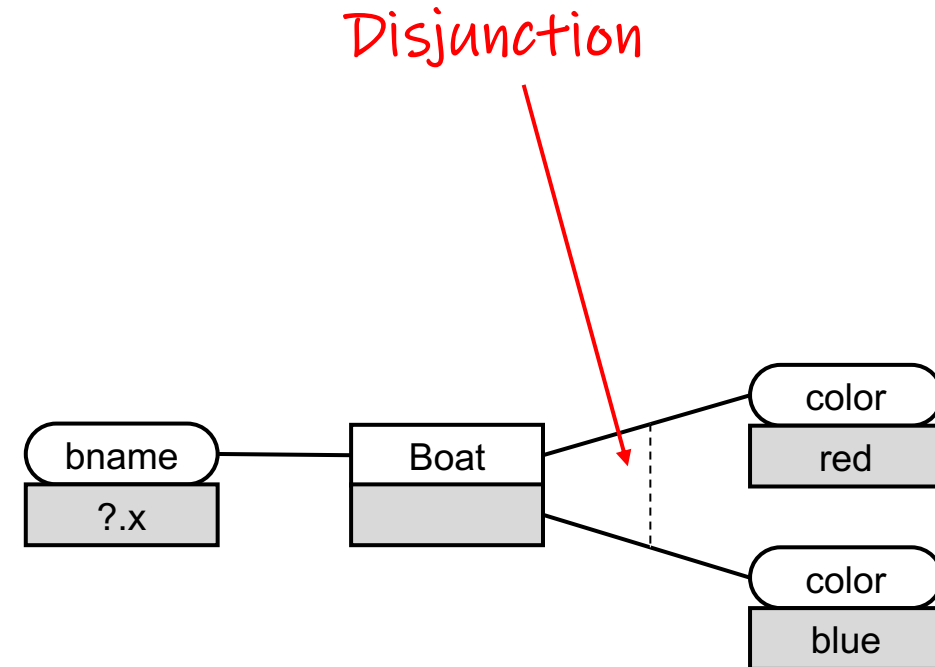
## DRC (Domain Relational Calculus)

$\{(x) \mid \text{Sailor}(\_, x, y, \_) \wedge (y \neq \text{'red'})\}$

# OO-VQL (Object-oriented VQL)

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```



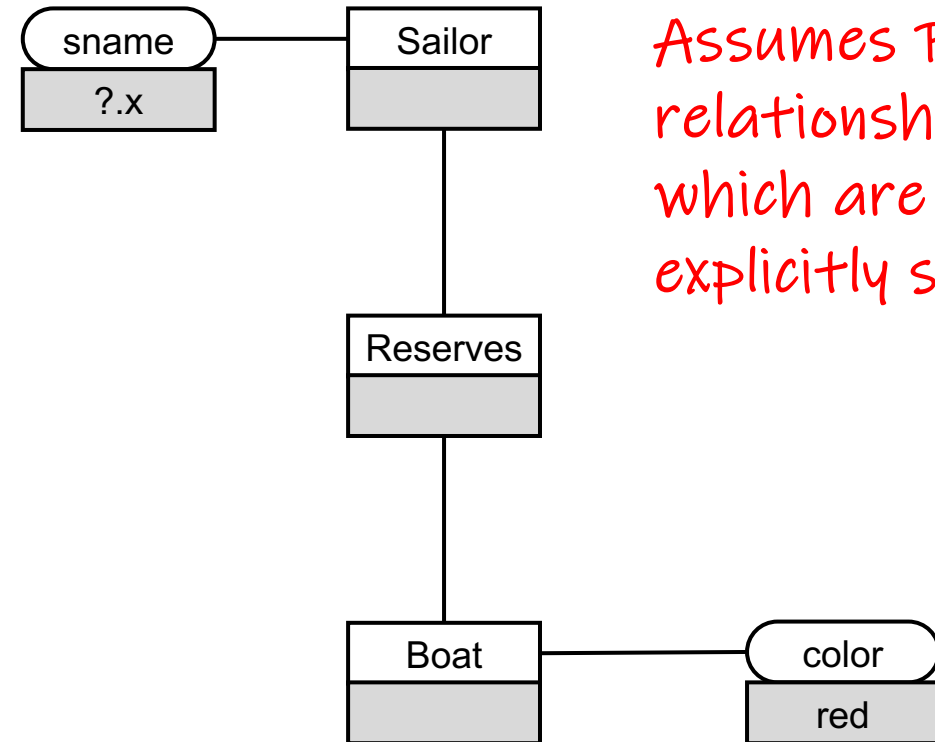
## DRC (Domain Relational Calculus)

$$\{(x) \mid \text{Sailor}(\_, x, y, \_) \wedge (y = \text{'red'} \vee y = \text{'red'})\}$$

# OO-VQL (Object-oriented VQL)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



Assumes PK-FK relationships, which are not explicitly shown

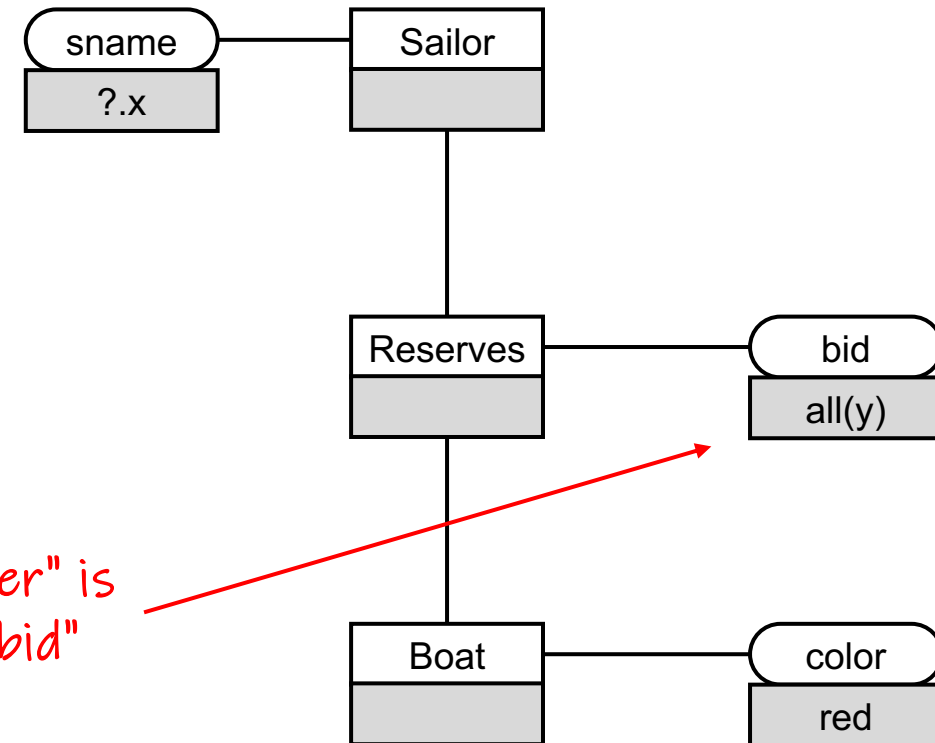
## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v[\text{Sailor}(v, x, \_, \_) \wedge \exists y[\text{Reserves}(v, y, \_) \wedge \text{Boat}(y, \_, 'red', \_)]]\}$$

# OO-VQL (Object-oriented VQL)

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v[\text{Sailor}(v, x, \_, \_) \wedge$$
$$(\forall y[\text{Reserves}(v, y, \_) \rightarrow$$
$$(\text{Boat}(y, \_, 'red', \_))]]\}$$

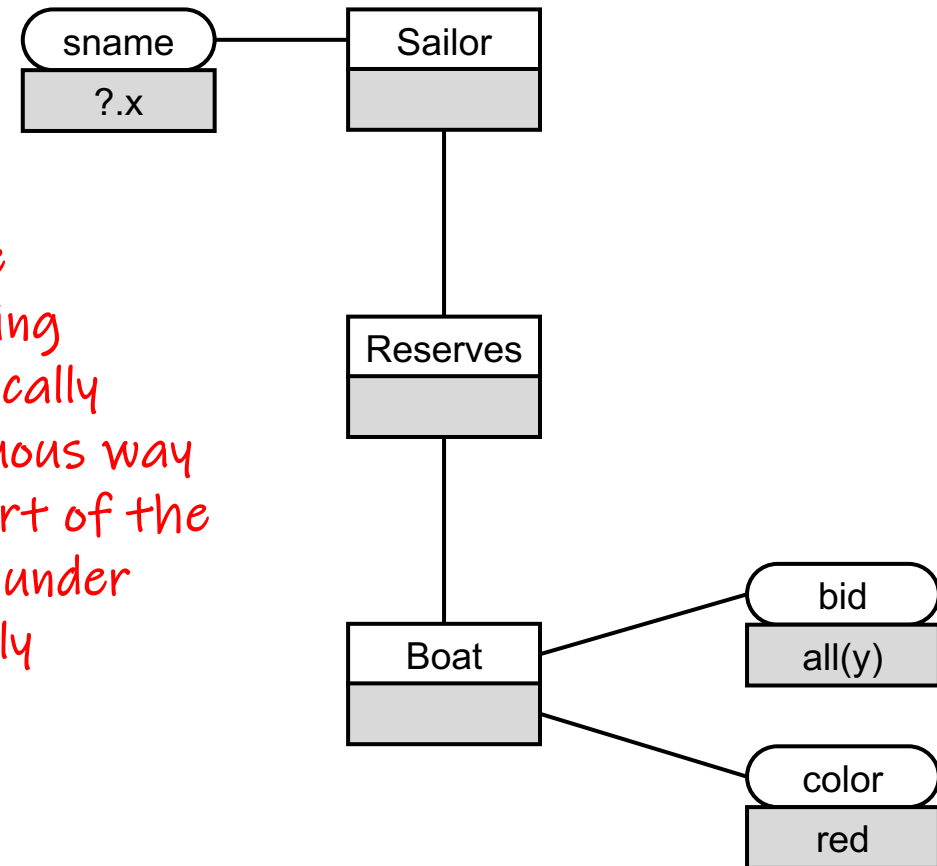
# OO-VQL (Object-oriented VQL)



Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

Visualization can become ambiguous because scoping cannot always be graphically represented in unambiguous way (e.g. is Reserves still part of the universal quantification under Boat, or is it existentially quantified under Boat?)



## DRC (Domain Relational Calculus)

$$\{(x) \mid \exists v[\text{Sailor}(v, x, \_, \_) \wedge (\forall y[\text{Boat}(y, \_, 'red', \_) \rightarrow (\text{Reserves}(v, y, \_))]]]\}$$

No way to express union!

# OO-VQL (Object-oriented VQL)

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

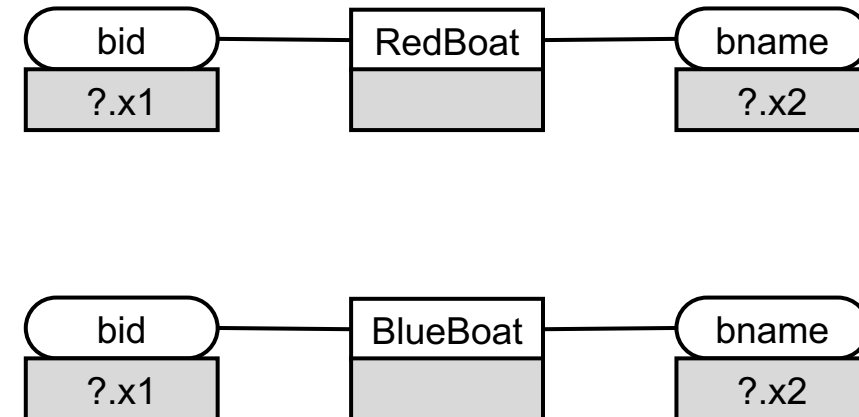
Paper does not discuss any way to handle union.  
But it is easy to imagine a Datalog-style "repeated derivation" presentation (?)

?

Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate



## Datalog

$Q(x, y) :- \text{RedBoat}(x, y, \_)$

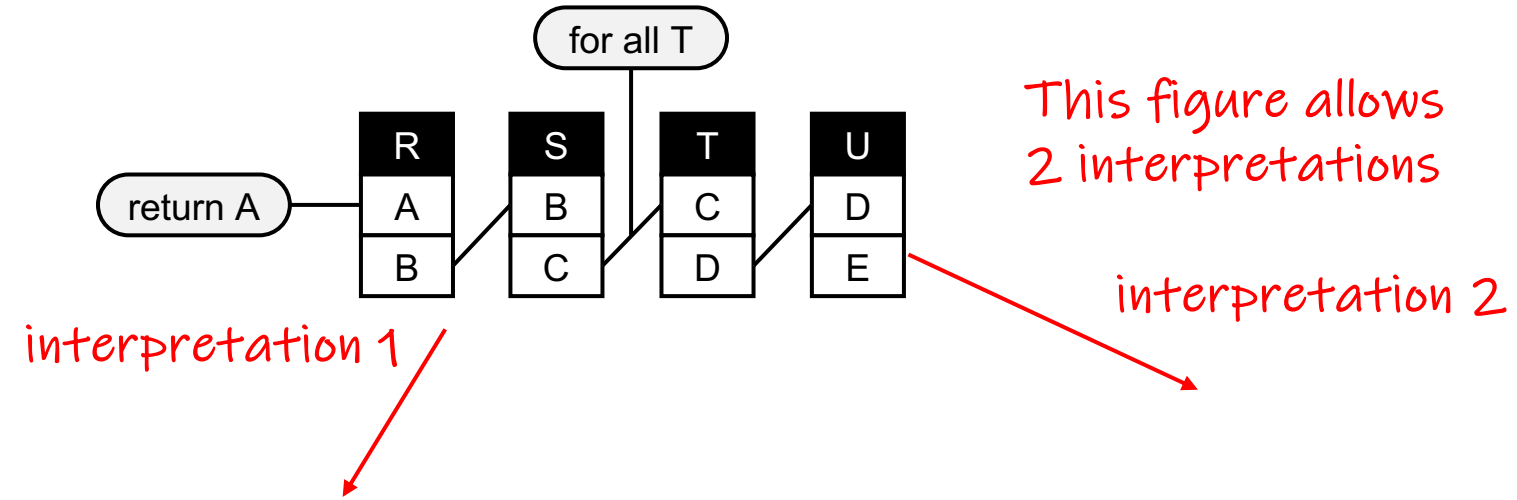
$Q(x, y) :- \text{BlueBoat}(x, y, \_)$

## DRC (Domain Relational Calculus)

$\{(x, y) \mid \exists z [\text{RedBoat}(x, y, z) \vee \text{BlueBoat}(x, y, z)]\}$

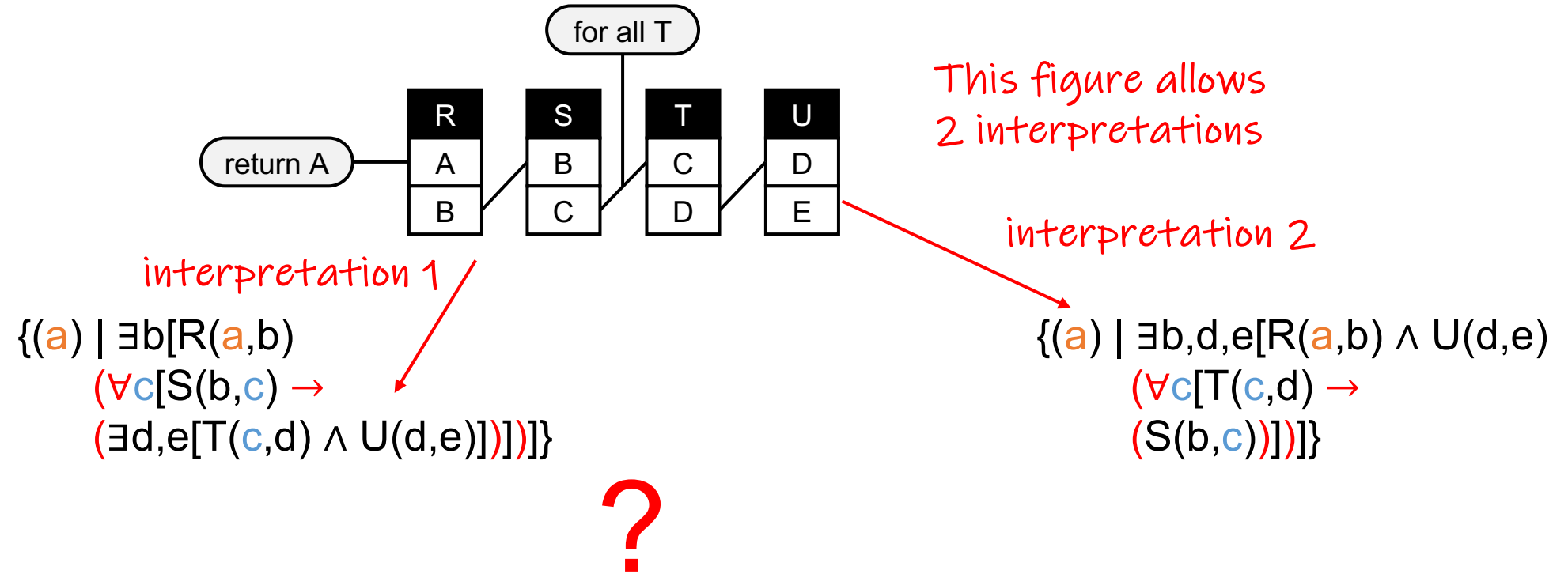


# When the quantifier scope becomes ambiguous

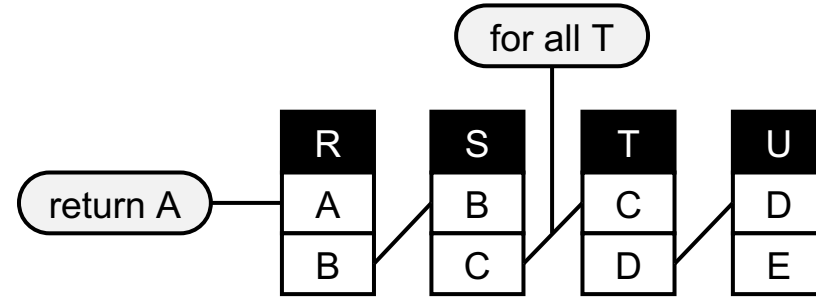


?

# When the quantifier scope becomes ambiguous



# When the quantifier scope becomes ambiguous



This figure allows  
2 interpretations

interpretation 1

```
select distinct R.A
from R
where not exists
(select *
from S
where R.B=S.B
and not exists
(select *
from T,U
where S.C=T.C
and T.D=U.D))
```

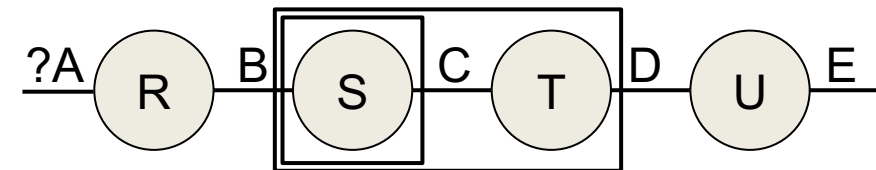
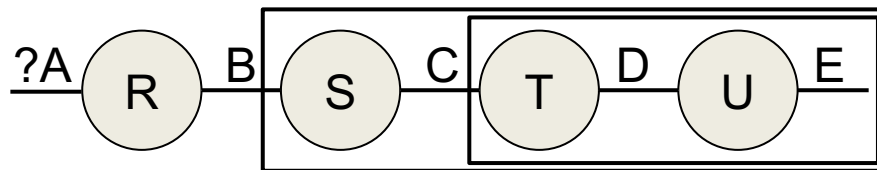
$$\{(a) \mid \exists b[R(a,b) \wedge (\forall c[S(b,c) \rightarrow (\exists d,e[T(c,d) \wedge U(d,e)])])]\}$$

$$\{q(A) \mid \exists r \in R[q.A=r.A \wedge \neg(\exists s \in S[r.B=s.B \wedge \neg(\exists t \in T, \exists u \in U[s.C=t.C \wedge t.D=u.D])])]\}$$

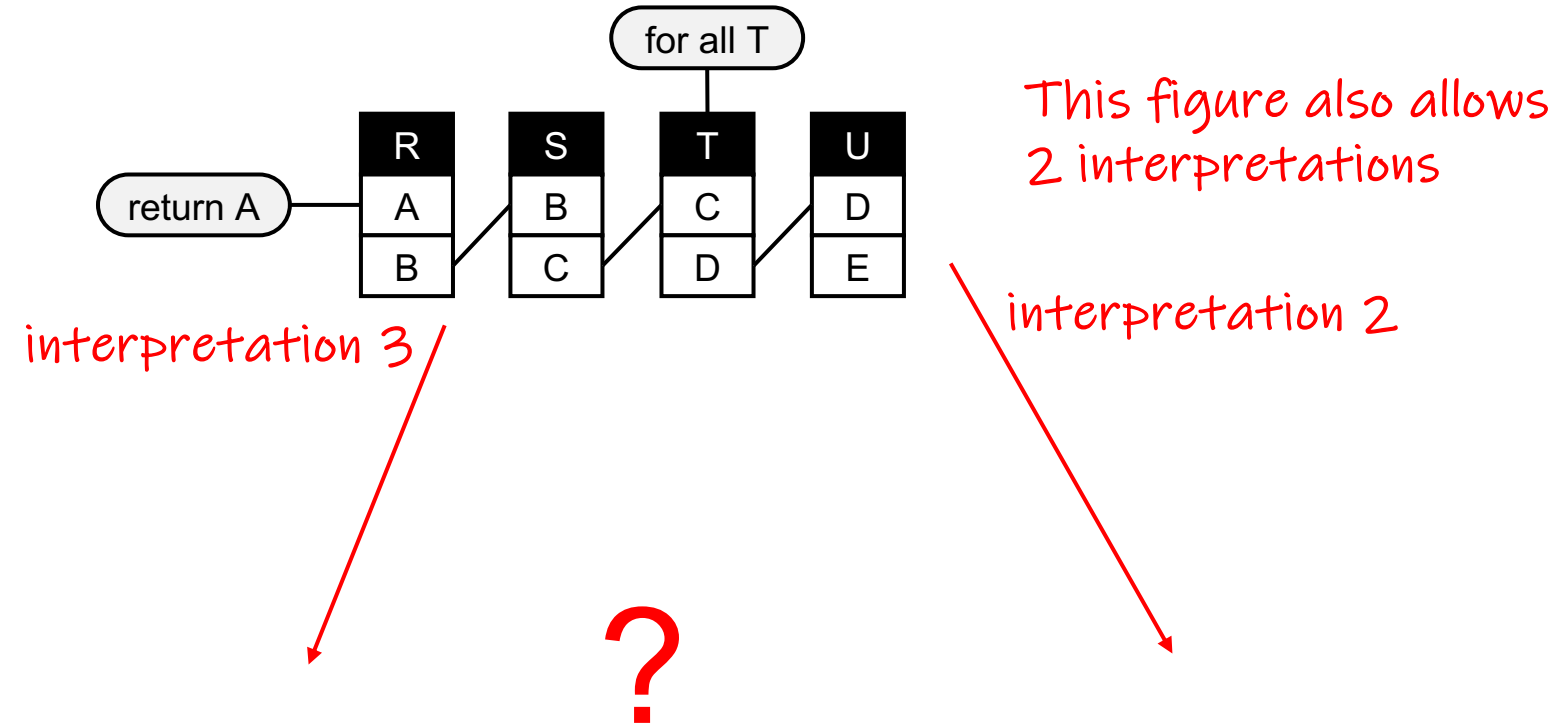
interpretation 2

```
select distinct R.A
from R, U
where not exists
(select *
from T
where T.D=U.D
and not exists
(select *
from S
where R.B=S.B
and S.C=T.C))
```

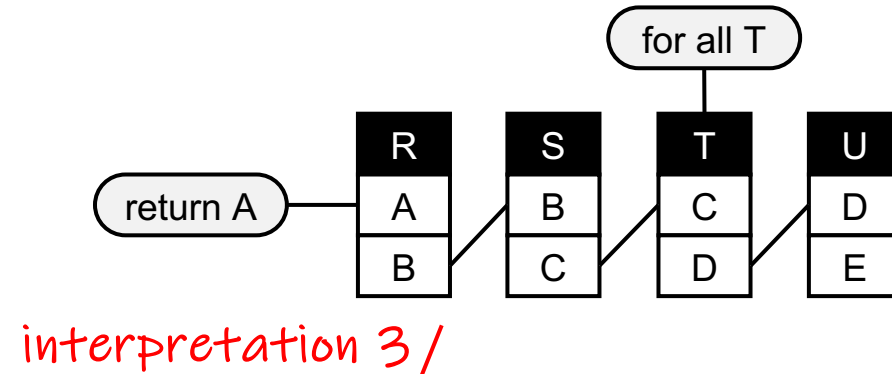
$$\{(a) \mid \exists b,d,e[R(a,b) \wedge U(d,e) \wedge (\forall c[T(c,d) \rightarrow (S(b,c))])]\}$$

$$\{q(A) \mid \exists r \in R, u \in U[q.A=r.A \wedge \neg(\exists t \in T[t.D=u.D \wedge \neg(\exists s \in S[r.B=s.B \wedge t.D=u.D])])]\}$$


# When the quantifier scope becomes ambiguous



# When the quantifier scope becomes ambiguous



This figure also allows  
2 interpretations

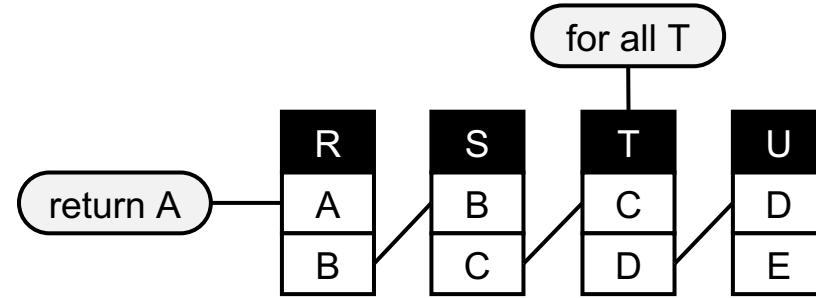
interpretation 3

$$\{q(A) \mid \exists r \in R, s \in S[q.A = r.A \wedge r.B = s.B \wedge \neg(\exists t \in T[s.C = t.C \wedge \neg(\exists u \in U[t.D = u.D])]]]\}$$

interpretation 2

$$\{q(A) \mid \exists r \in R, u \in U[q.A = r.A \wedge \neg(\exists t \in T[t.D = u.D \wedge \neg(\exists s \in S[r.B = s.B \wedge t.D = u.D])]]]\}$$

# When the quantifier scope becomes ambiguous



This figure also allows  
2 interpretations

interpretation 3

```
select distinct R.A
from R, S
where R.B=S.B
and not exists
(select *
 from T
 where S.C=T.C
 and not exists
 (select *
  from U
  where T.D=U.D))
```

$$\{(a) \mid \exists b, c [R(a, b) \wedge S(b, c) \wedge$$

$$(\forall d [T(c, d) \rightarrow$$

$$(\exists e [U(d, e)])]]\}$$

$$\{q(A) \mid \exists r \in R, s \in S [q.A = r.A$$

$$\wedge r.B = s.B \wedge$$

$$\neg(\exists t \in T [s.C = t.C \wedge$$

$$\neg(\exists u \in U [t.D = u.D])]]\}$$

interpretation 2

```
select distinct R.A
from R, U
where not exists
(select *
 from T
 where T.D=U.D
 and not exists
 (select *
  from S
  where R.B=S.B
  and S.C=T.C))
```

$$\{(a) \mid \exists b, d, e [R(a, b) \wedge U(d, e)$$

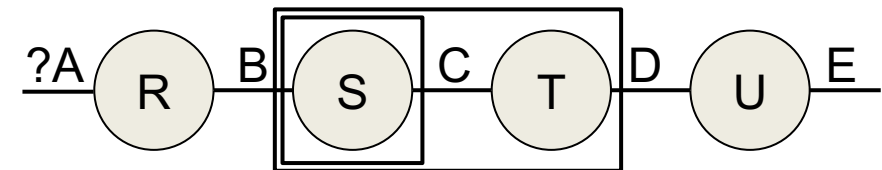
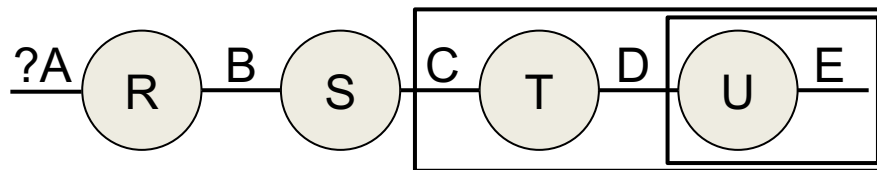
$$(\forall c [T(c, d) \rightarrow$$

$$(S(b, c))]]\}$$

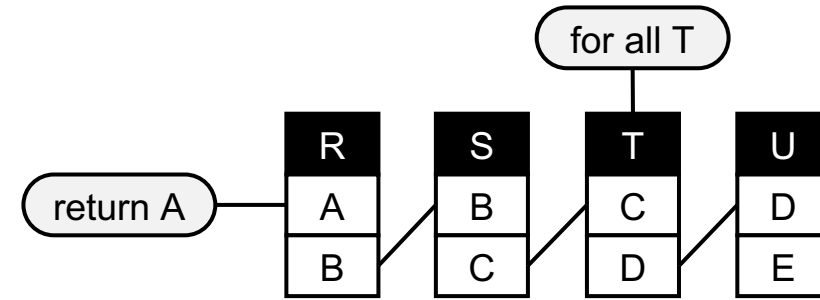
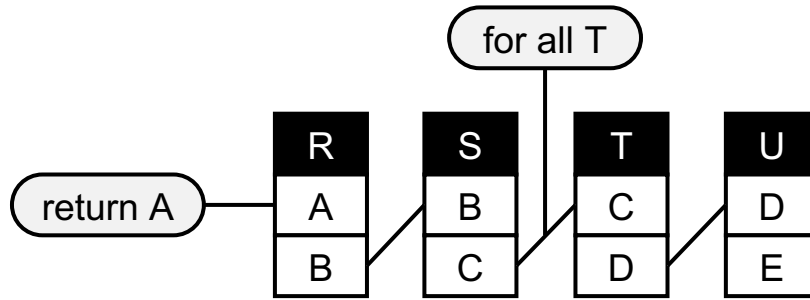
$$\{q(A) \mid \exists r \in R, u \in U [q.A = r.A$$

$$\neg(\exists t \in T [t.D = u.D \wedge$$

$$\neg(\exists s \in S [r.B = s.B$$

$$\wedge t.D = u.D])]]\}$$


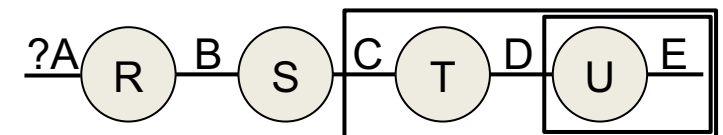
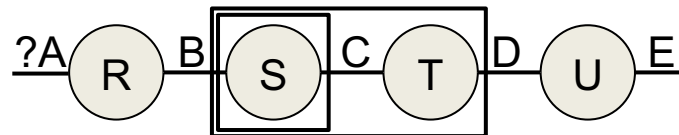
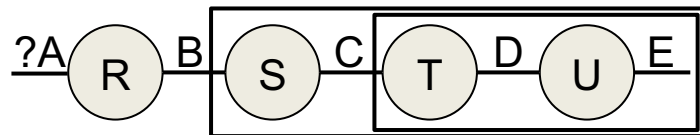
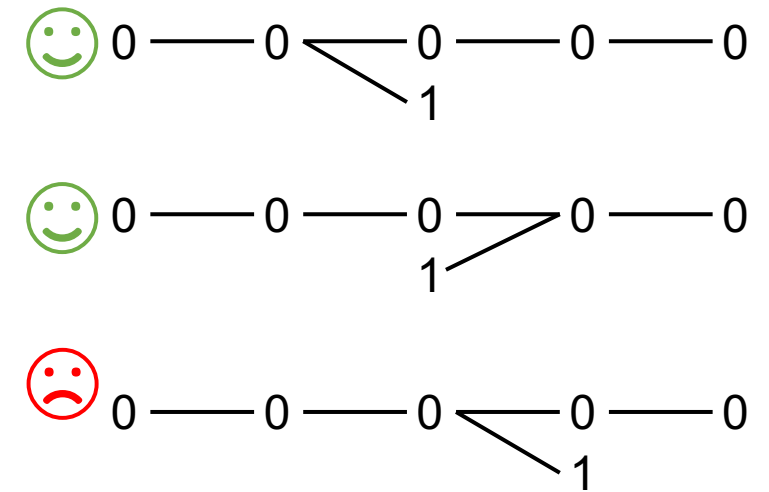
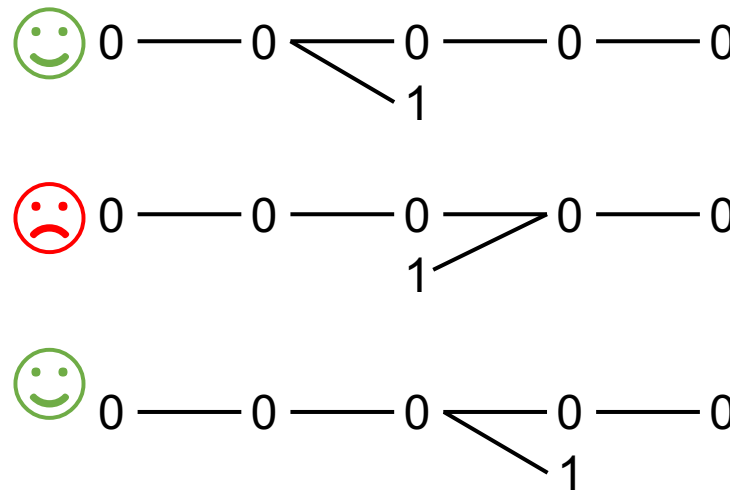
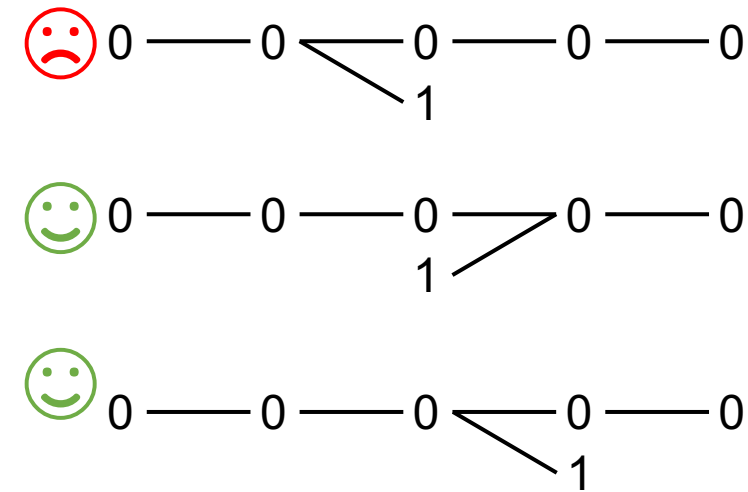
# When the quantifier scope becomes ambiguous



interpretation 1

interpretation 2

interpretation 3



# "Object-oriented VQL" (1993) Backup



# OO-VQL (Object-oriented VQL)

InletNeedle (idNumber, diameter, length, weight)

*Q2: Find the idNumbers of all the InletNeedles that have diameter greater than 0.25 and have length greater than 12.5.*

$x1: (\text{InletNeedle}, (x1, > 0.25, > 12.5, \_))$

*Q3: Find the idNumbers of all the InletNeedles that have either diameter greater than 0.25 or have length greater than 12.5.*

$x1: (\text{InletNeedle}, (x1, > 0.25, \_, \_))$

$\vee (\text{InletNeedle}, (x1, \_, 12.5, \_))$

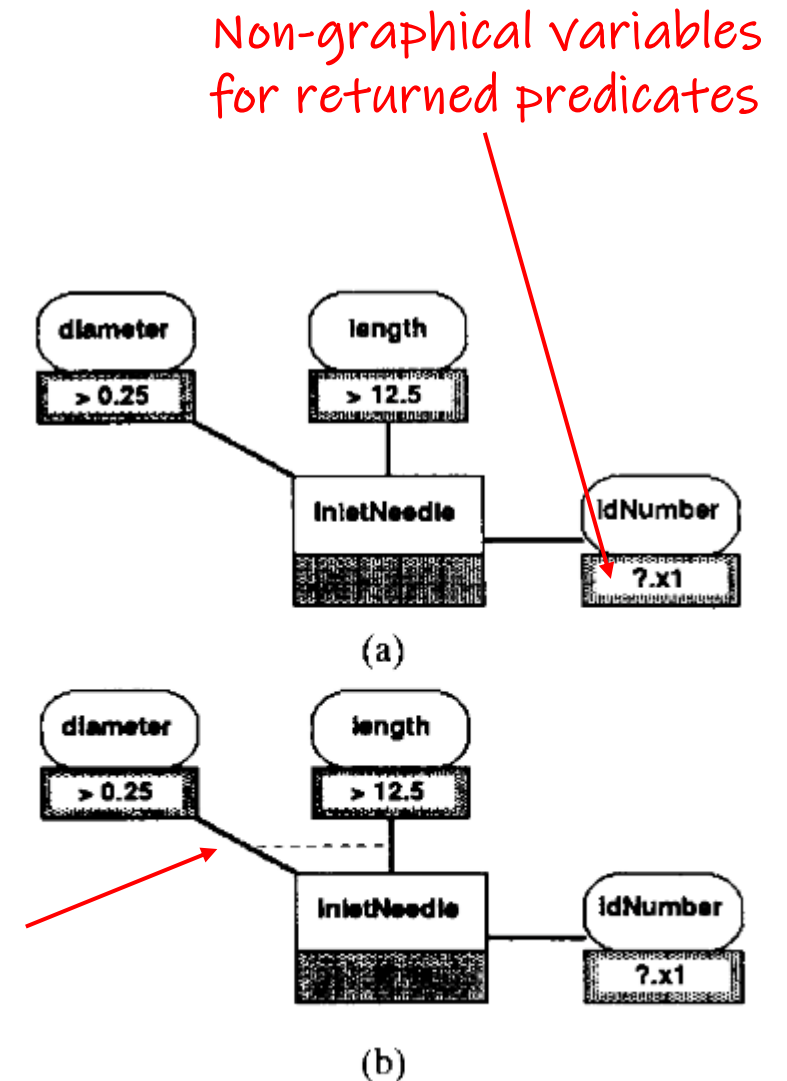
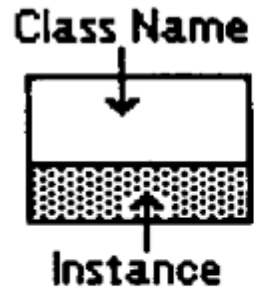
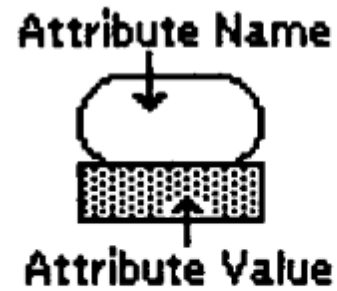


Fig. 6. Conjunctive and disjunctive queries.

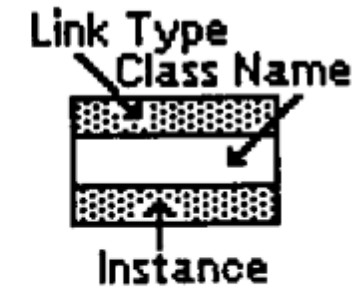
# OO-VQL (Object-oriented VQL)



(a)



(b)



(c)

Fig. 3. Visual query primitives.

# OO-VQL (Object-oriented VQL)

InletNeedle (idNumber, diameter, length, weight)  
Manufacturer (name, streetAddress, city)  
MadeBy [InletNeedle.idNumber, Manufacturer.name]

*Q4: Find the names of those manufacturers who manufacture InletNeedles with diameters greater than 0.25.*

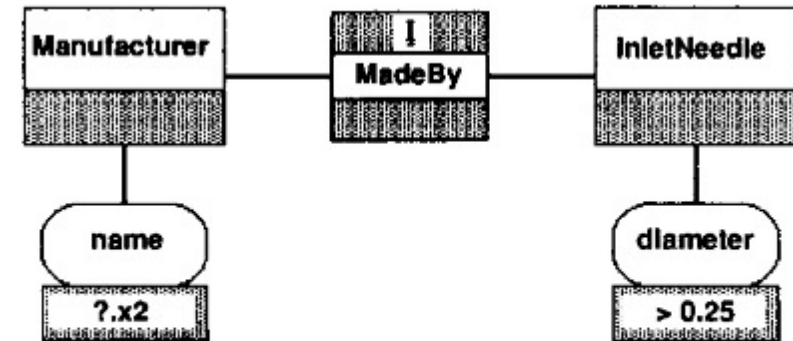


Fig. 7. An associative “Join” query using the “Interaction” link.

$x2: (I, \text{MadeBy}, (x1, x2))$   
 $[(\text{InletNeedle}, (x1, > 0.25, \_, \_)),$   
 $(\text{Manufacturer}, (x2, \_, \_))]$

# OO-VQL (Object-oriented VQL)

*Q5: Find the suppliers that supply an item sold by the TOY department.*

Department [name, size, location]  
Sells [Department.name, item.name]  
Item [name, color, size, weight]  
Supplies [Supplier.name, item.name]  
Supplier [name, street, city, zip]

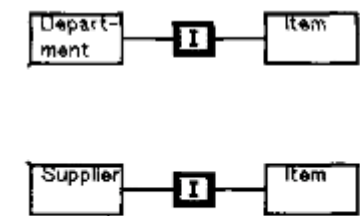


Fig. 8. Portions of two separate schemas.

Not clear why the same item object cannot be used for both relationships

$x2: (I, \text{Sells}, (\_, x1))[(\text{Department},$   
 $(\text{Toy}, \_, \_)), (\text{Item}, \_)]$   
 $\vee (I, \text{Supplies}, (\_, x1))[(\text{Supplier},$   
 $(x2, \_, \_, \_)), (\text{Item}, \_)]$

Disjunction here seems to be an error

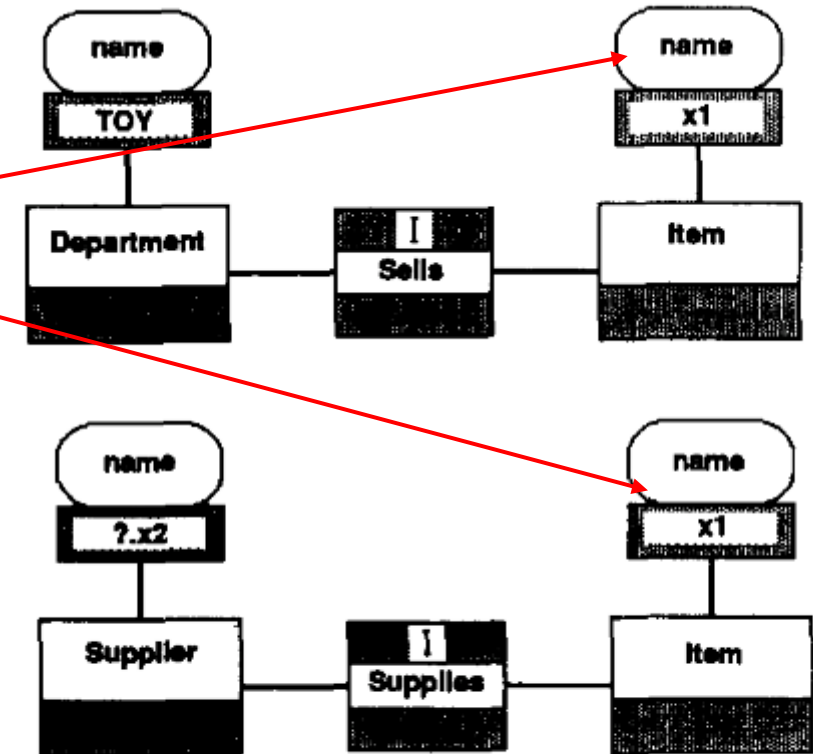


Fig. 9. A "Join" query that links unconnected schemas.

# OO-VQL (Object-oriented VQL)

*Q6: Find the names of those employees that earn more than their managers.*

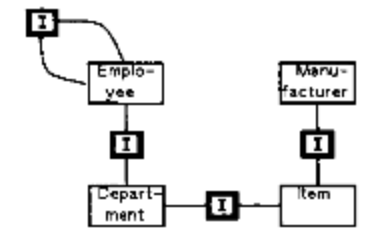


Fig. 10. A department store schema as represented in SSonet.

Non-graphical variables for built-in predicates

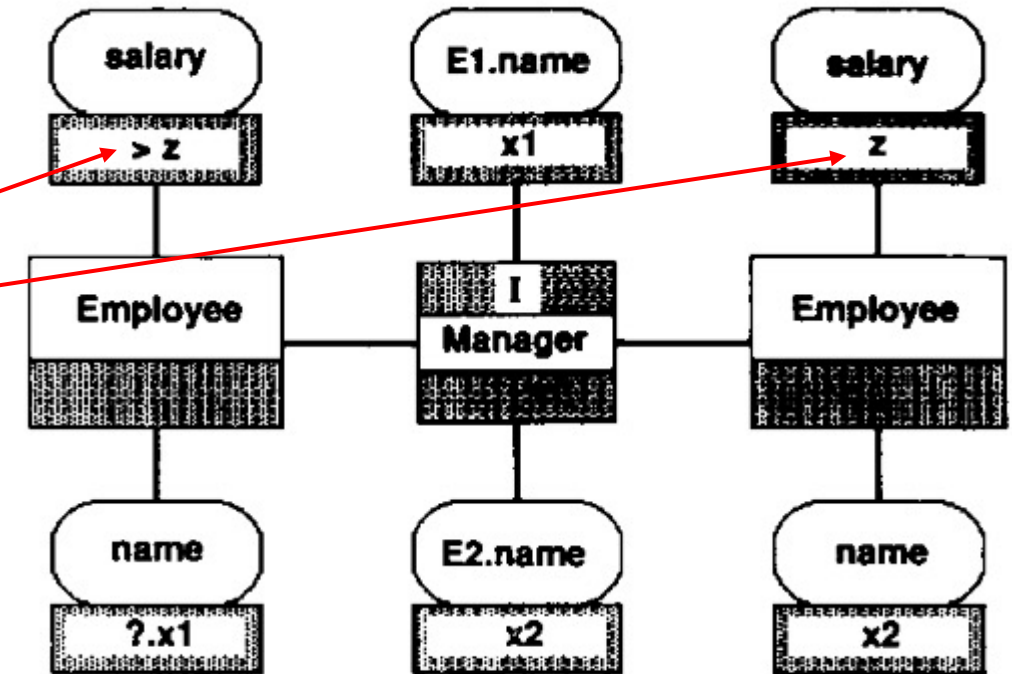


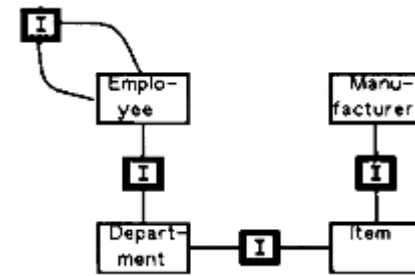
Fig. 11. A query involving a reflexive relationship.

$x1: (I, \text{ManagedBy}, (x1, x2))$

$[(\text{Employee}, (x1, > z, \_, \_)), (\text{Employee}, (x2, z, \_, \_))]$

# OO-VQL (Object-oriented VQL)

Department [name, size, location]  
Item [name, color, size, weight]  
Manufacturer [name, street, city, zip]  
**MadeBy(mname, ipname)**  
**Sells(dname, iname)**



*Q7: Find those departments that sell all the items that are manufactured by the manufacturer “Ping”*

This expression seems unsafe and would likely be written in today's notation as follows:

$$\{(x) \mid \text{Department}(x, \_, \_) \wedge (\forall v [\text{MadeBy}(v, \text{'Ping'}) \rightarrow (\text{Sells}(x, v))])\}$$

$x1: \forall y(I, \text{MadeBy}, (y, \text{Ping}))[(\text{Item}, \_), (\text{Manufacturer}, \_)] \rightarrow$   
 $(I, \text{Sells}, (x1, y))[(\text{Department}, \_), (\text{Item}, \_)]$

It is not evident how this diagram distinguishes between "that sells all items by Ping" vs. "s.t. that all sold items are by Ping"

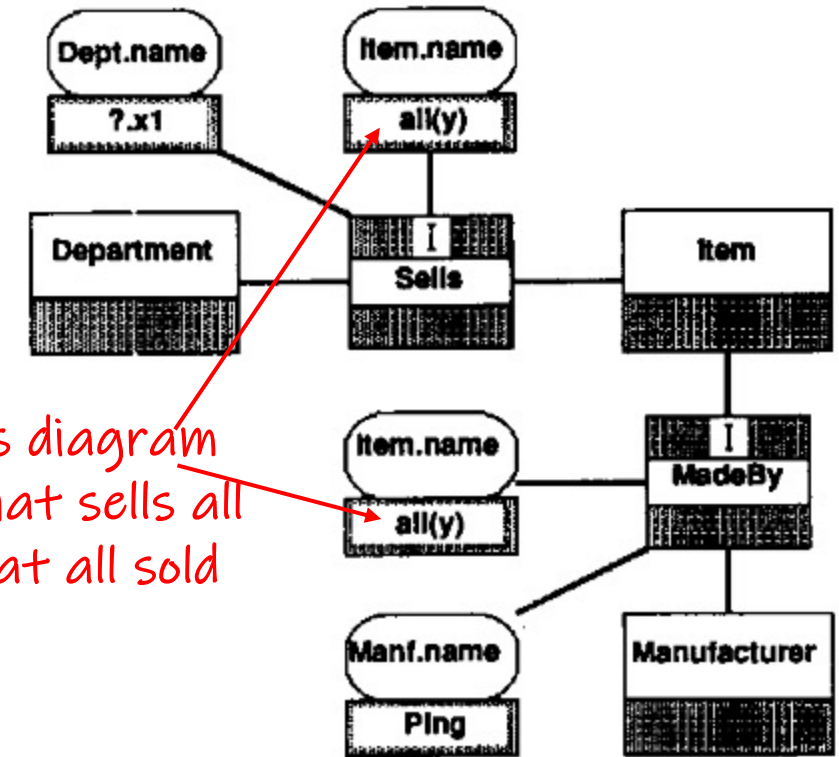


Fig. 12. A query that uses the “all” operator.



# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# DFQL (1994)

## DataFlow QL

Sources used:

- Clark, Wu. DFQL: Dataflow query language for relational databases. Information & Management, 1994. [https://doi.org/10.1016/0378-7206\(94\)90098-1](https://doi.org/10.1016/0378-7206(94)90098-1)
- Girsang. The comparison of SQL, QBE, and DFQL as query languages for relational databases, Master thesis, Naval Postgraduate School, 1994. <https://core.ac.uk/download/pdf/36723678.pdf>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>



# DFQL (DataFlow Query Language)

- Example visual representation that is relationally complete by mapping its visual symbols to the operators of RA
- Actually many Visual Query Languages (VQLs) become "visual" by introducing visual representations of RA operators in a dataflow
- Here, nodes represent the operations, instead of edges as in QBD
- We chose DFQL as representative since it has a nice documentation

We will ignore the "Display" operator that sends output to the screen

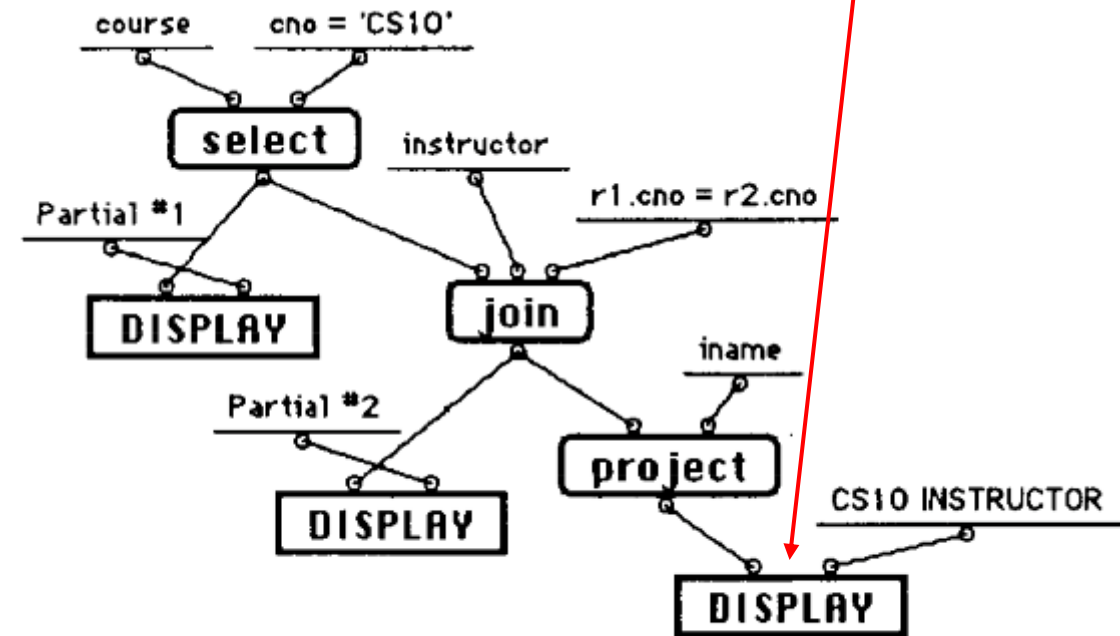
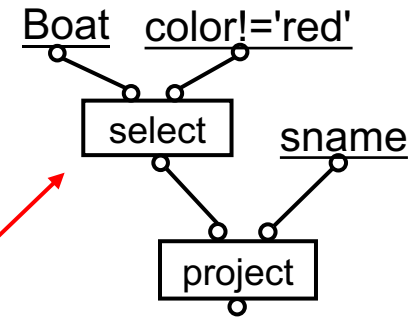


Fig. 19.

# DFQL (DataFlow Query Language)

*Q1b: "Find boats that are not red."*

```
select distinct bname  
from Boat  
where color != 'red'
```



boxes model the operators  
of RA (relational Algebra)  
in a top down "dataflow"

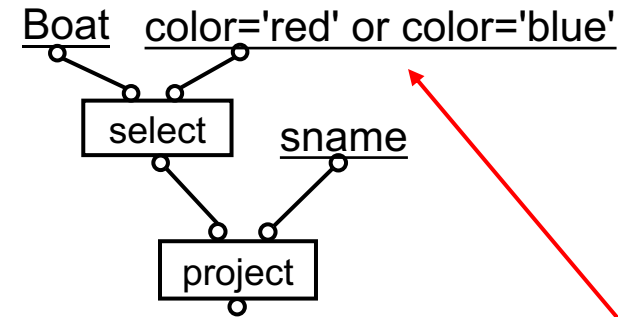
## Relational Algebra

$$\pi_{\text{sname}}(\sigma_{\text{color} \neq \text{'red'}} B)$$

# DFQL (DataFlow Query Language)

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```



conditions are in text

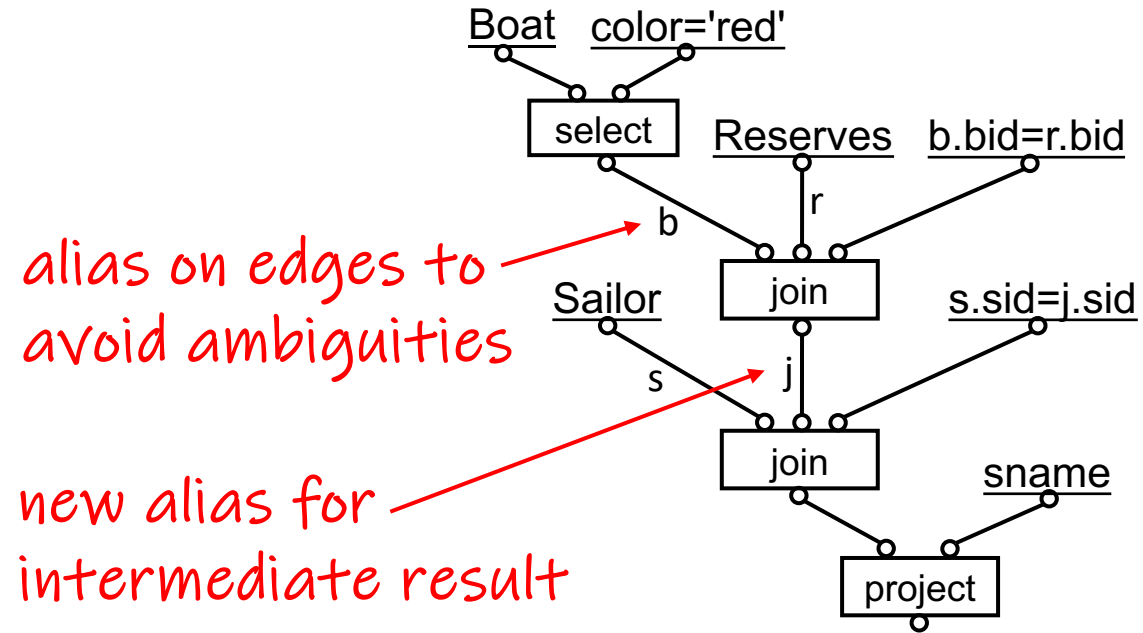
## Relational Algebra

$$\pi_{\text{sname}}(\sigma_{\text{color}='red' \vee \text{color}='blue'} B)$$

# DFQL (DataFlow Query Language)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



## Relational Algebra

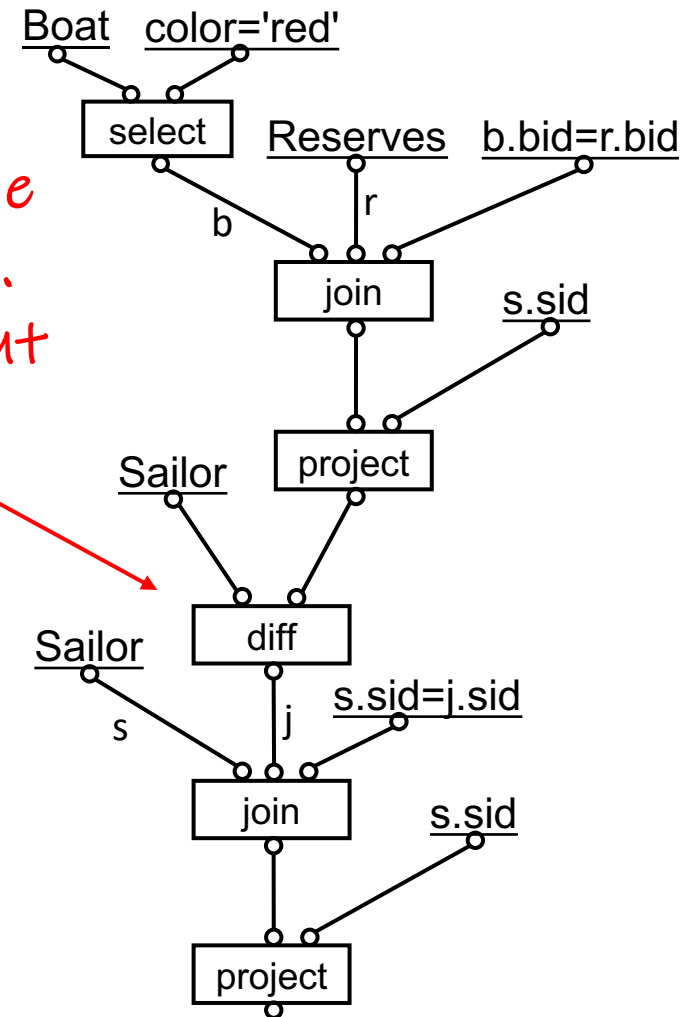
$$\pi_{\text{sname}}(S \bowtie R \bowtie \sigma_{\text{color}='red'} B)$$

# DFQL (DataFlow Query Language)

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

The diff operator is same  
as binary minus (-) in RA.  
Notice that order of input  
matters!



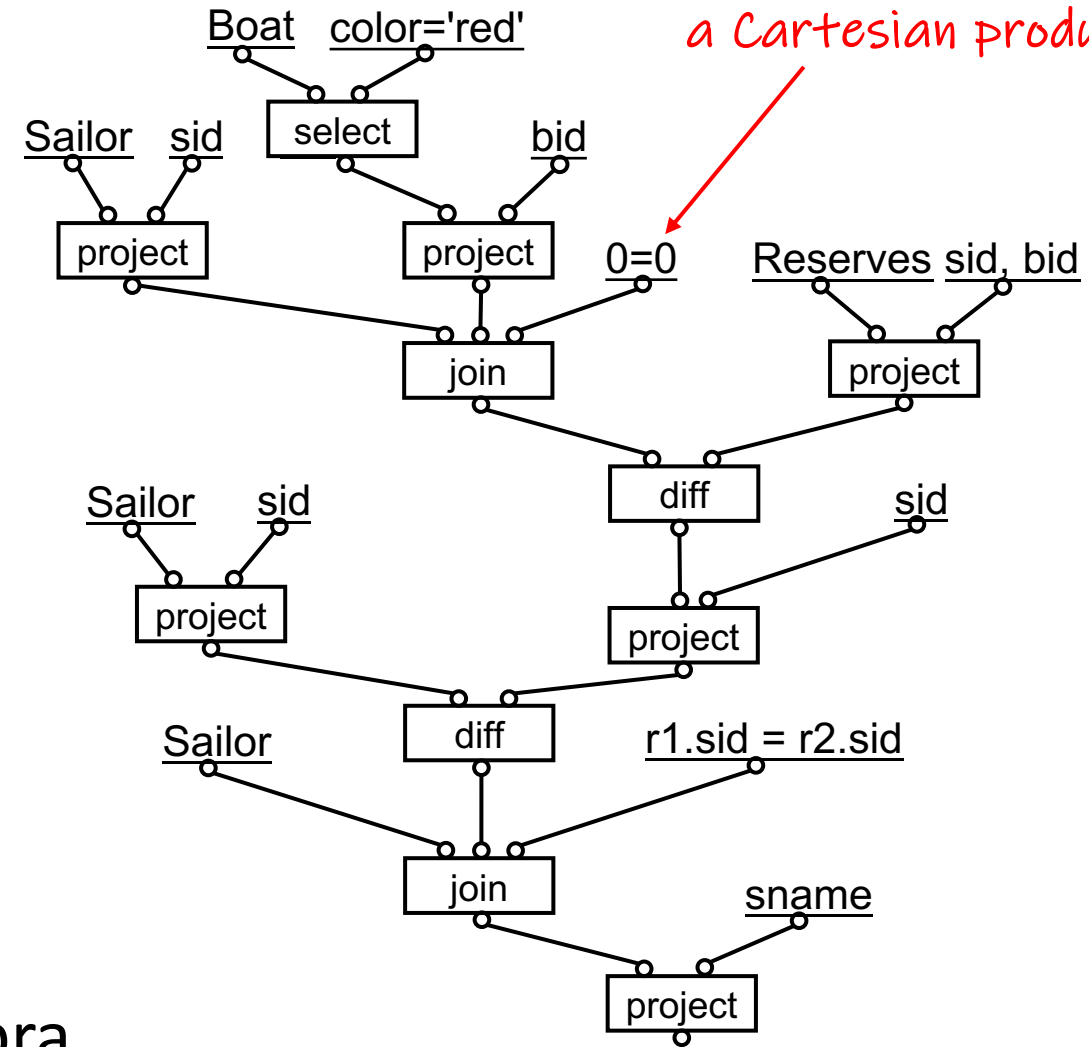
## Relational Algebra

$$\pi_{\text{sname}}(S \bowtie (\pi_{\text{sid}} S - (\pi_{\text{sid}} (R \bowtie \sigma_{\text{color}='red'} B))))$$

# DFQL (DataFlow Query Language)

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```



The tautology "0 = 0" in join operator is needed for a Cartesian product

## Relational Algebra

$$\pi_{sname}(S \bowtie (\pi_{sid} S - \pi_{sid}((\pi_{sid} S \times \pi_{bid} \sigma_{color='red'} B) - \pi_{sid,bid} R)))$$

# DFQL (DataFlow Query Language)

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where
  (select R.bid
   from Reserves R
   where S.sid=R.sid)
  CONTAINS
  (select B.bid
   from Boat B
   where color = 'red')
```

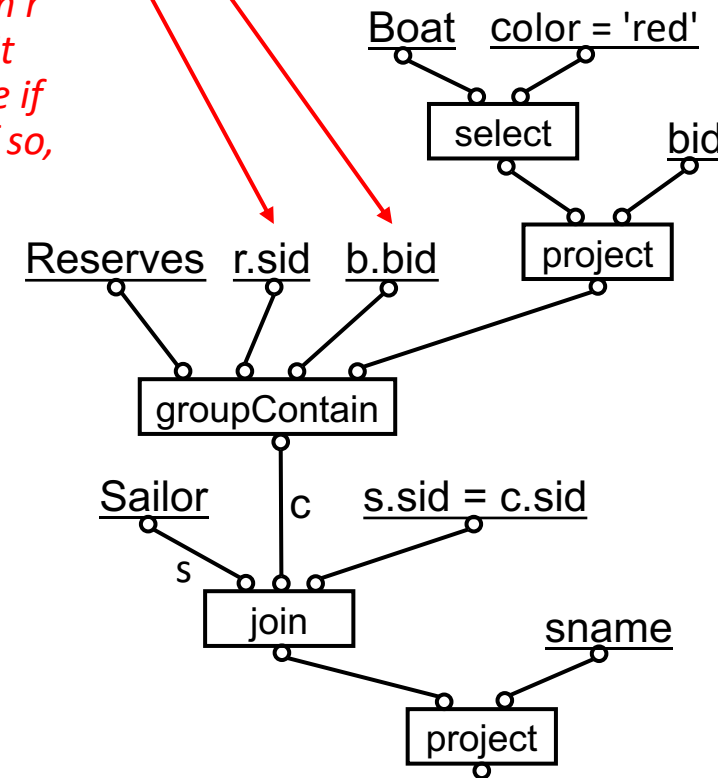
The "groupContain" operators takes the RESERVES relation  $r$  and the second relation  $b$  (with red boats) and groups the tuples in  $r$  according to the grouping attribute  $r.sid$ . It then compares with attributes  $b.bid$  to see if one  $r.sid$  has all the  $b.bid$  values from  $b$ . If so, the  $sid$  is selected

Invented SQL operator similar to relational division (but does not match exactly)

Relational Algebra

$$\pi_{sname}(S \bowtie (\pi_{sid,rid} R \div \pi_{bid} \sigma_{color='red'} B))$$

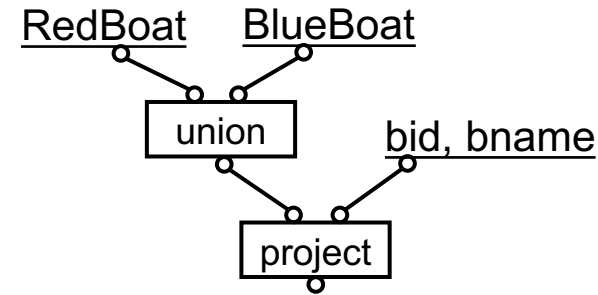
order left/right is crucial here



# DFQL (DataFlow Query Language)

Q5: "Find boats  
that are red or blue."

```
select bid, bname  
from RedBoat R  
union  
select bid, bname  
from BlueBoat B
```



Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

## Relational Algebra

$$\pi_{bid, bname}(\text{RedBoat} \cup \text{BlueBoat})$$



# DFQL (1994) DataFlow QL BACKUP

# DFQL (DataFlow Query Language)

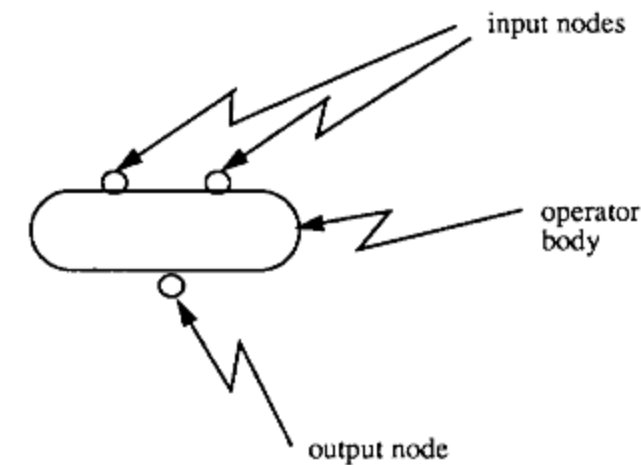


Fig. 3.

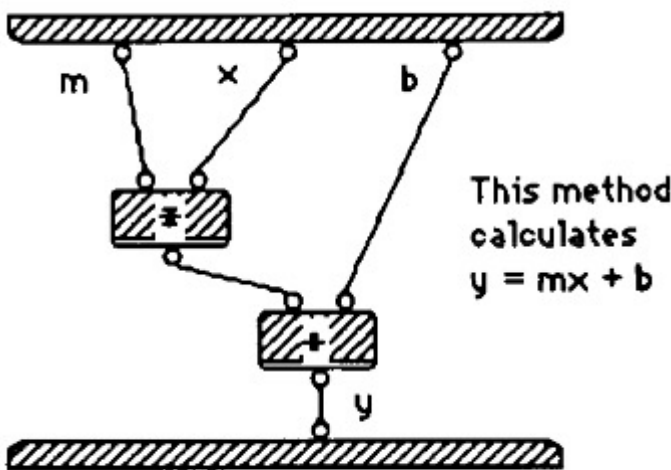
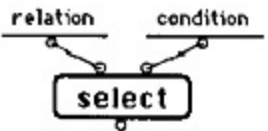
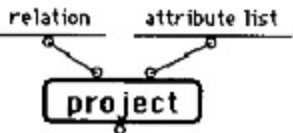


Fig. 2.

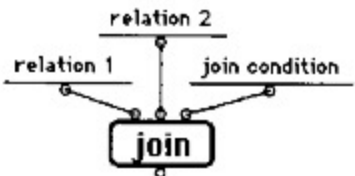
## DFQL



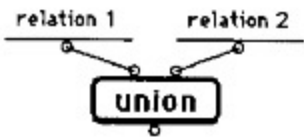
SELECT DISTINCT \*  
FROM relation  
WHERE condition;



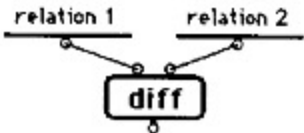
SELECT DISTINCT attribute list  
FROM relation;



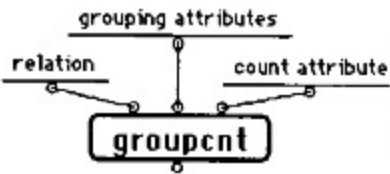
SELECT DISTINCT \*  
FROM relation1 r1, relation2 r2  
WHERE join condition;



SELECT DISTINCT \*  
FROM relation1  
UNION  
SELECT DISTINCT \*  
FROM relation2;



SELECT DISTINCT \*  
FROM relation1  
MINUS  
SELECT DISTINCT \*  
FROM relation2;



SELECT DISTINCT grouping attributes  
COUNT(\*) count attribute  
FROM relation  
GROUP BY grouping attributes;

Fig. 4.

# DFQL (DataFlow Query Language)

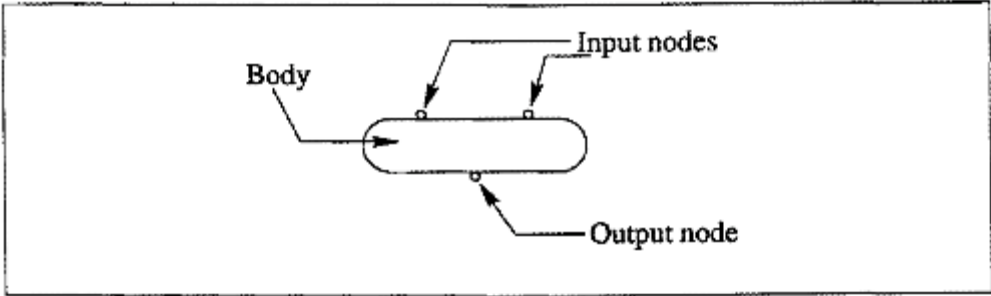


Figure 2.2: Operator Construction

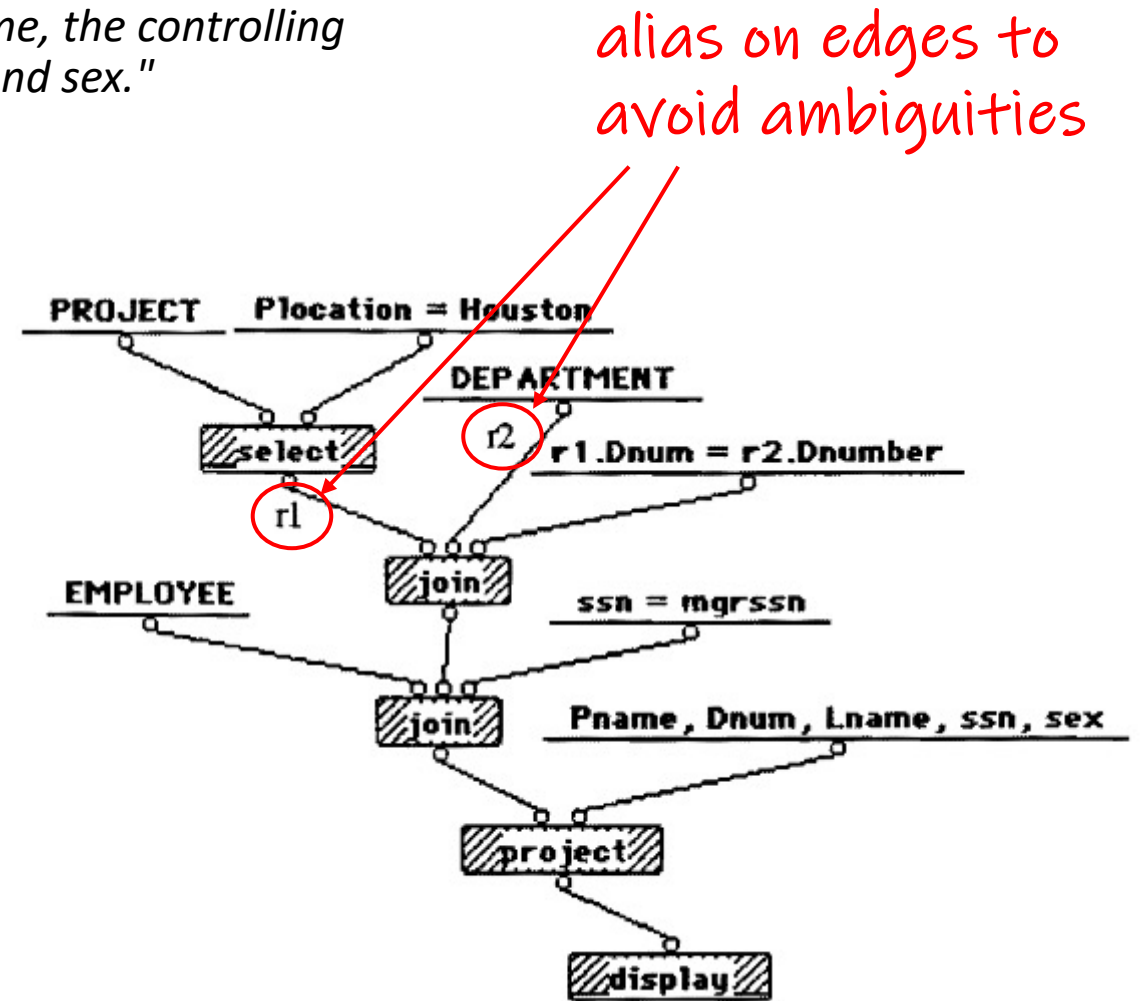
TABLE 2.1: BASIC DFQL OPERATORS AND THEIR SQL EQUIVALENTS

SQL	Description	SQL Equivalent
<div><div>relation   condition</div><div><div></div><div></div></div><div>select</div><div>SELECT</div></div>	<p>Implements the relational algebra <i>selection</i> operator. The algebraic notation is:</p> <p><math>\sigma_{\langle condition \rangle}(\langle relation \rangle)</math>.</p> <p>It retrieves tuples from the relation which fits the specified condition. There are no duplicate tuples in the result.</p>	<p><b>SELECT DISTINCT *</b></p> <p><b>FROM</b> relation</p> <p><b>WHERE</b> condition</p>
<div><div>relation   attribute list</div><div><div></div><div></div></div><div>project</div><div>PROJECT</div></div>	<p>Implements the relational algebra <i>projection</i> operator. The algebraic notation is:</p> <p><math>\pi_{\langle attribute list \rangle}(\langle relation \rangle)</math>.</p> <p>The attributes list, separated by commas contains the names of attributes to be retrieved from the relation . The <i>project</i> operator eliminates duplicate tuples from the result.</p>	<p><b>SELECT DISTINCT</b></p> <p>attribute list</p> <p><b>FROM</b> relation</p>

# DFQL (DataFlow Query Language)

Query 3: "For every project located in Houston, list the project name, the controlling department number, and department manager's last name, ssn, and sex."

```
SELECT PNAME, DNUM, LNAME, SSN, SEX
FROM   EMPLOYEE, DEPARTMENT, PROJECT
WHERE  MGRSSN = SSN AND DNUM = DNUMBER
      AND PLOCATION = 'Houston'
```

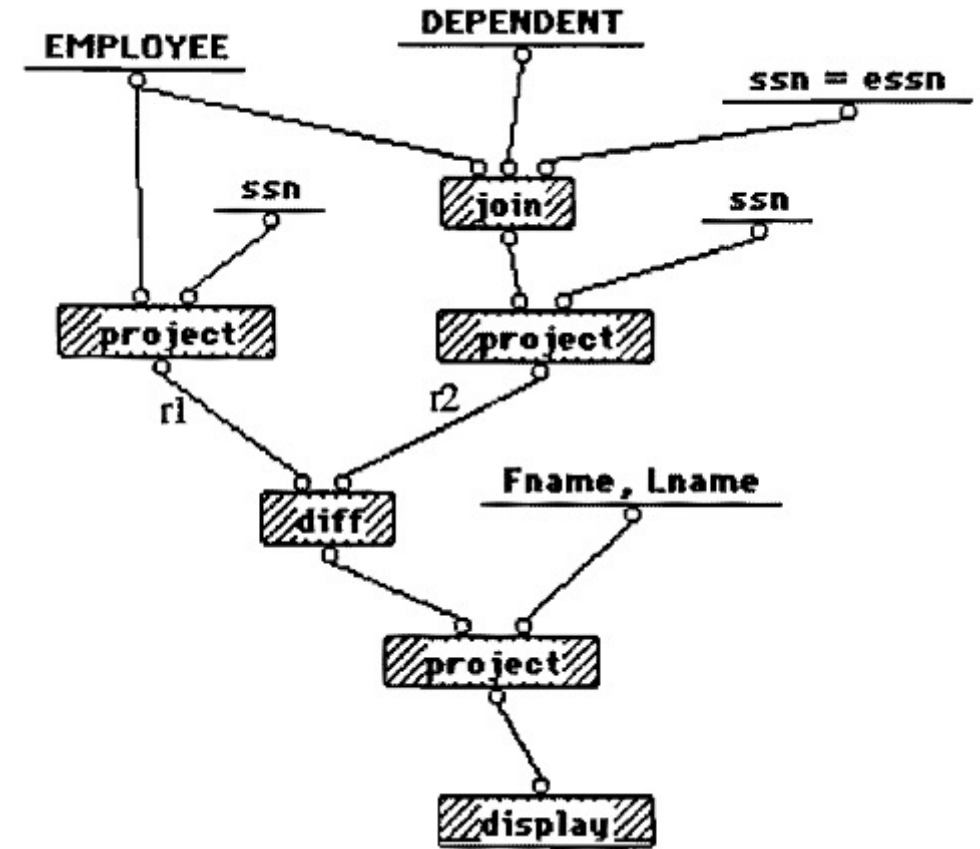


# DFQL (DataFlow Query Language)

Query 5: "For each department retrieve the first names and the last names of employees who have no dependents."

```
SELECT DNO FNAME, LNAME
FROM   EMPLOYEE
WHERE  NOT EXISTS (SELECT *
                   FROM   DEPENDENT
                   WHERE  SSN = ESSN)

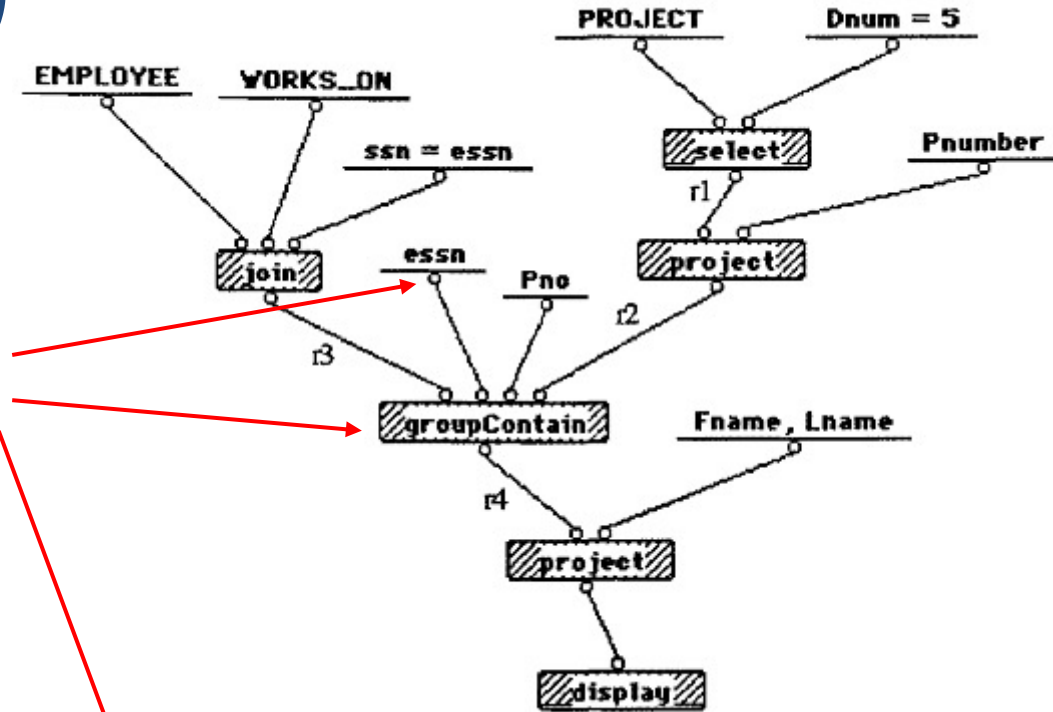
GROUP BY DNO
```



# DFQL (DataFlow Query Language)

Query 9: "Retrieve the first name and last name of each employee who works on all the projects managed by department number 5."

Based on the description of the operator, there seems to be an error in the visualization: the "groupContain" only returns the essn's, and a subsequent join with Employee is necessary



```
SELECT FNAME, LNAME
FROM EMPLOYEE
WHERE NOT EXISTS
```

```
(SELECT *
FROM WORKS_ON B
WHERE (B.PNO IN (SELECT PNUMBER
FROM PROJECT
WHERE DNUM = 5))
```

```
AND
NOT EXIST (SELECT *
FROM WORKS_ON C
WHERE C.ESSN = SSN
AND C.PNO = B.PNO))
```

```
SELECT FNAME, LNAME
FROM EMPLOYEE
WHERE (SELECT PNO
FROM WORKS_ON
WHERE SSN = ESSN)
CONTAINS
(SELECT PNUMBER
FROM PROJECT
WHERE DNUM = '5')
```

The **groupContain** operator takes the WORKS\_ON relation (r1) and the second relation (r2) and groups the tuples according to the grouping attribute essn. It then compares attribute Pno to see if one essn has all the Pno values contained in r2. If so, the essn is selected.

1. *GroupContain* operator is a part of *Group Set Comparison*. *GroupSet Comparison* also provides *GroupEqual* and *GroupContainBy* operators. These operators are discussed in class notes of Dr. C. Thomas Wu, Computer Science Department, Naval Postgraduate School, Monterey, CA.

Notice that the **CONTAINS** comparison operator in this query is similar in function to the DIVISION operation of the relational algebra [Elma 89].



# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# Visual SQL (2003)

## Sources used:

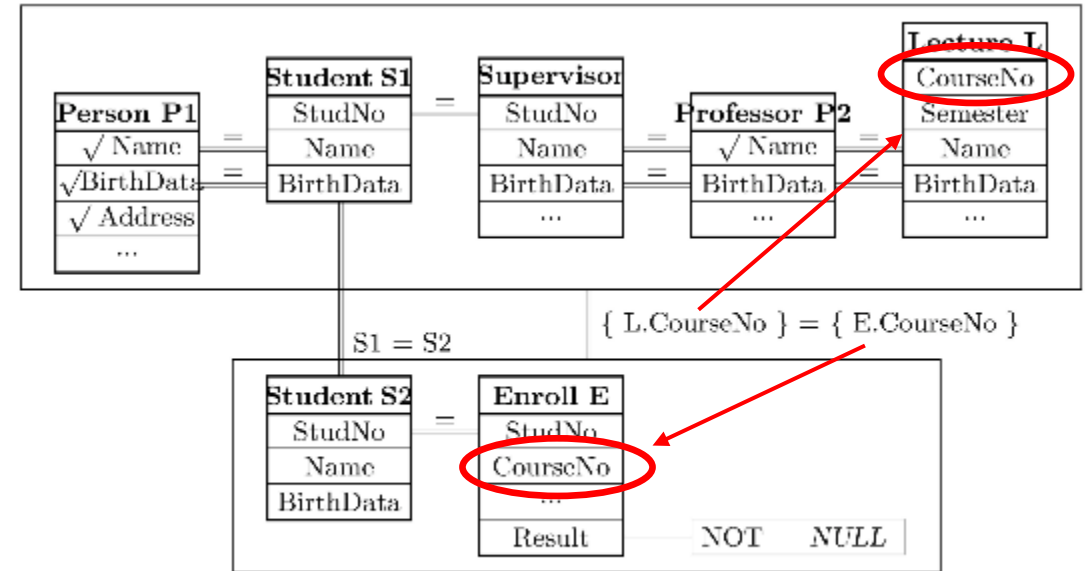
- Jaakkola, Thalheim. Visual SQL -- high-quality ER-based query treatment. ER workshops, 2003. [https://doi.org/10.1007/978-3-540-39597-3\\_13](https://doi.org/10.1007/978-3-540-39597-3_13)
- Thalheim. Visual SQL -- Eine ER-basierte Einfuehrung in die Datenbankprogrammierung. Teil I. Report I-08/03 of the Computer Science Institute at BTU Cottbus, Cottbus, 2003.
- Thalheim. Visual SQL as the alternative to Linear SQL. Talk slides. 2013. Originally available online at:  
[https://www.is.informatik.uni-kiel.de/fileadmin/arbeitsgruppen/is\\_engineering/visualsql/HERM.VisualSQL.Talk2013.pdf](https://www.is.informatik.uni-kiel.de/fileadmin/arbeitsgruppen/is_engineering/visualsql/HERM.VisualSQL.Talk2013.pdf) (4/2020)



# Visual SQL

- The goal of Visual SQL was primarily **query composition**, but a Java implementation also supports the reverse functionality of query visualization to a large extent
- The tool focus on representing syntactic details and some details are not shown visually
- Notice that the notation uses a **more visually familiar UML notation**

- Notice that the original website has since disappeared and other unrelated tools can now be found under the name "VisualSQL"

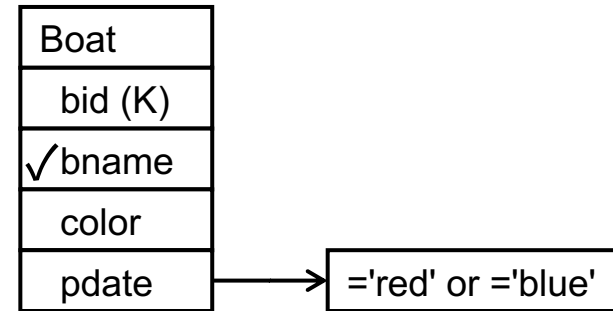


**Fig. 1.** Visual SQL Involving Equality On Two Visual SQL Subqueries

# Visual SQL

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```

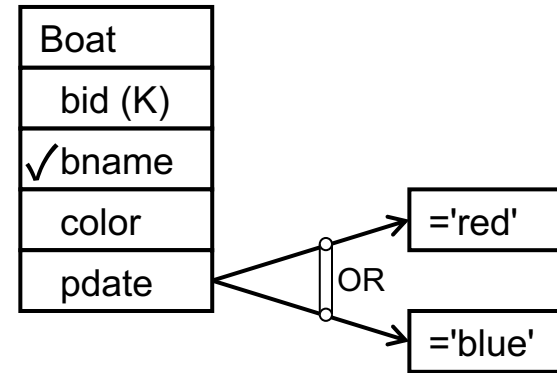


Disjunctions are explicitly  
expressed inside a box

# Visual SQL

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```

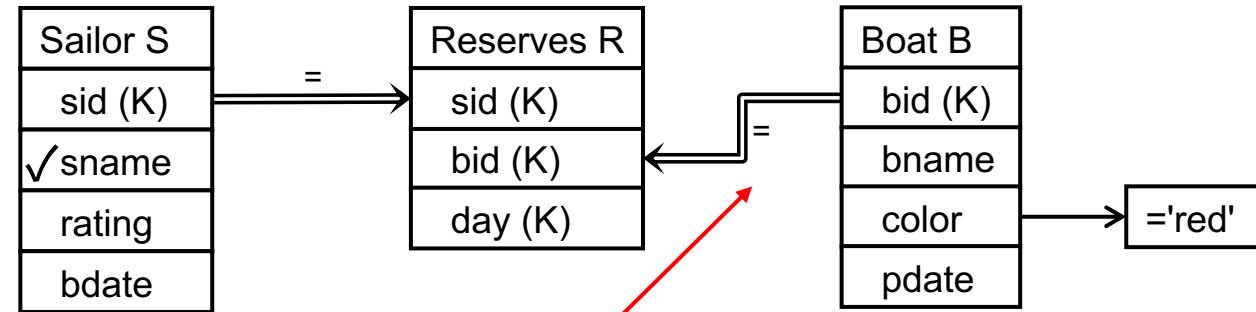


*An alternative suggestion was  
to connect two alternative lines  
with an "OR" labeled connector*

# Visual SQL

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



Joins use double-lined arcs. Direction is determined by the predicate

... B.bid=R.bid ...

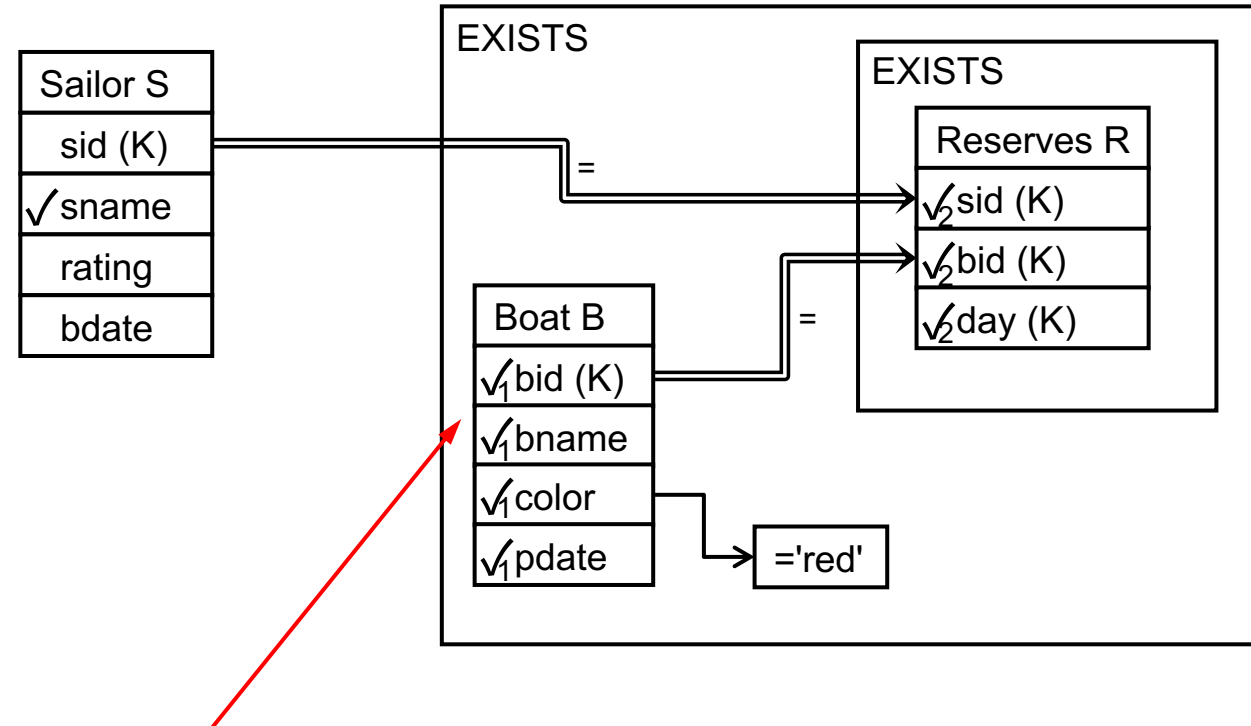


# Visual SQL

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
where exists
  (select *
   from Boat B
   where color = 'red'
   and exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

Nested queries preserve the scope of nestings

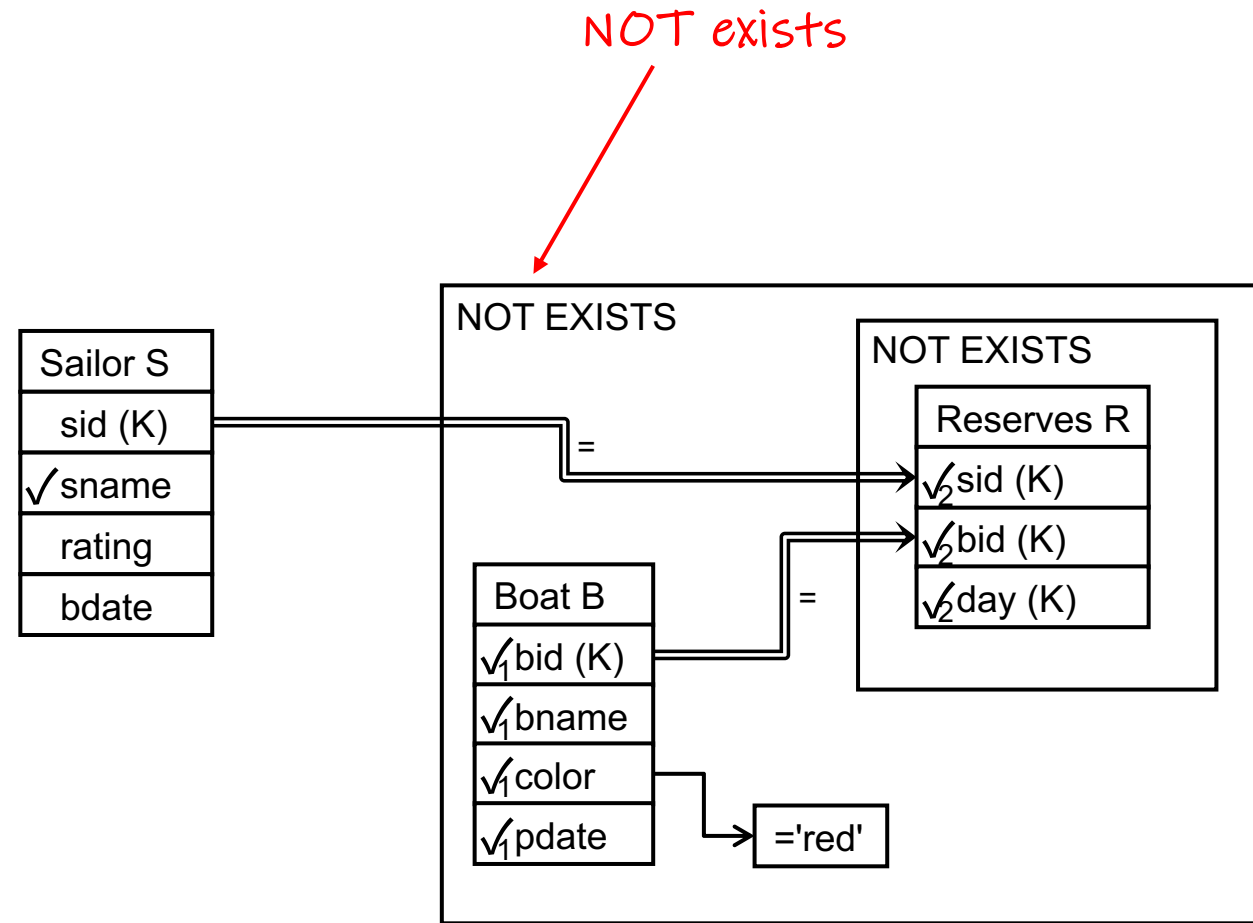


Check-marks are labeled with indices likely based on when the subquery appears in the SQL text. SELECT \* leads to all attributes being checked.

# Visual SQL

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

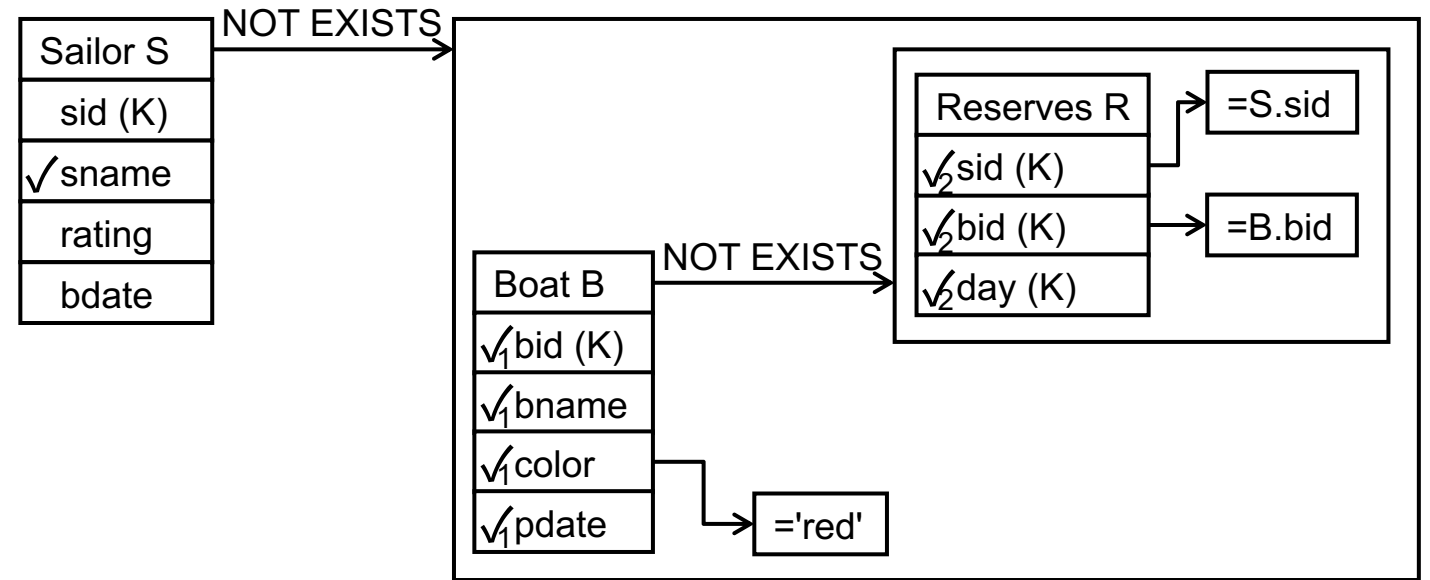


# Visual SQL

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

An alternative proposal that visually represents "NOT EXISTS" as connection between a table and the subquery

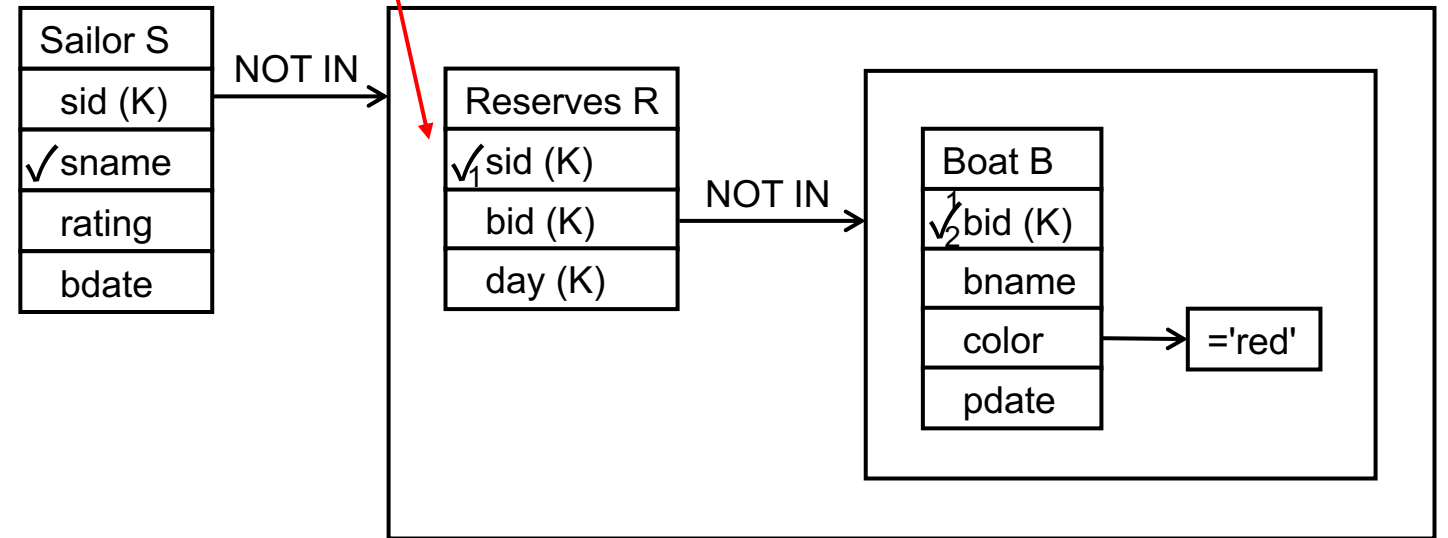


# Visual SQL

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where S.sid not in
  (select R.sid
   from Reserves R
   where R.bid not in
     (select B.bid
      from Boat B
      where color = 'red'))
```

"NOT IN" is represented as connection between an attribute and the subquery. The projected attribute in the subquery is important.

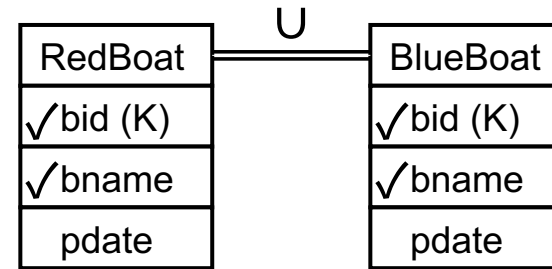




# Visual SQL

Q5: "Find boats  
that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```



## Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

# Visual SQL (2003)

## BACKUP

# Visual SQL

Q: "Return ("successless") students who no enrollment with null as result."

Check-marks show selected attributes

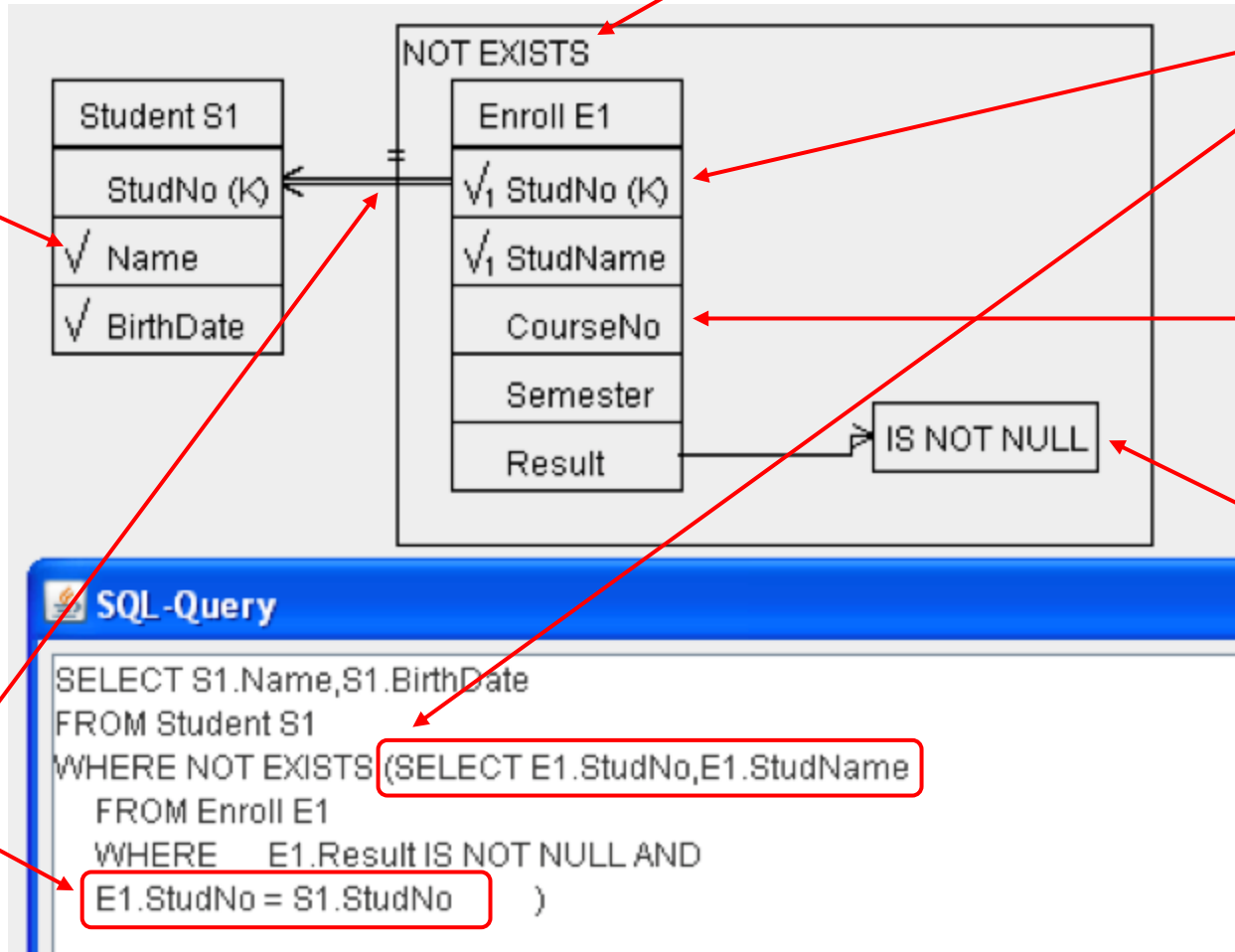
EXISTS / NOT EXISTS written out with words and different from IN / NOT IN

Attributes "selected" in a subquery are marked with a labeled check mark

All attributes from a table are shown even if not used.

Constants for selection predicates are in separate boxes

Arrows preserve the order of the attributes in the predicate



# Visual SQL

*Provide data on students who have successfully completed those and only those courses which have successfully been given or which are currently given by the student's supervisor?*

```
SELECT  P1.Name, P1.BirthData, P1. Address,
        P2.Name AS "Name of supervisor"
FROM    Person P1, Professor P2, Student S1, Supervisor, Lecture L,
        Enroll E
WHERE   P1.Name = Student.Name AND P1.BirthData = Student.BirthData
        AND S1.StudNo = E.StudNo
        AND E.Result NOT NULL
        AND S1.StudNo = Supervisor.StudNo
        AND Supervisor.Name = Professor.Name
        AND Supervisor.BirthData = Professor.BirthData
        AND P2.Name = Professor.Name AND P2.BirthData = P2.BirthData
        AND L.Name = Professor.Name AND L.BirthData = Professor.BirthData
        AND
        L.CourseNo
        IN
        (SELECT E2.CourseNo
         FROM  Enroll E2
         WHERE
             S1.StudNo = E2.StudNo  AND
             E2.Result NOT NULL
        )
        AND
        E.CourseNo
        IN
        (SELECT  L2.CourseNo
         FROM    Lecture L2
         WHERE
             L2.Name = P2.Name AND
             L2.BirthData = P2.BirthData
        );
```

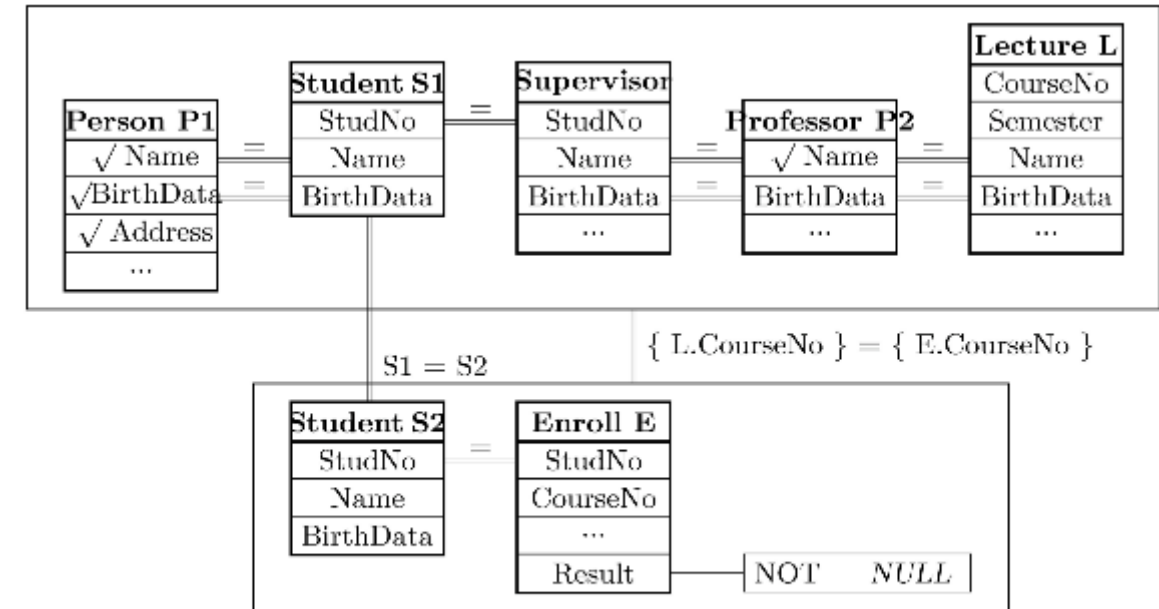
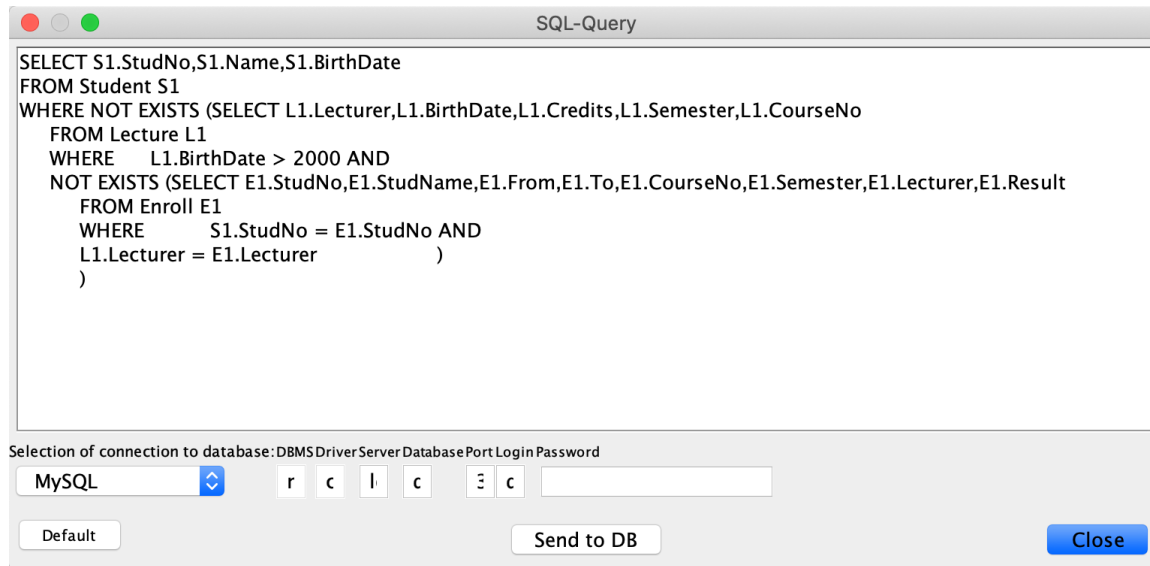


Fig. 1. Visual SQL Involving Equality On Two Visual SQL Subqueries

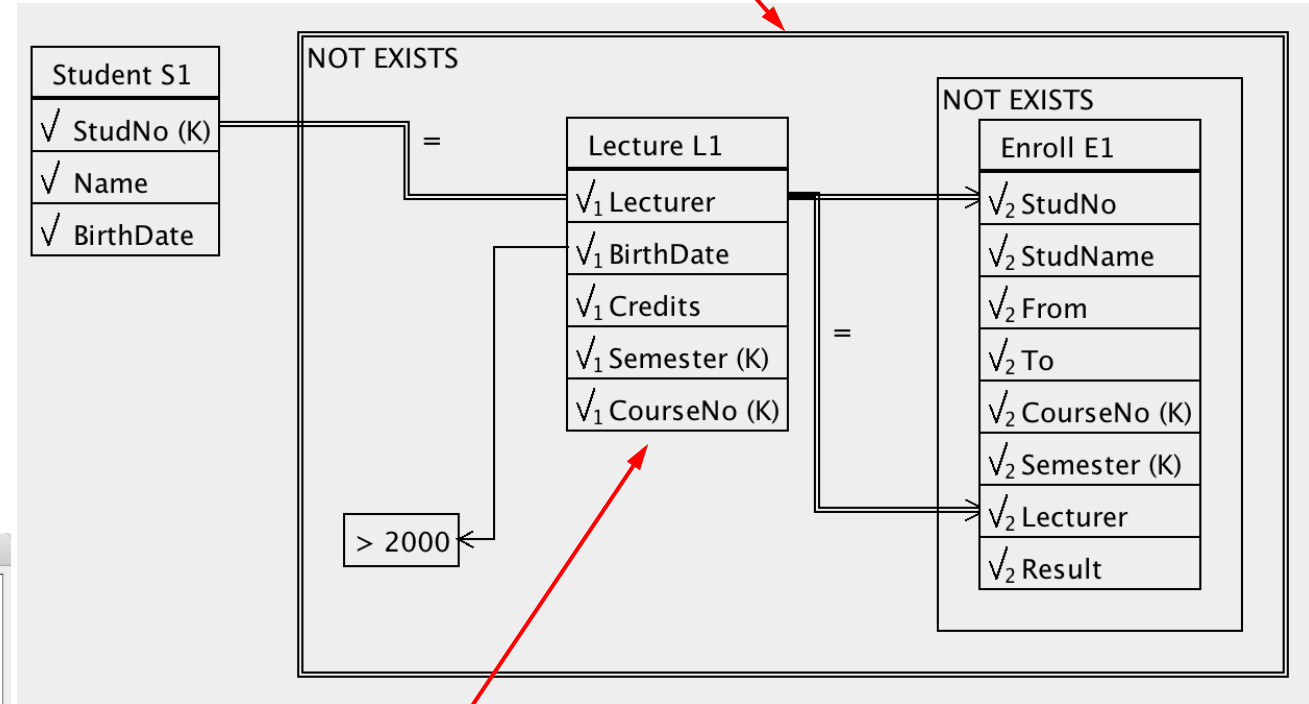
The visualization contains fewer tables and the translation between the visualization and SQL is not explained in the paper.

# Visual SQL

*Q: "Find students who have taken classes from all lecturer who were born after 2000"*



double-line is assumed a bug and not part of the motivation



outline of L1 is overlapping with the connection between S1 and E1 and is better moved to the right or below)

# Visual SQL

Subqueries connected other than "(not) exists" are connected at the whole nesting level of the subquery.

This line likely should start at S1.MatrNr. to mean:  
... and S1.MatrNr not in  
(select S2.Matr.Nr from...

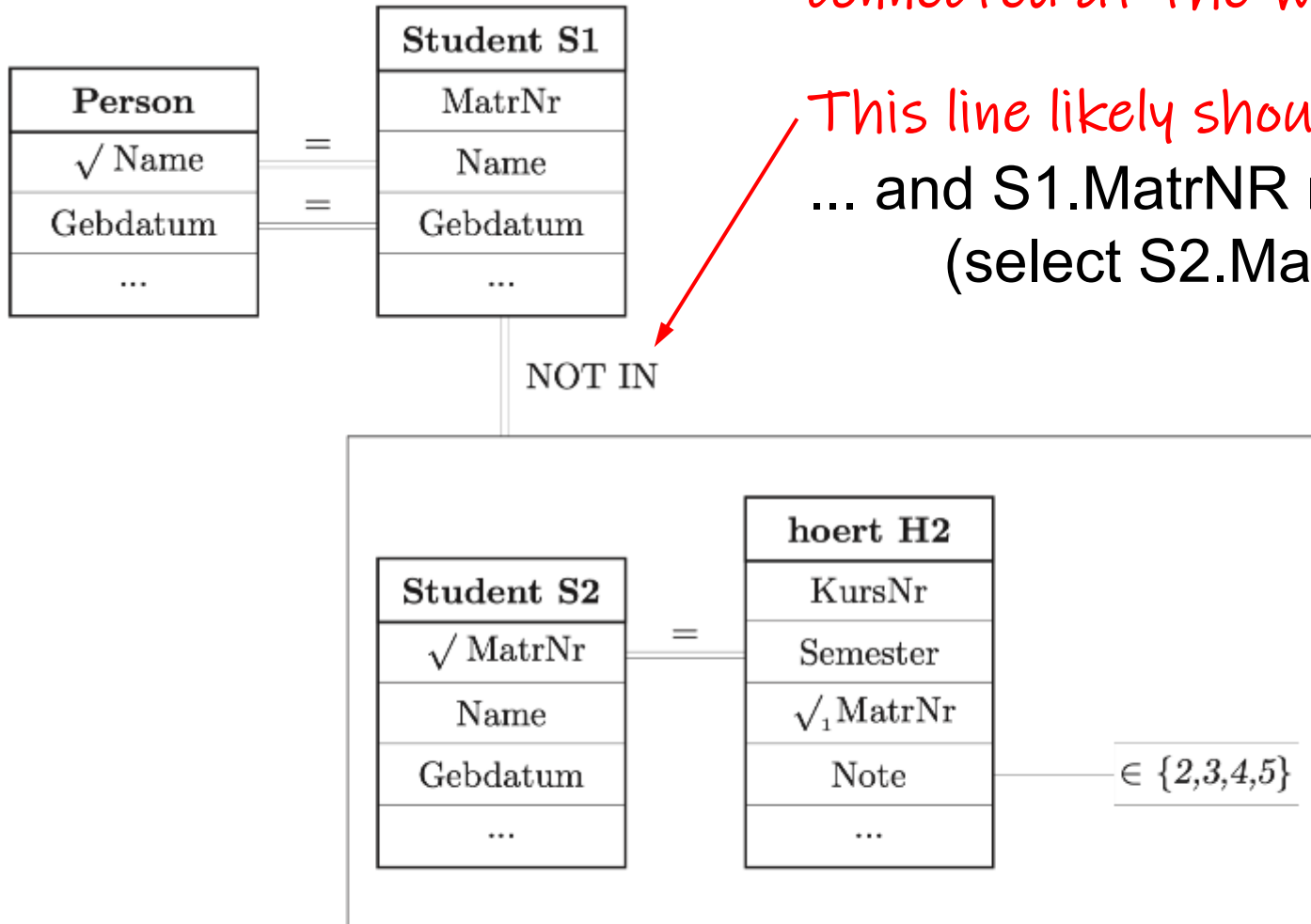


Bild 40: Teilanfrage mit Differenzbildung

# Visual SQL

Complicated Boolean expressions are hard to visualize (by nature)

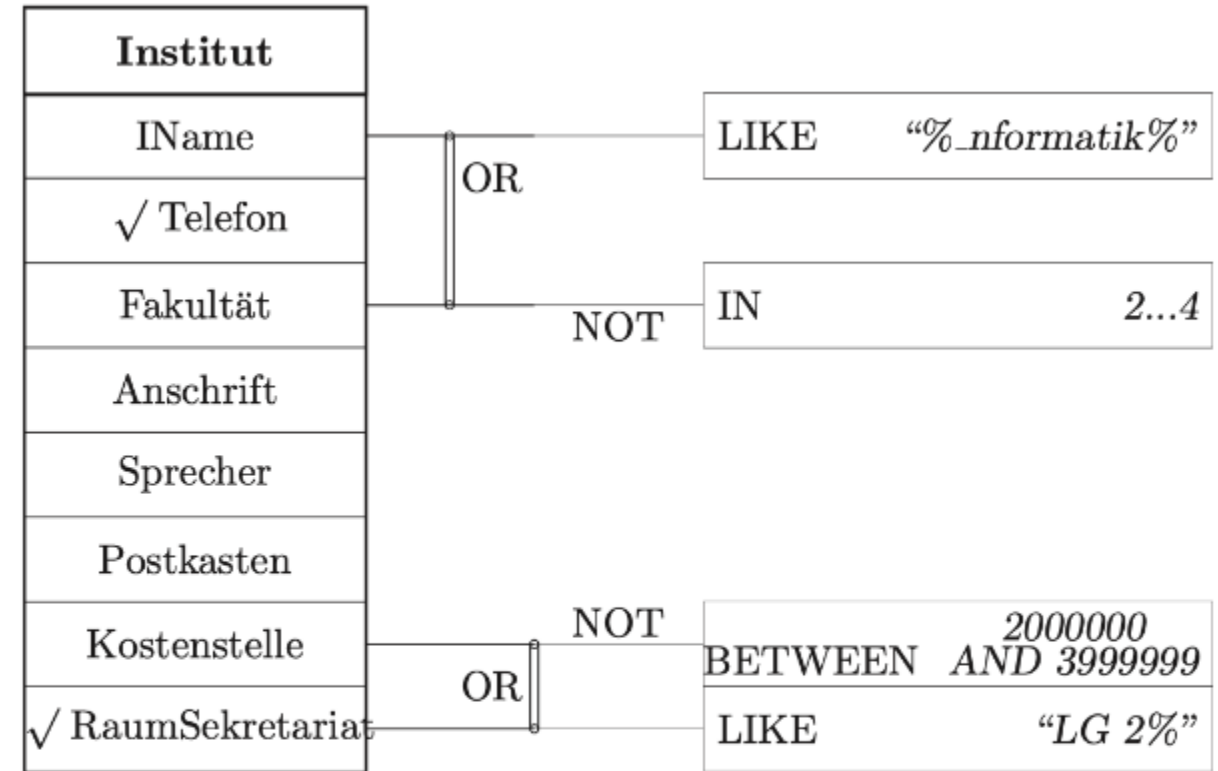


Bild 20: Auswahl in Klassen mit AND, OR und NOT

```
SELECT  Telefon, RaumSekretariat
FROM    Institut
WHERE   (IName LIKE "%_nformatik%" OR Fakultät NOT IN (2,3,4))
AND     (RaumSekretariat LIKE "LG 2%" OR
         Kostenstelle NOT BETWEEN 2000000 AND 3999999);
```

# Visual SQL

*Complicated Boolean expressions are hard to visualize (by nature)*

*Here the nesting sequence is captured by indices*

*... X or Y or (A and B)...*

*or is higher nested, thus index 1 and then has index 2*

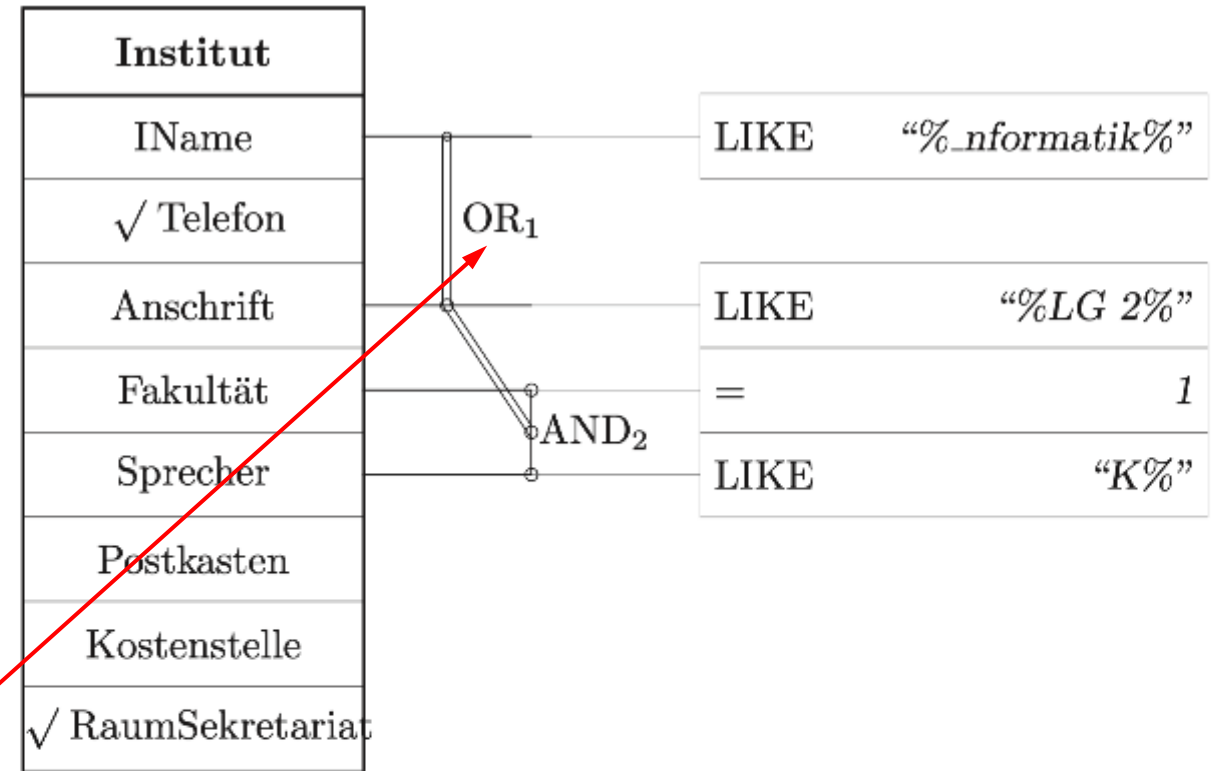


Bild 19: Auswahl in Klassen mit AND und OR

```
SELECT  Telefon, RaumSekretariat
FROM    Institut
WHERE   Anschrift LIKE "%LG 2%"    OR    IName LIKE '%_nformatik\%'
        OR    (Fakultaet = 1    AND    Sprecher LIKE "K%");
```



# Visual SQL

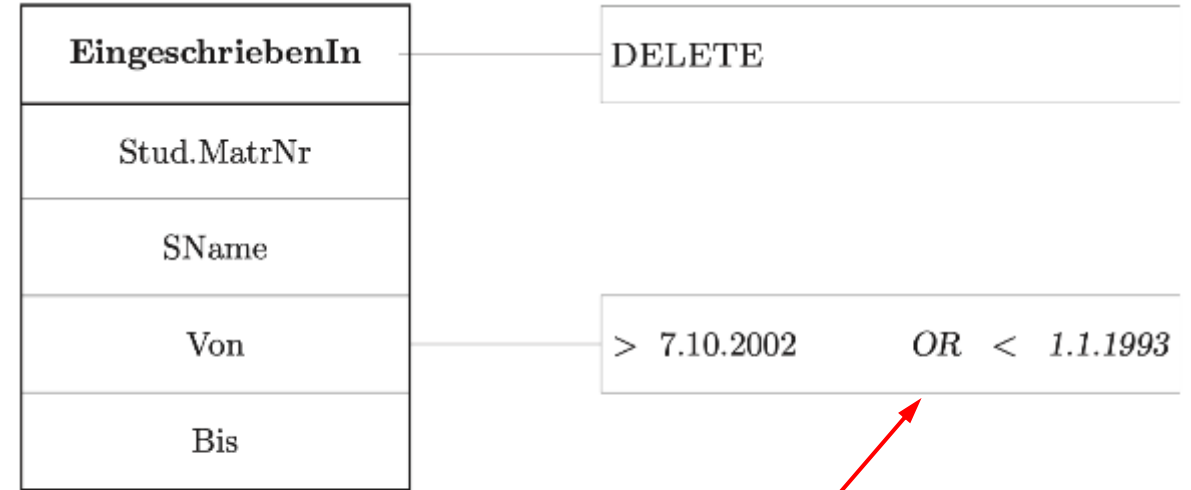


Bild 14: Streichen von Objekten mit Bedingung

```
DELETE FROM Eingeschrieben
WHERE Von > 7.10.2002 OR Von < 1.1.1993;
```

# Visual SQL

*Additional box is used  
for Cartesian product*

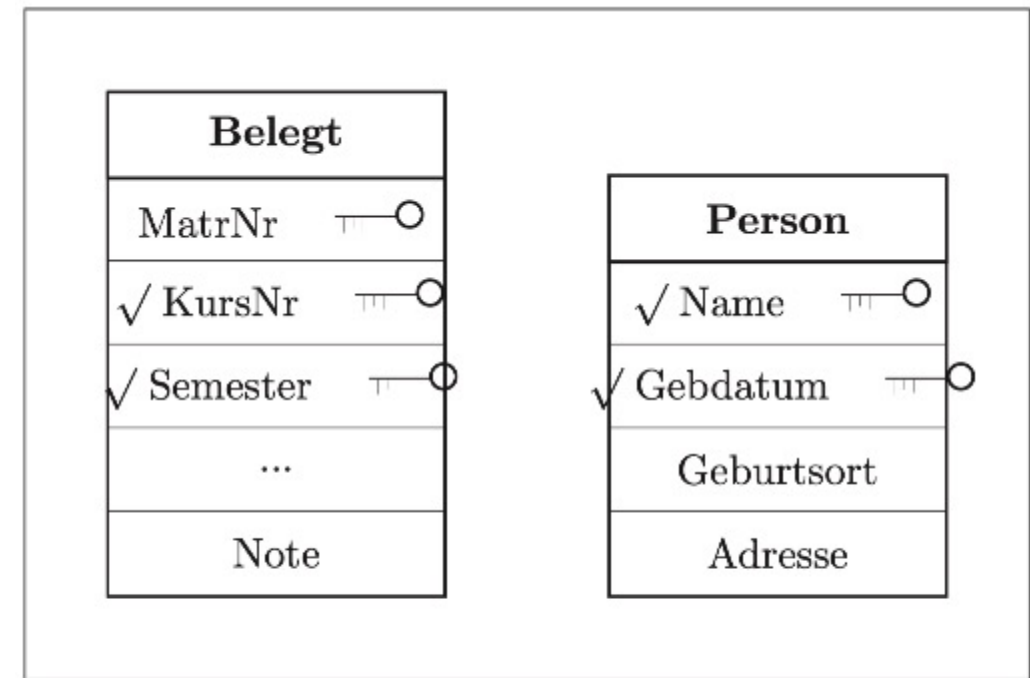


Bild 28: Kartesisches Produkt mit Projektion

```
SELECT  KursNr, Semester, Name, Gebdatum
FROM    Belegt, Person;
```

# Visual SQL

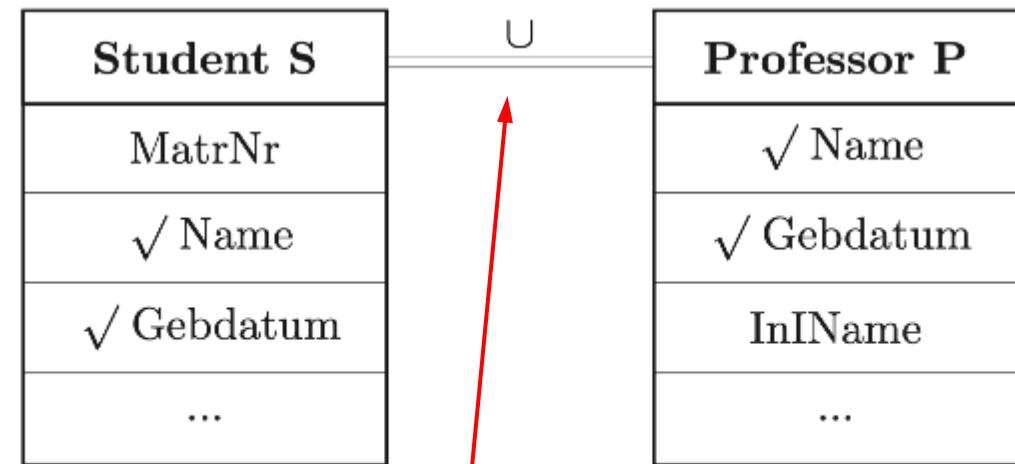


Bild 47: Vereinigung von zwei vollständig typengleichen Relationen

```
SELECT      S.Name, S.Gebdatum
  FROM      Student S
UNION
SELECT      P.Name, P.Gebdatum
  FROM      Professor P;
```

# Visual SQL

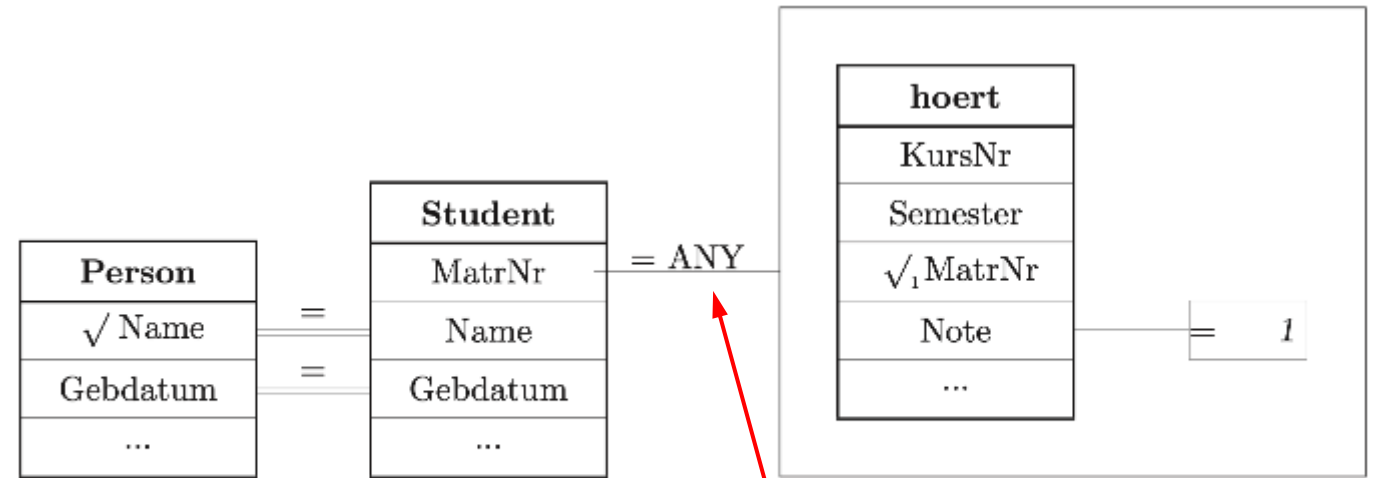


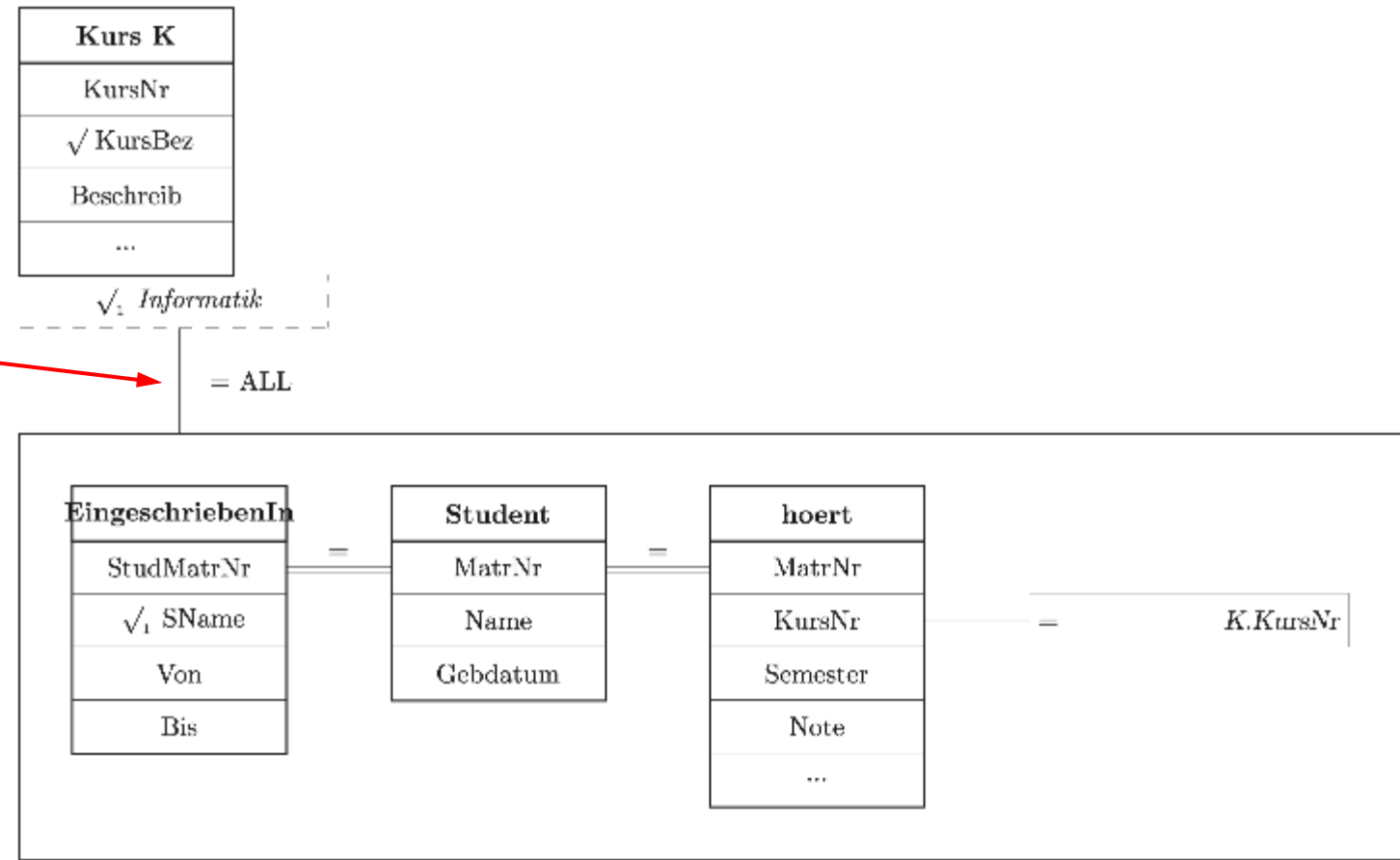
Bild 38: Teilanfrage mit Vergleich

Subquery with ANY

```
SELECT  Name
FROM    Person, Student
WHERE   Person.Name = Student.Name AND Person.Gebdatum = Student.Gebdatum AND
        MatrNr = ANY
        (SELECT S1.MatrNr
         FROM hoert S1
         WHERE Note = 1);
```

# Visual SQL

Subquery with ALL



```
SELECT      K.KursBez
FROM        Kurs K
WHERE       "Informatik" = ALL
            (SELECT      SName
              FROM        hoert, Student, EingeschriebenIn
              WHERE       K.KursNr = hoert.KursNr
                        AND Student.MatrNr = hoert.MatrNr
                        AND EingeschriebenIn.StudMatrNr = Student.MatrNr );
```

Bild 52: Korrelierte Teilanfragen mit ALL

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

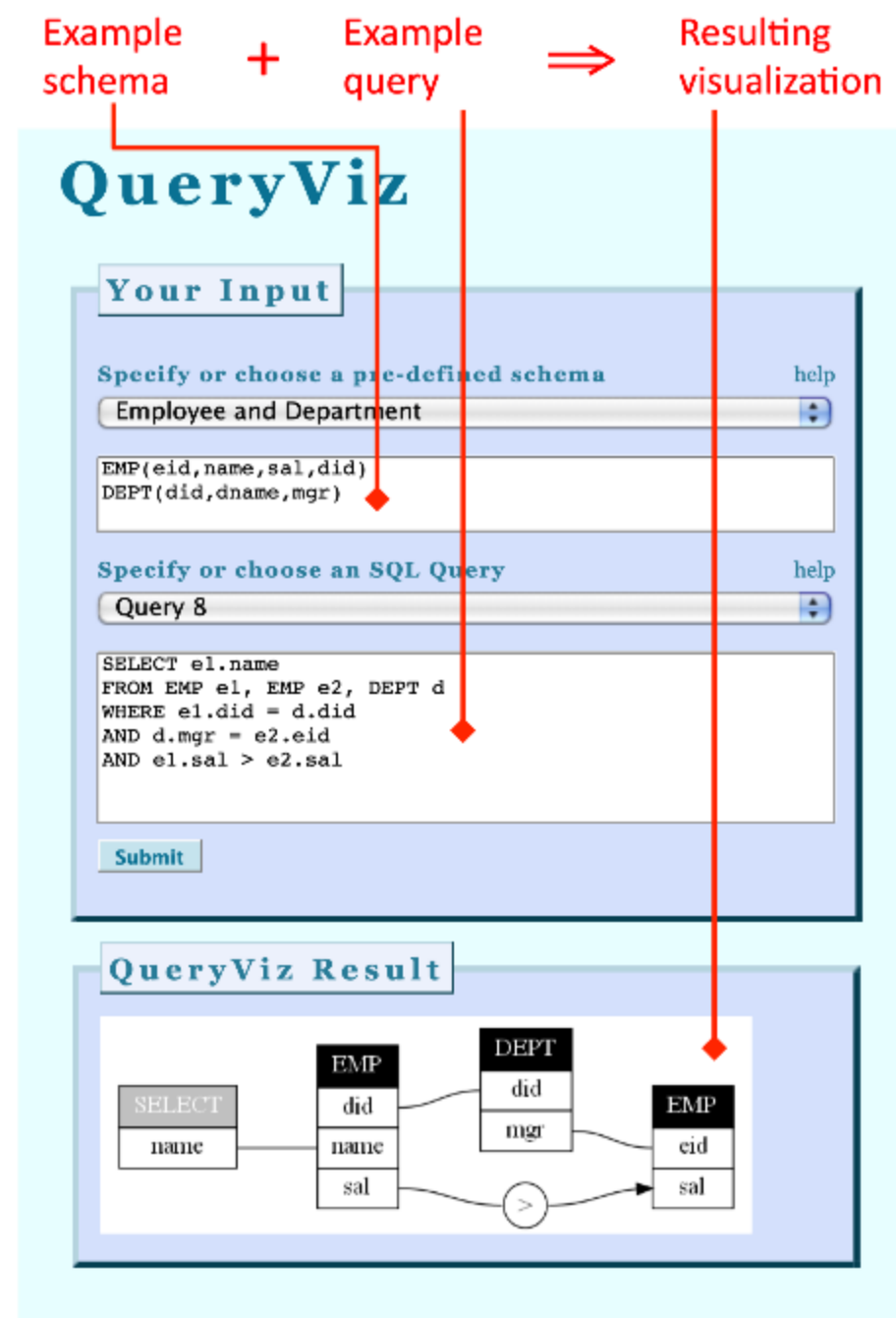
# QueryVis (2011) (also QueryViz)

## Sources used:

- Danaparamita, Gatterbauer. QueryViz: Helping Users Understand SQL queries and their patterns. EDBT demo. 2011. <https://doi.org/10.1145/1951365.1951440>
  - Gatterbauer. Databases will Visualize Queries too. PVLDB vision 2011. <https://doi.org/10.14778/3402755.3402805>,  
presentation slides: [https://gatterbauer.name/download/vldb2011\\_Database\\_Query\\_Visualization\\_presentation.pdf](https://gatterbauer.name/download/vldb2011_Database_Query_Visualization_presentation.pdf),  
video: [https://www.youtube.com/watch?v=kVFhQRGAQIs&list=PL\\_72ERGKF6DR4R0Cowx-LnnnqLXRf4ZjB](https://www.youtube.com/watch?v=kVFhQRGAQIs&list=PL_72ERGKF6DR4R0Cowx-LnnnqLXRf4ZjB)
  - Leventidis, Zhang, Dunne, Gatterbauer, Jagadish, Riedewald. QueryVis: Logic-based Diagrams help Users Understand Complicated SQL Queries Faster. SIGMOD. 2020. <https://doi.org/10.1145/3318464.3389767>
- Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# QueryVis (formerly QueryViz)

- The goal of QueryVis is the reverse functionality of VQLs and to **visualize existing SQL queries** with simple, easy-to-read diagrams
- Inspired by diagrammatic reasoning systems, uses topological properties, such as enclosure, to represent logical expressions and set-theoretic relationships
- The EDBT'11 demo takes a SQL query as input and returns a query visualization. It has been online since then (with interruptions):  
<http://demo.queryvis.com>

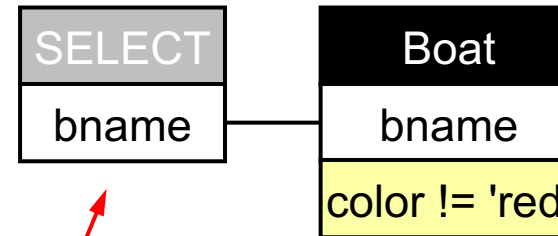




# QueryVis (formerly QueryViz)

*Q1b: "Find boats  
that are not red."*

```
select distinct bname  
from Boat  
where color != 'red'
```



*An output table is explicitly models  
(allows e.g. renaming of attributes)*

Schema

Boat
<u>bid</u>
bname
color
pdate

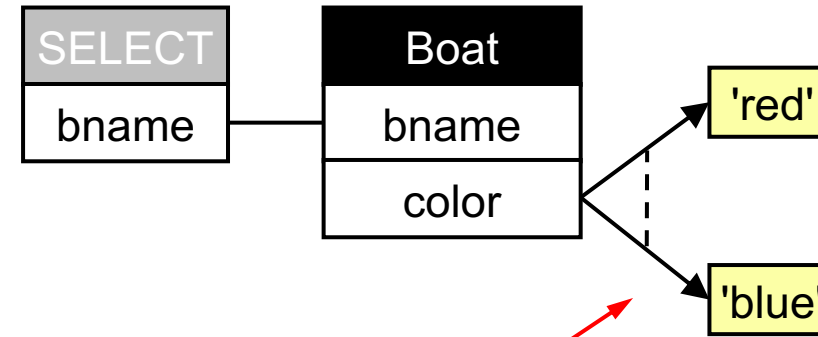
# QueryVis (formerly QueryViz)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```



Disjunction was never implemented in online QueryVis

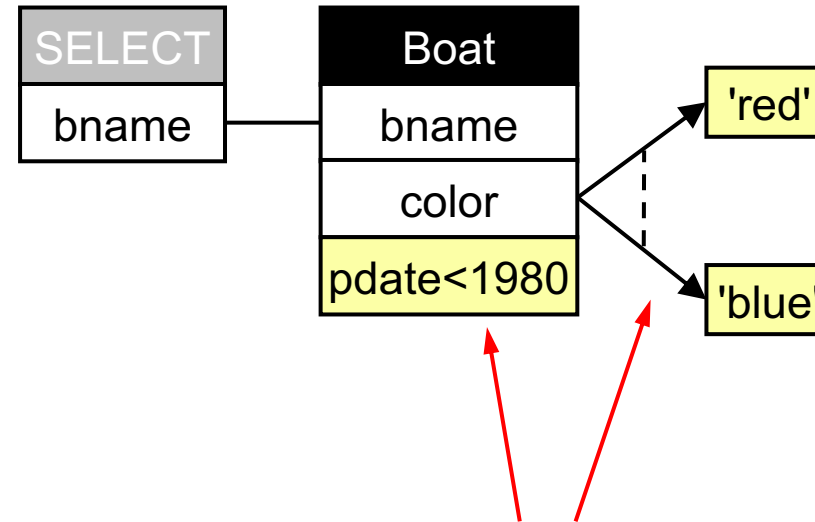
# QueryVis (formerly QueryViz)

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```



Conditions on separate attributes can be applied on each attribute separately. However, it is not clear how to express complicated Boolean expressions involving multiple attributes, such as:  
"(color = 'red' and pdate < 1980) or (color = 'blue' and pdate > 1980)"  
More on this later

Figure drawn based on the presentations for "Gatterbauer. Databases will Visualize Queries too. PVLDB vision 2011. <https://doi.org/10.14778/3402755.3402805>":

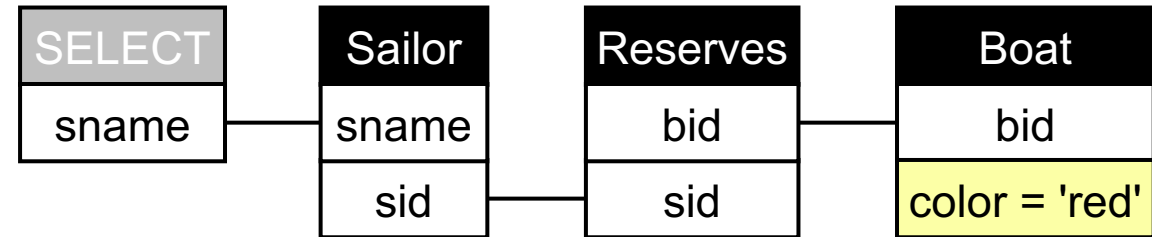
[https://www.youtube.com/watch?v=kVFhQRGAQIs&list=PL\\_72ERGKF6DR4R0Cowx-LnnngLXRf4ZjB](https://www.youtube.com/watch?v=kVFhQRGAQIs&list=PL_72ERGKF6DR4R0Cowx-LnnngLXRf4ZjB)

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# QueryVis (formerly QueryViz)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



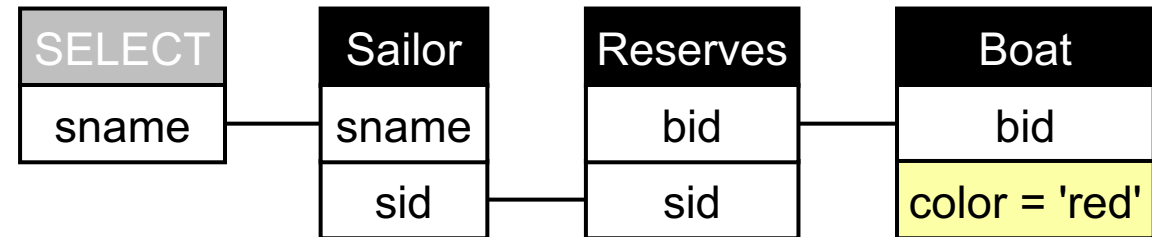
## TRC (Tuple Relational Calculus)

$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [q.sname = s.sname \wedge r.sid = s.sid \wedge b.bid = r.bid \wedge b.color = 'red']\}$

# QueryVis (formerly QueryViz)

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
where exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



QueryVis does not focus on the way the query is written but assumes the existential quantifiers pushed up as much as possible.

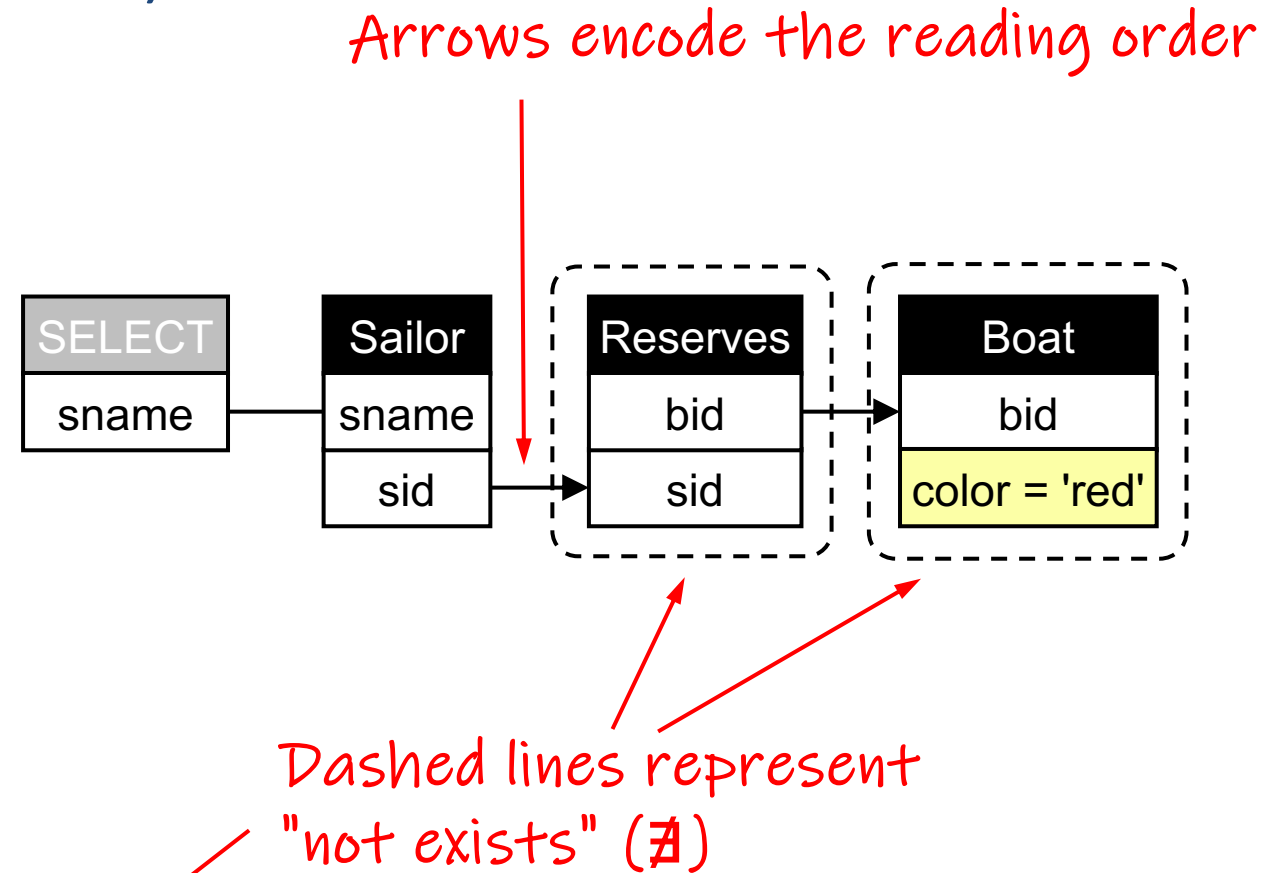
## TRC (Tuple Relational Calculus)

$\{q.sname \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [q.sname = s.sname \wedge r.sid = s.sid \wedge b.bid = r.bid \wedge b.color = 'red']\}$   
 $\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \exists r \in \text{Reserves} [r.sid = s.sid \wedge \exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = 'red']]]\}$

# QueryVis (formerly QueryViz)

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



## TRC (Tuple Relational Calculus)

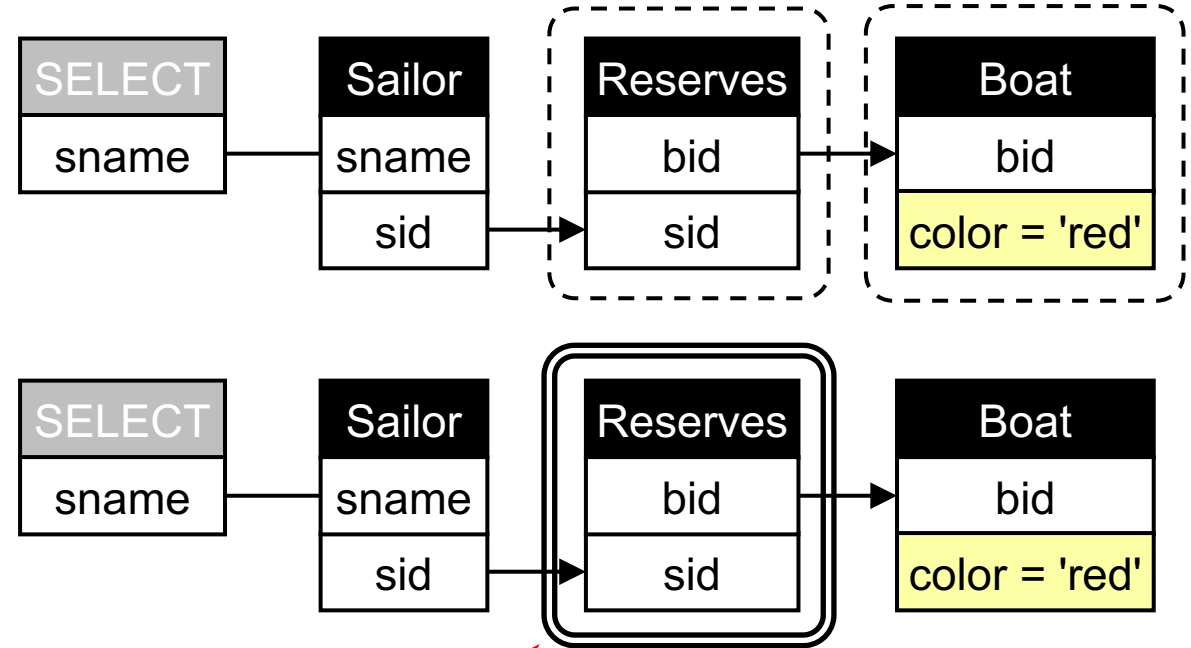
$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \neg (\exists r \in \text{Reserves} [r.sid = s.sid \wedge \neg (\exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = 'red'])])]\}$

# QueryVis (formerly QueryViz)

Q3: "Find sailors who reserved only red boats."

The theory of QueryVis (but not the online demo) allows a rewriting and replacing double negation with universal quantification

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



Double lines represent for all  $\forall$

## TRC (Tuple Relational Calculus)

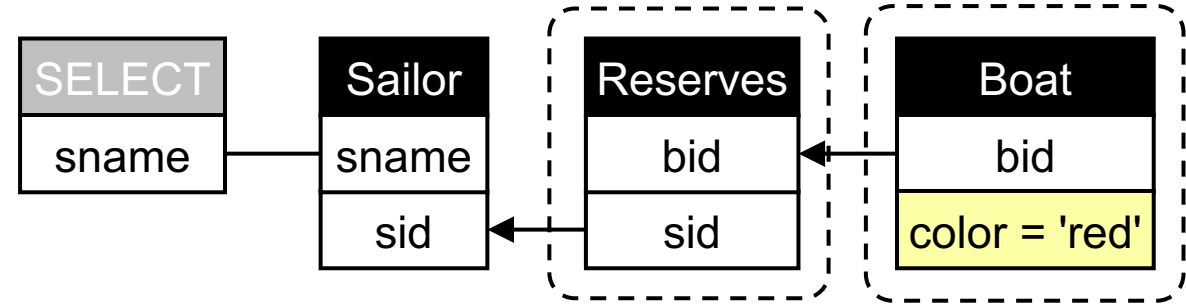
$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \neg(\exists r \in \text{Reserves} [r.sid = s.sid \wedge \neg(\exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = 'red'])])]\}$$
$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge (\forall r \in \text{Reserves} [r.sid = s.sid \rightarrow (\exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = 'red'])])]\}$$

# QueryVis (formerly QueryViz)

Q4: "Find sailors who reserved all red boats."

Correlated nested queries pose no problem.  
But notice the changed arrow direction!

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```



## TRC (Tuple Relational Calculus)

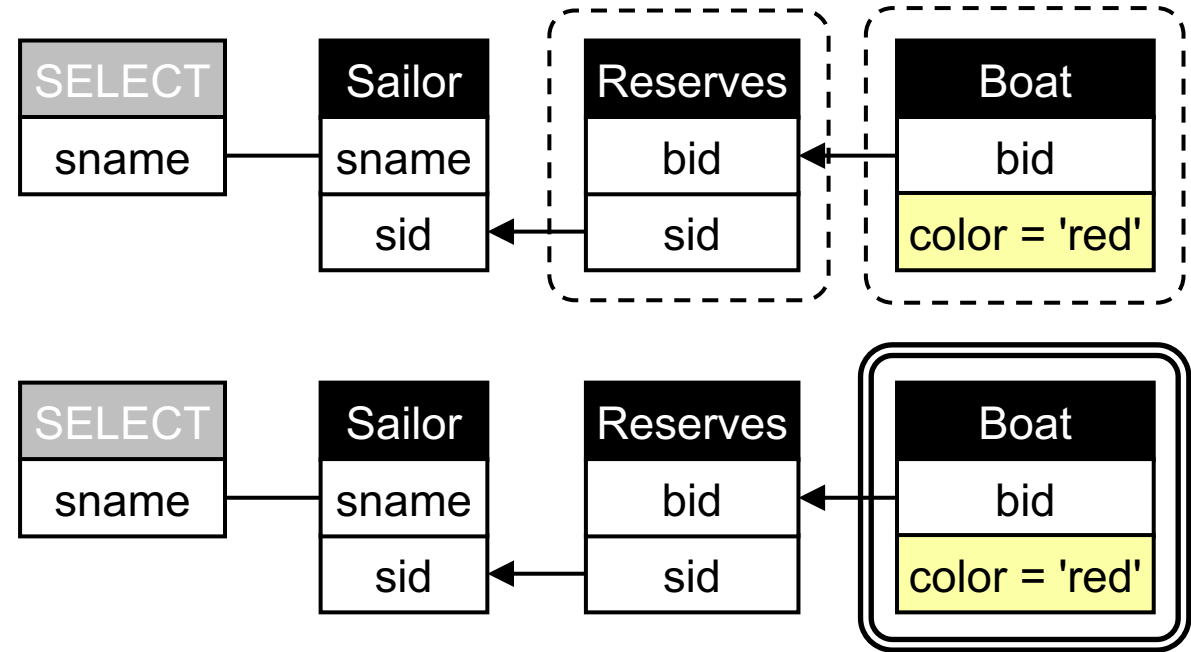
$\{q.sname \mid \exists s \in \text{Sailor}[q.sname = s.sname \wedge \neg(\exists b \in \text{Boat}[b.color = 'red' \wedge \neg(\exists r \in \text{Reserves}[b.bid = r.bid \wedge r.sid = s.sid])])]\}$



# QueryVis (formerly QueryViz)

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```



## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \neg (\exists b \in \text{Boat} [b.color = 'red' \wedge \neg (\exists r \in \text{Reserves} [b.bid = r.bid \wedge r.sid = s.sid])])]\}$$
$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge (\forall b \in \text{Boat} [b.color = 'red' \rightarrow (\exists r \in \text{Reserves} [b.bid = r.bid \wedge r.sid = s.sid])])]\}$$

Figure drawn based on "Danaparamita, Gatterbauer. QueryViz: Helping Users Understand SQL queries and their patterns. EDBT demo. 2011. <https://doi.org/10.1145/1951365.1951440>"  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# QueryVis (formerly QueryViz)

Q5: "Find boats  
that are red or blue."

```
select bid, bname  
from RedBoat R  
union  
select bid, bname  
from BlueBoat B
```

QueryVis does not support Union

Schema

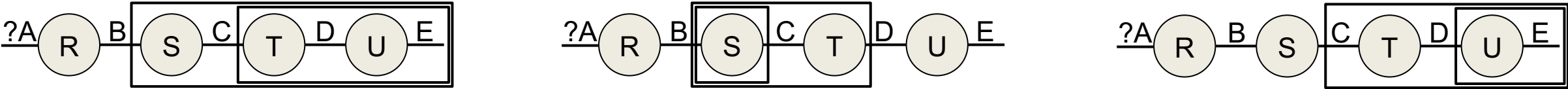
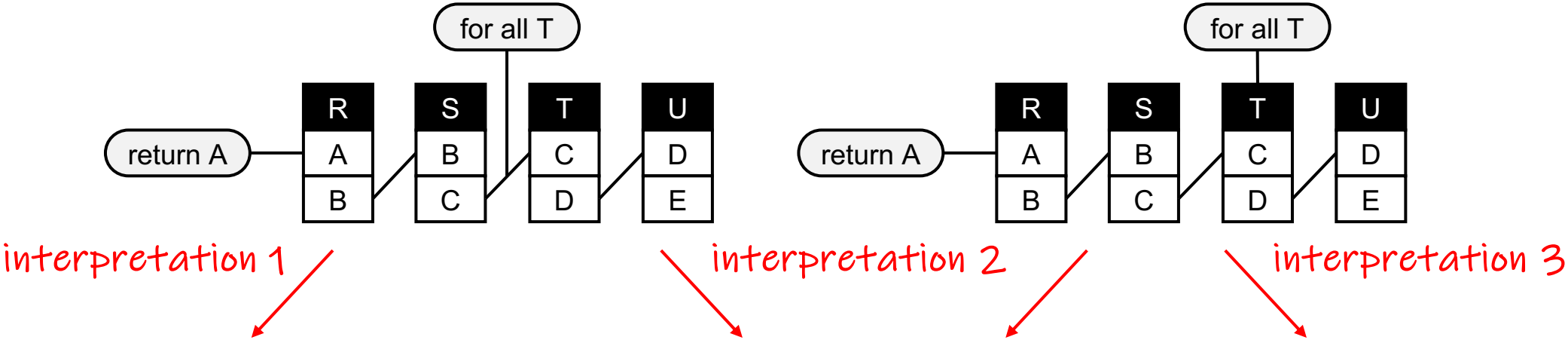
RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

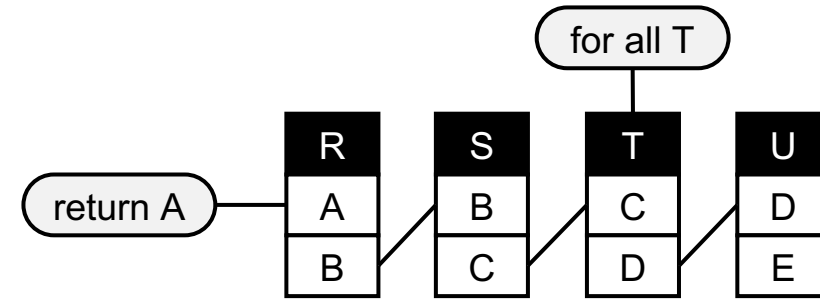
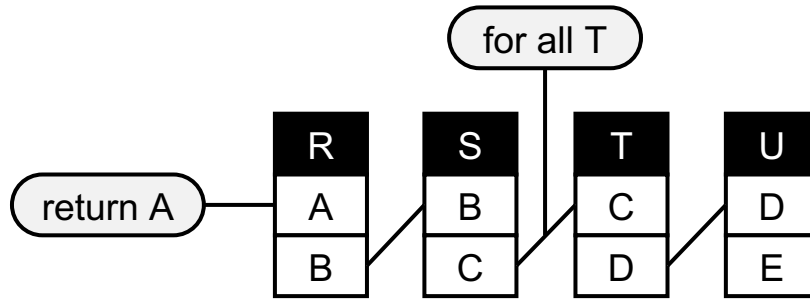
## TRC (Tuple Relational Calculus)

$$\{q(\text{bid}, \text{bname}) \mid \exists b \in \text{RedBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}] \\ \vee \exists b \in \text{BlueBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}]\}$$

# The quantifier example from OO-VQS is unambiguous



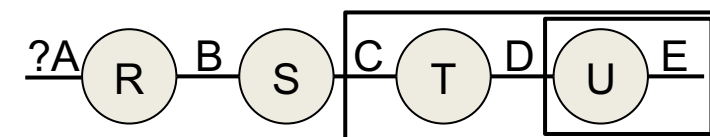
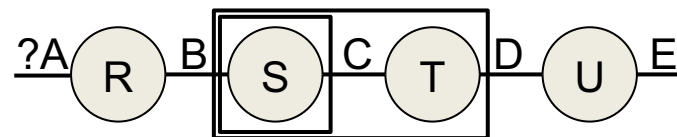
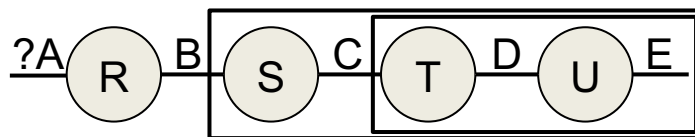
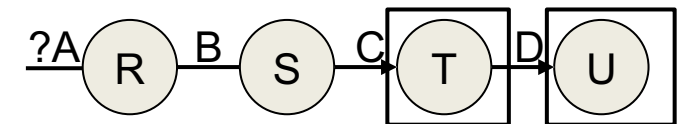
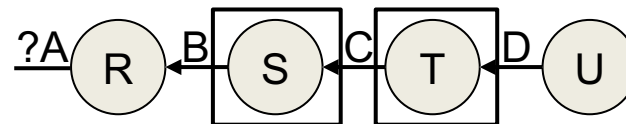
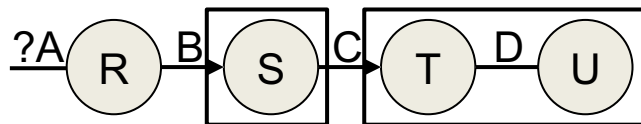
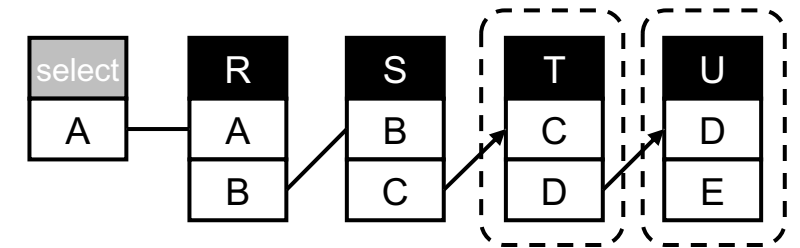
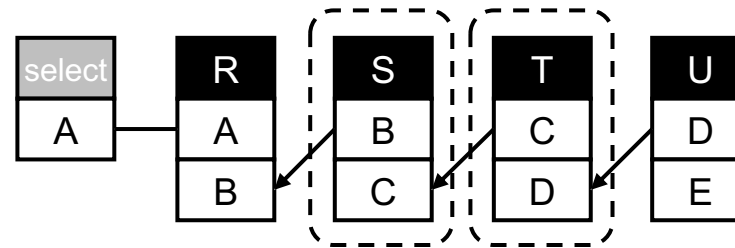
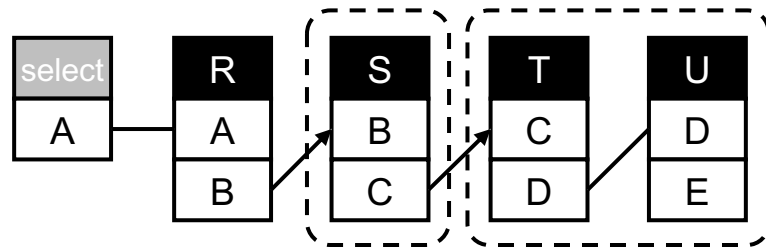
# The quantifier example from OO-VQS is unambiguous



interpretation 1

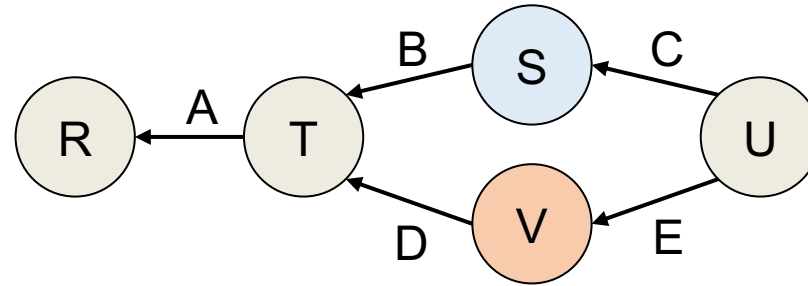
interpretation 2

interpretation 3

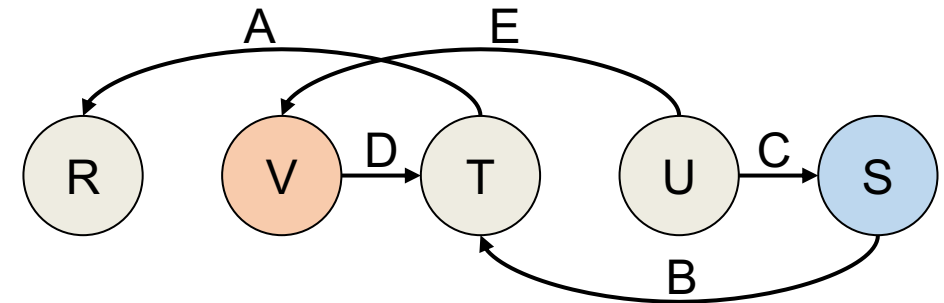
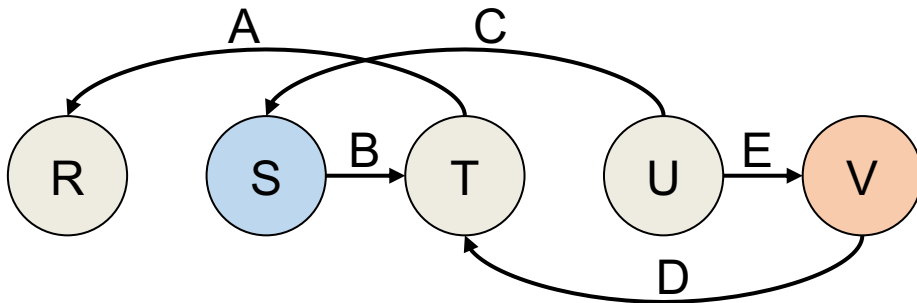


# With nesting depth 4, arrows can become ambiguous

One visualization:

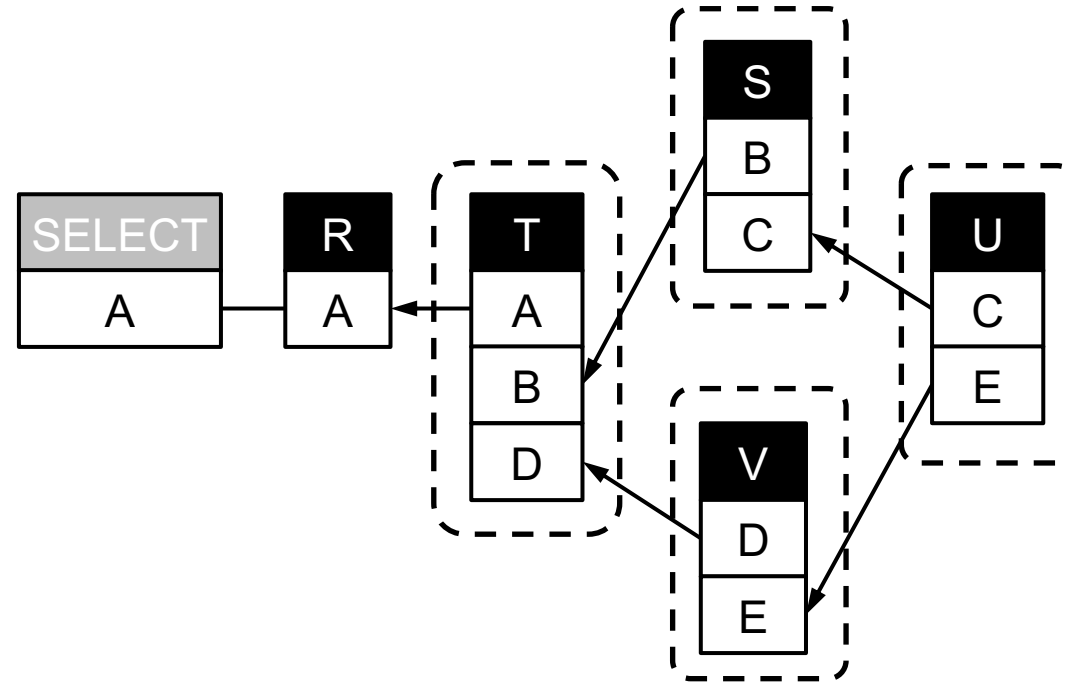


Two interpretations:

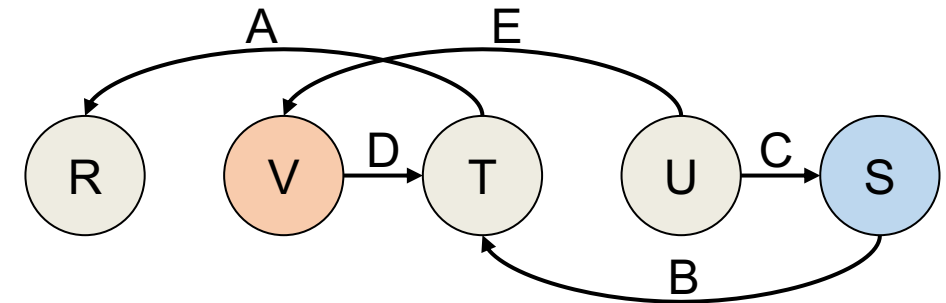
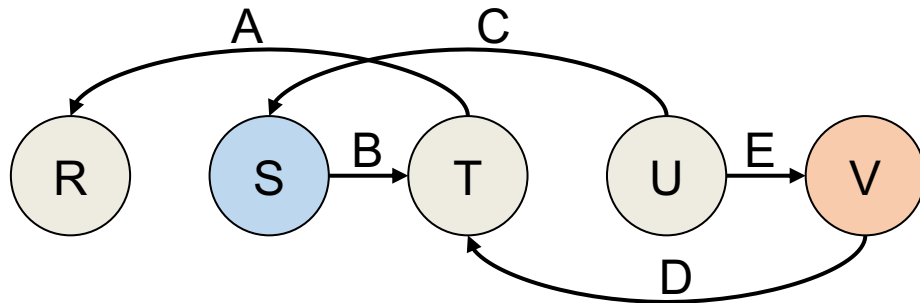


# With nesting depth 4, arrows can become ambiguous

```
select distinct A
from R
where not exists
  (select *
   from S
   where not exists
     (select *
      from T
      where T.A = R.A
        and T.B = S.B
        and not exists
          (select *
           from U
           where U.C = S.C
            and not exists
              (select *
               from V
               where V.D = T.D
                and V.E = U.E))))))
```



```
select distinct A
from R
where not exists
  (select *
   from V
   where not exists
     (select *
      from T
      where T.A = R.A
        and T.D = V.D
        and not exists
          (select *
           from U
           where U.E = V.E
            and not exists
              (select *
               from S
               where S.B = T.B
                and S.C = U.C))))))
```



# QueryVis (2011) (also QueryViz) Backup

# QueryVis (formerly known as QueryViz)

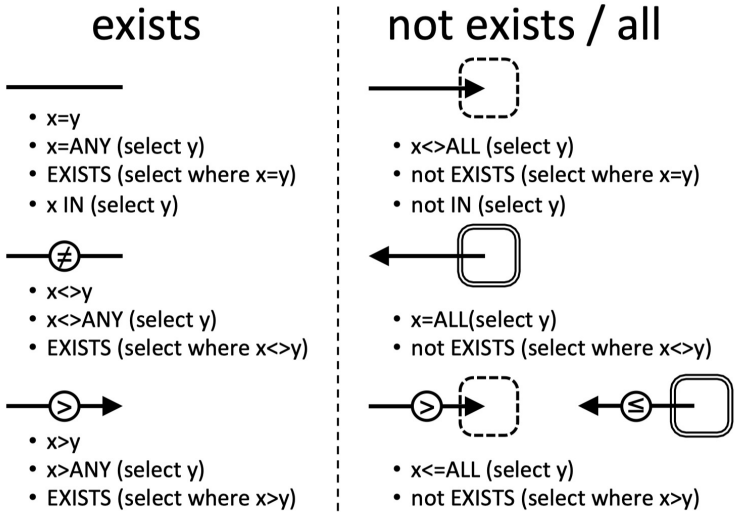


Figure 5: Lines with optional direction and comparison operators, together with bounding boxes in two line styles that group together relations suffice to express the most important syntactic constructs of nested SQL queries.

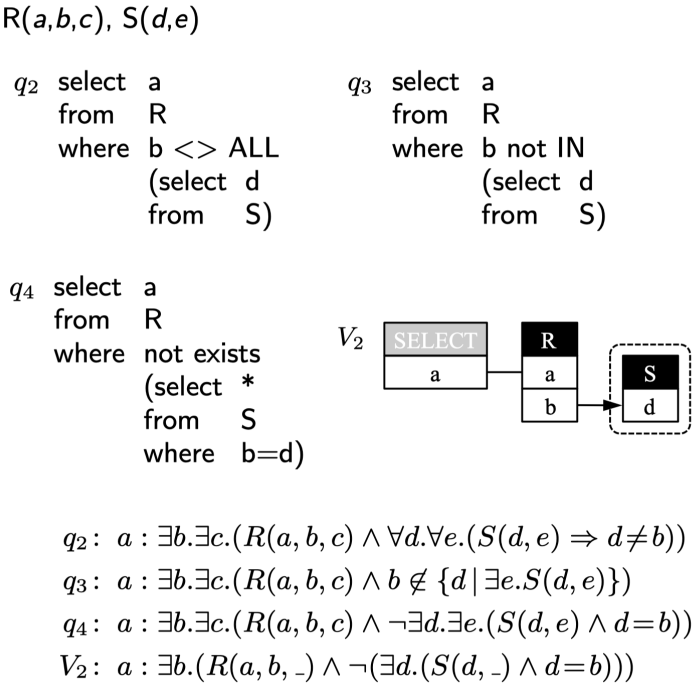


Figure 4: Schema with three equivalent queries ( $q_1$  to  $q_3$ ), their common QueryViz representation  $V_2$  and their respective translations into FOL.

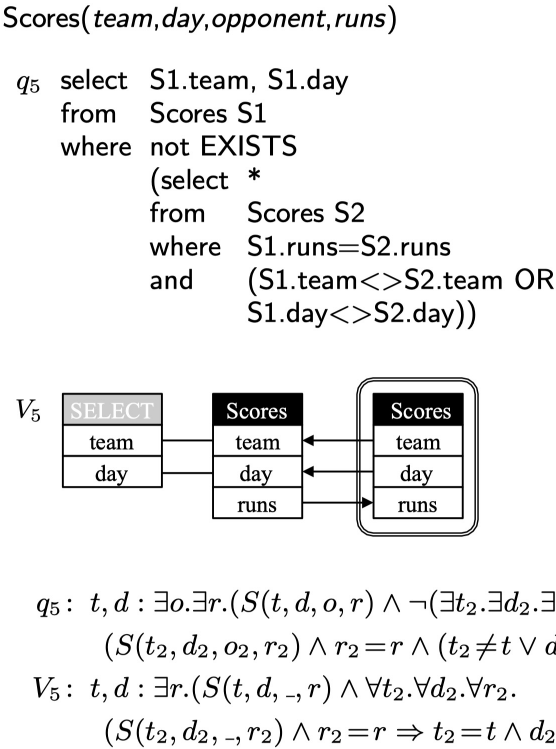


Figure 6: Query for “teams and days on which the team had a run that was neither repeated on another day nor by another team,” its QueryViz representation, and their respective translations into FOL.



# QueryVis (formerly known as QueryViz)

```
SELECT F.person
FROM   Frequents F, Likes L, Serves S
WHERE  F.person = L.person
AND    F.bar = S.bar
AND    L.drink = S.drink
```

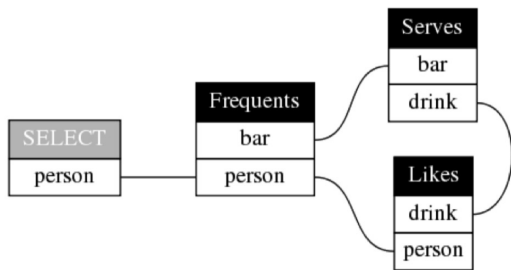


Figure 5: Visualizing a conjunctive query closely follows an all-familiar UML notation. *Q: Find persons who frequent some bar that serves some drink they like.* There is nothing really new here.

```
SELECT F.person
FROM   Frequents F
WHERE  not exists
      (SELECT *
       FROM   Serves S
       WHERE  S.bar = F.bar
       AND    not exists
            (SELECT L.drink
             FROM   Likes L
             WHERE  L.person = F.person
             AND    S.drink = L.drink))
```

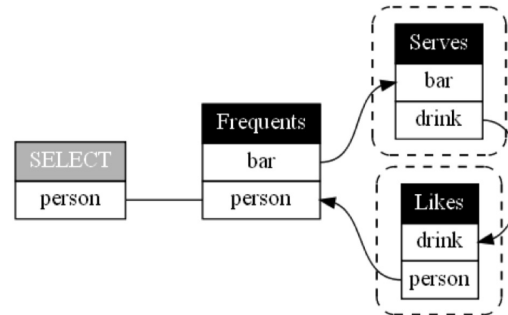


Figure 6: Visualizing a nested query still follows familiar UML notations, but now adds visual metaphors for  $\nexists$  (dashed box) and reading order (arrows). *Q: Find persons who frequent some bar that serves only drinks they like  $\equiv$  ... some bar that serves no drink that is not liked by them.*

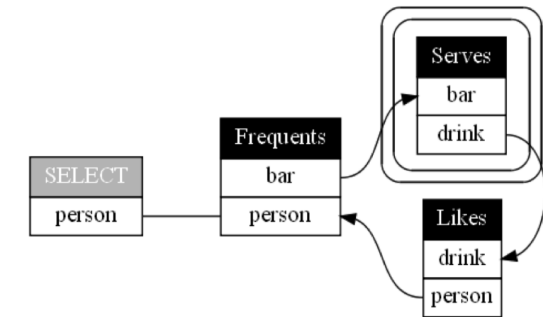
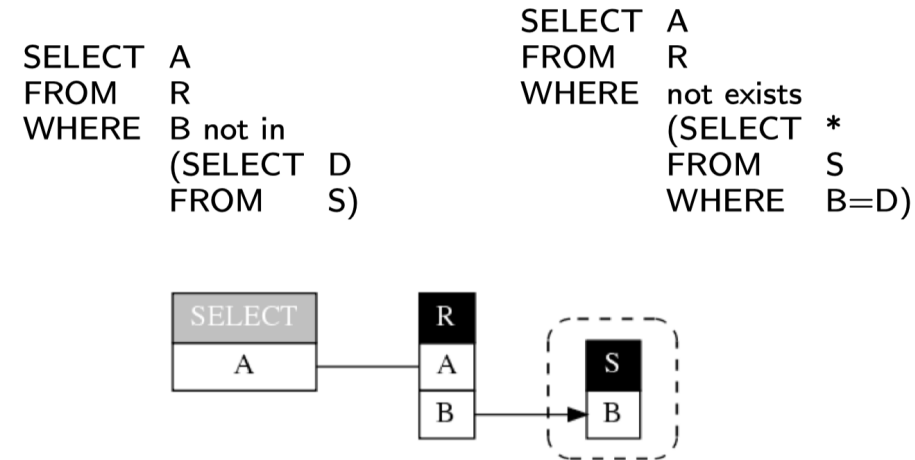


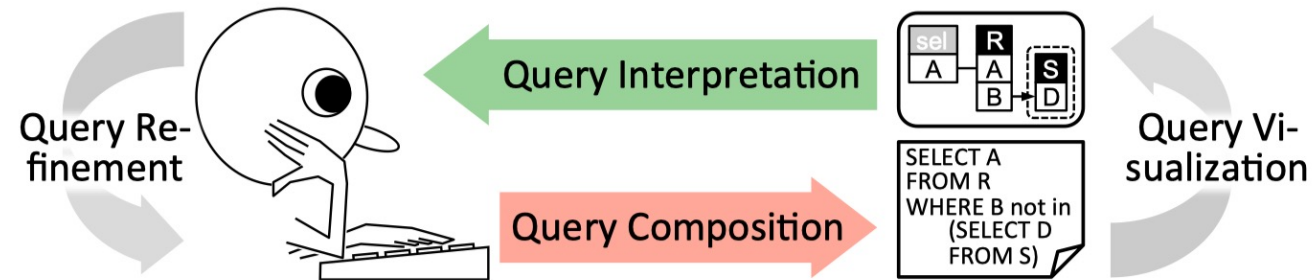
Figure 7: The visualization from **Fig. 6** can be further simplified by using another visual metaphor for  $\forall$  (double-lined box), a logical and intuitive operator that does not exist in SQL. *Q: Find persons who frequent some bar that serves only drinks they like  $\equiv$  ... some bar so that all drinks served are liked by them.*

# QueryVis (formerly known as QueryViz)



**Figure 4:** Two queries which are equivalent *except* if the column *S.b* contains NULL values. Ignoring this one case, they are equivalent. Hence, the *query intent* can be shown by the same representation.

# QueryVis (formerly known as QueryViz)



**Figure 8: The vision:** In the near future, *DBMSs will visualize queries too*, and not just data (as in information and scientific data visualization). This feature will allow iterative query refinement and will enhance the usability of databases.

# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

103 Bars: Persons who frequent some bar that serves some drink they like. ▾

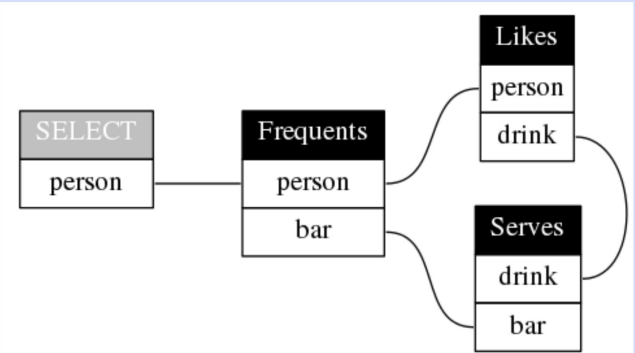
```
SELECT F.person
FROM   Frequents F, Likes L, Serves S
WHERE  F.person = L.person
AND    F.bar = S.bar
AND    L.drink = S.drink
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

111 Bars: Persons who frequent only bars that serve some drink they like. ▾

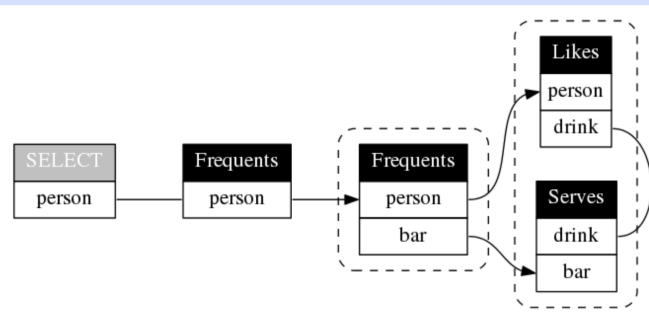
```
SELECT distinct F1.person
FROM   Frequents F1
WHERE  not exists
      (SELECT *
       FROM   Frequents F2
       WHERE  F2.person = F1.person
       AND    not exists
            (SELECT *
             FROM   Serves S3, Likes L4
             WHERE  S3.drink = L4.drink
             AND    S3.bar = F2.bar
             AND    L4.person = F2.person))
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

121 Bars: Persons who frequent some bar that serves only drinks they like. ▾

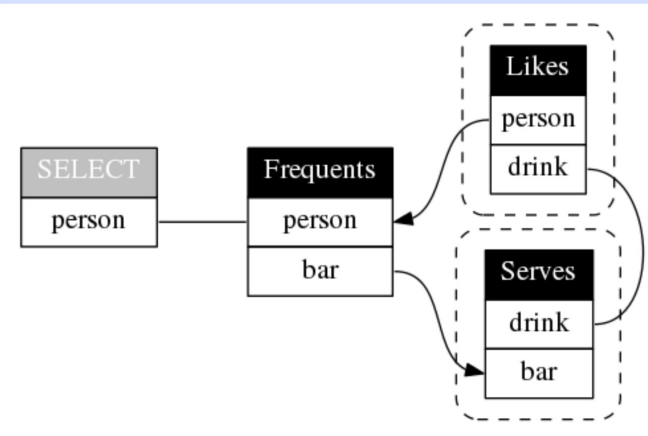
```
SELECT F.person
FROM   Frequents F
WHERE  not exists
      (SELECT *
       FROM   Serves S
       WHERE  S.bar = F.bar
       AND    not exists
            (SELECT L.drink
             FROM   Likes L
             WHERE  L.person = F.person
             AND    S.drink = L.drink))
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

131 Bars: Bars that serve a drink liked by Joe, but none liked by Michael.

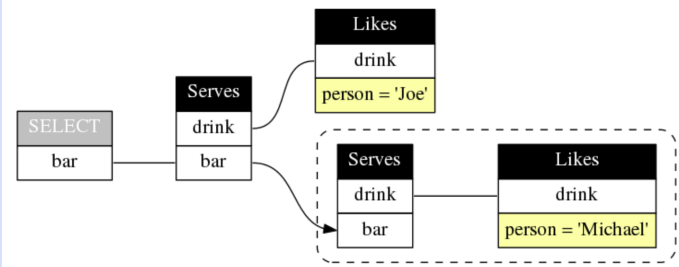
```
SELECT S.bar
FROM Serves S, Likes L
WHERE S.drink = L.drink
AND L.person = 'Joe'
AND not exists
      (SELECT S2.bar
       FROM Serves S2, Likes L2
       WHERE S2.drink = L2.drink
       AND L2.person = 'Michael'
       AND S.bar = S2.bar)
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

137 Bars: Persons who frequent bars with a drink < 3\$ and at least two with :

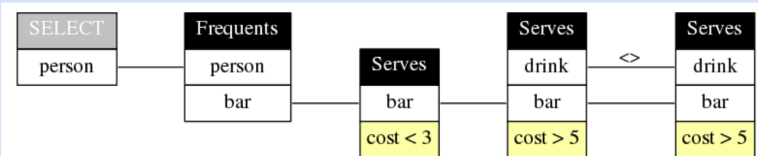
```
SELECT F.person
FROM Frequents F, Serves S
WHERE F.bar = S.bar
AND S.cost < 3
AND exists
      (SELECT S1.bar
       FROM Serves S1, Serves S2
       WHERE S1.bar = S2.bar
       AND S1.drink <> S2.drink
       AND S1.cost > 5
       AND S2.cost > 5
       AND S.bar = S1.bar)
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

136 Bars: Persons who frequent a bar with >= 2 beers they like, one <3\$ and <

```
SELECT F.person
FROM Frequents F, Serves S1, Serves S2, Likes L1, Likes L2
WHERE F.bar = S1.bar AND S1.bar = S2.bar
AND S1.drink = L1.drink AND S2.drink=L2.drink
AND S1.drink <> S2.drink AND S1.cost < 3 AND S2.cost > 5
AND F.person = L1.person AND F.person = L2.person
```

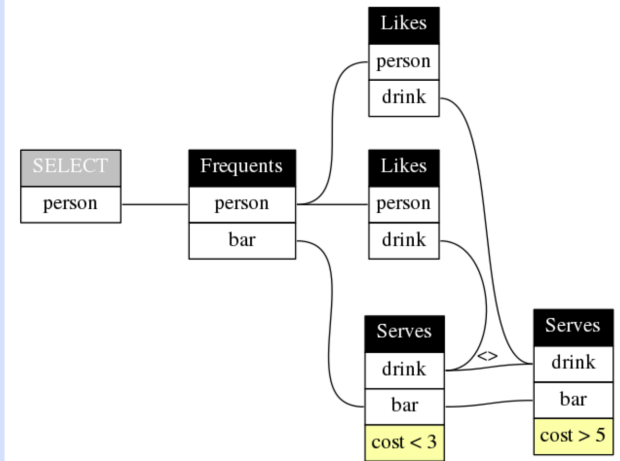
Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

160 Bars: Drinks that are the unique drinks liked by a person. ▾

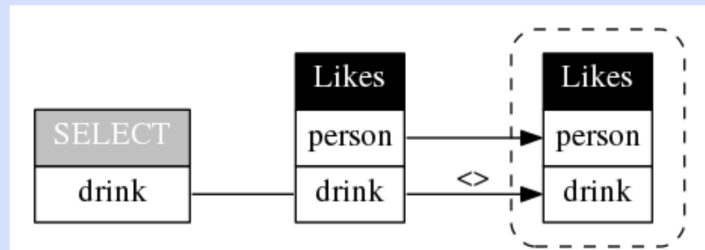
```
SELECT L.drink
FROM   Likes L
WHERE  not exists(
  SELECT *
  FROM   Likes L2
  WHERE  L2.person = L.person
  AND    L2.drink <> L.drink)
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Likes(person, drink)
Frequents(person, bar)
Serves(bar, drink, cost)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

161 Bars: Drinks that are the unique drinks liked by a person. ▾

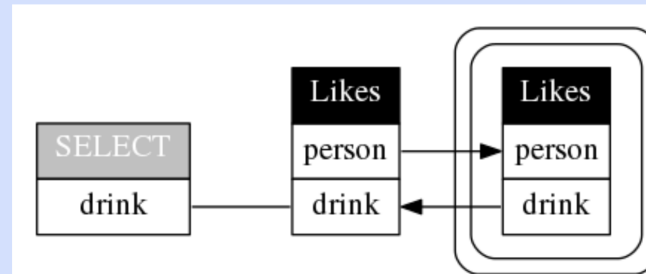
```
SELECT L.drink
FROM   Likes L
WHERE  L.drink = ALL (
  SELECT L2.drink
  FROM   Likes L2
  WHERE  L2.person = L.person)
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Online QueryVis

## SQL Query Visualization

Your Input

1. Specify a Schema

Actor(aid, fname, lname)  
Movie(id, name, year, rating)  
Casts(pid, mid, role)

2. Specify or choose a Query

Supported grammar

203 IMDB: Movies in which Kevin Bacon plays, together with all its actors.

```
SELECT  Movie.name, Actor.fname, Actor.lname
FROM    Actor, Movie, Casts c1, Casts c2, Actor bacon
WHERE   bacon.fname = 'Kevin'
AND     bacon.lname = 'Bacon'
AND     c2.pid = bacon.aid
AND     c1.mid = c2.mid
AND     Movie.id = c1.mid
AND     Actor.aid = c1.pid
```

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result

```
graph LR
    SELECT[SELECT] --- Movie[Movie]
    SELECT --- Actor1[Actor]
    Actor1 --- Casts1[Casts]
    Actor1 --- Casts2[Casts]
    Casts1 --- Actor2[Actor]
    Casts2 --- Actor2
    Actor2 --- aid[aid]
    Actor2 --- fname[fname]
    Actor2 --- lname[lname]
```

## SQL Query Visualization

Your Input

1. Specify a Schema

Actor(aid, fname, lname)  
Movie(id, name, year, rating)  
Casts(pid, mid, role)

2. Specify or choose a Query

Supported grammar

204 IMDB: Movies in which Kevin Bacon plays, together with all its actors.

```
SELECT  Movie.name, Actor.fname, Actor.lname
FROM    Actor, Movie, Casts c1, Casts c2
WHERE   c1.mid = c2.mid
AND     Movie.id = c1.mid
AND     Actor.aid = c1.pid
AND     exists
        (SELECT *
         FROM   Actor bacon
         WHERE  bacon.fname = 'Kevin'
         AND    bacon.lname = 'Bacon'
         AND    c2.pid = bacon.aid)
```

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result

```
graph LR
    SELECT[SELECT] --- Movie[Movie]
    SELECT --- Actor1[Actor]
    Actor1 --- Casts1[Casts]
    Actor1 --- Casts2[Casts]
    Casts1 --- Actor2[Actor]
    Casts2 --- Actor2
    Actor2 --- aid[aid]
    Actor2 --- fname[fname]
    Actor2 --- lname[lname]
```

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

345



# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Actor(aid, fname, lname)
Movie(id, name, year, rating)
Casts(pid, mid, role)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

205 IMDB: Actors with Kevin Bacon number 1.

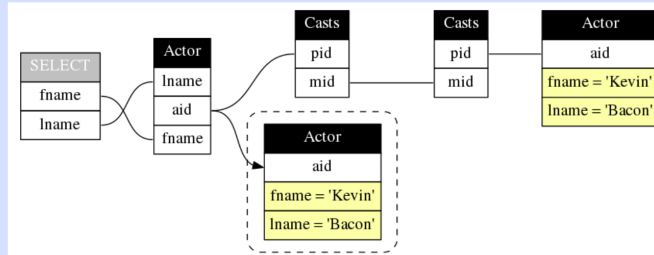
```
SELECT Actor.fname, Actor.lname
FROM Actor, Casts c1, Casts c2, Actor bacon
WHERE c1.mid = c2.mid
AND Actor.aid = c1.pid
AND bacon.fname = 'Kevin'
AND bacon.lname = 'Bacon'
AND c2.pid = bacon.aid
AND not exists
(SELECT *
FROM Actor nonbacon
WHERE nonbacon.fname = 'Kevin'
AND nonbacon.lname = 'Bacon'
AND Actor.aid = nonbacon.aid)
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryVis Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Actor(aid, fname, lname)
Movie(id, name, year, rating)
Casts(pid, mid, role)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

206 IMDB: Actors with Kevin Bacon number 2.

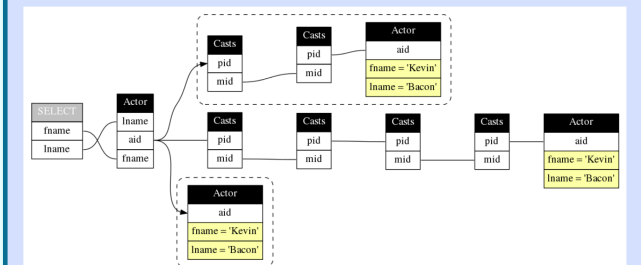
```
SELECT distinct a3.fname, a3.lname
FROM Actor a0, Casts c0, Casts c1, Casts c2, Casts c3, Actor a3
WHERE a0.fname = 'Kevin'
AND a0.lname = 'Bacon'
AND c0.pid = a0.aid
AND c0.mid = c1.mid
AND c1.pid = c2.pid
AND c2.mid = c3.mid
AND c3.pid = a3.aid
AND not exists
(SELECT *
FROM Actor xa0, Casts xc0, Casts xc1
WHERE xa0.fname = 'Kevin'
AND xa0.lname = 'Bacon'
AND xa0.aid = xc0.pid
AND xc0.mid = xc1.mid
AND xc1.pid = a3.aid)
AND not exists
(SELECT *
FROM Actor ya0
WHERE ya0.fname = 'Kevin'
AND ya0.lname = 'Bacon'
AND ya0.aid = a3.aid)
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryVis Result





# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Sailors(sid, sname, rating, age)
Boats(bid, bname, color)
Reserves(sid, bid, day)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

301 Sailors: Sailors who have reserved all boats.

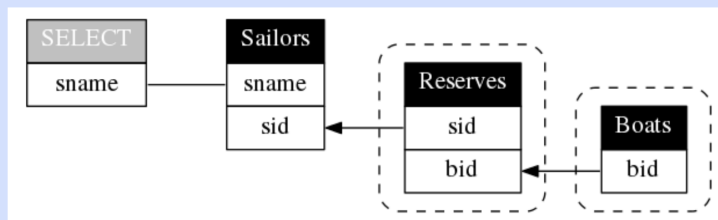
```
SELECT S.sname
FROM   Sailors S
WHERE  not exists
      (SELECT B.bid
       FROM   Boats B
       WHERE  not exists
            (SELECT R.bid
             FROM   Reserves R
             WHERE R.bid = B.bid
             AND   R.sid = S.sid))
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Sailors(sid, sname, rating, age)
Boats(bid, bname, color)
Reserves(sid, bid, day)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

302 Sailors: Sailors who have reserved all red boats.

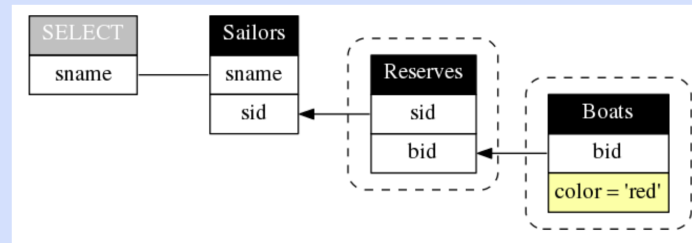
```
SELECT S.sname
FROM   Sailors S
WHERE  not exists
      (SELECT B.bid
       FROM   Boats B
       WHERE B.color = 'red'
       AND   not exists
            (SELECT R.bid
             FROM   Reserves R
             WHERE R.bid = B.bid
             AND   R.sid = S.sid))
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

```
Sailors(sid, sname, rating, age)
Boats(bid, bname, color)
Reserves(sid, bid, day)
```

#### 2. Specify or choose a Query

[Supported grammar](#)

303 Sailors: Sailors who have not reserved a red boats.

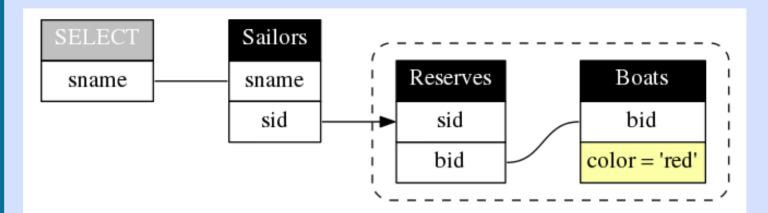
```
SELECT S.sname
FROM   Sailors S
WHERE  not exists
      (SELECT *
       FROM   Boats B, Reserves R
       WHERE  R.bid = B.bid
       AND    B.color = 'red'
       AND    R.sid = S.sid)
```

[Submit](#) [Reset](#)

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Online QueryVis

## SQL Query Visualization

Your Input

1. Specify a Schema

Worlds(wid, tid)

2. Specify or choose a Query

[Supported grammar](#)

401 Worlds: Worlds where each tuple is already contained in some earlier wc ▾

```
SELECT W1.wid
FROM   Worlds W1
WHERE  not exists
      (SELECT W2.tid
       FROM   Worlds W2
       WHERE  W2.wid = W1.wid
       AND    not exists
            (SELECT W3.wid
             FROM   Worlds W3
             WHERE  W3.tid = W2.tid
             and    W3.wid < W2.wid))
```

SubmitReset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

```
graph LR
    S[SELECT wid] --> W1[Worlds wid]
    W1 --> J1[Worlds wid, tid]
    J1 --> J2[Worlds wid, tid]
    J1 --> J2
```

## SQL Query Visualization

Your Input

1. Specify a Schema

Worlds(wid, tid)

2. Specify or choose a Query

[Supported grammar](#)

451 Worlds: Worlds with a tuple that does not appear in a later world. ▾

```
SELECT W1.wid
FROM   Worlds W1
WHERE  W1.wid >= all
      (SELECT W2.wid
       FROM   Worlds W2
       WHERE  W2.tid = W1.tid)
```

SubmitReset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

```
graph LR
    S[SELECT wid] --> W1[Worlds wid, tid]
    W1 --> J1[Worlds wid, tid]
    J1 --> J2[Worlds wid, tid]
    J1 --> J2
```

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

348

# Online QueryVis

## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

Worlds(wid, tid)

#### 2. Specify or choose a Query

[Supported grammar](#)

411 Worlds: Worlds for which there exists one other, earlier world that contain

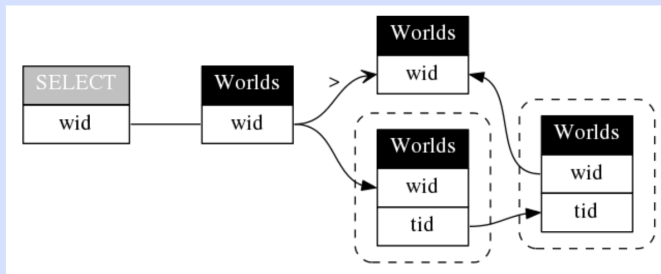
```
SELECT W1.wid
FROM   Worlds W1, Worlds W2
WHERE  W1.wid > W2.wid
AND    not exists
      (SELECT *
       FROM   Worlds W3
       WHERE  W3.wid = W1.wid
       AND    not exists
            (SELECT *
             FROM   Worlds W4
             WHERE  W4.wid = W2.wid
             AND    W4.tid = W3.tid))
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

Worlds(wid, tid)

#### 2. Specify or choose a Query

[Supported grammar](#)

412 Worlds: Worlds for which there is no earlier world that contains all its tu

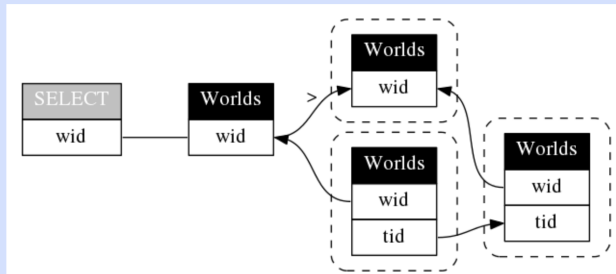
```
select W1.wid
from   Worlds W1
where  not exists
      (select *
       from   Worlds W2
       where  W2.wid < W1.wid
       and    not exists
            (select *
             from   Worlds W3
             where  W3.wid = W1.wid
             and    not exists
                  (select *
                   from   Worlds W4
                   where  W4.wid = W2.wid
                   and    W4.tid = W3.tid)))
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

### Your Input

#### 1. Specify a Schema

Worlds(wid, tid)

#### 2. Specify or choose a Query

[Supported grammar](#)

416 Worlds: Worlds for which there is no earlier world with exactly the same

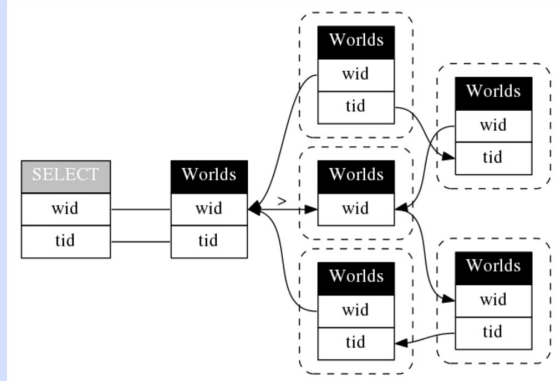
```
select W1.*
from   Worlds W1
where  not exists
      (select W2.wid
       from   Worlds W2
       where  W2.wid < W1.wid
       and    not exists
            (select W3.tid
             from   Worlds W3
             where  W3.wid = W1.wid
             and    not exists
                  (select *
                   from   Worlds W4
                   where  W4.wid = W2.wid
                   and    W4.tid = W3.tid)))
and    not exists
      (select W5.tid
       from   Worlds W5
       where  W5.wid = W2.wid
       and    not exists
            (select *
             from   Worlds W6
             where  W6.wid = W1.wid
             and    W6.tid = W5.tid)))
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Online QueryVis

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

503 Abstract: Attribute comparisons.

SELECT R.A  
FROM R  
WHERE not exists  
      (SELECT \*  
      FROM S  
      WHERE R.A < S.A  
      AND S.B < S.A  
      AND S.C < 10)

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

S

A

B

C < 10

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

511 Abstract: Multiple conjunctive selections on predicates.

SELECT R.A  
FROM R,S  
WHERE R.A > 2  
AND R.A < 10  
AND S.A = 3  
AND R.A = S.A

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

A > 2

A < 10

S

A

A = 3

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

551 Abstract: R.A with R.B biggest among all R.Bs.

SELECT R.A  
FROM R  
WHERE R.B > ALL  
      (SELECT R2.B  
      FROM R as R2)

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

B

R

B

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

350

# Online QueryVis

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

562 Abstract: R.A where R.B is different from at least one S.B.

SELECT R.A  
FROM R  
WHERE exists  
(SELECT \*  
FROM S  
WHERE R.B <> S.B)

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

B

S

B

<>

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

571 Abstract: R.A so that R.B is different from all S.B.

SELECT R.A  
FROM R  
WHERE R.B <> ALL  
(SELECT S.B  
FROM S)

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

B

S

B

<>

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

573 Abstract: R.A for which R.B is not in S.B.

SELECT R.A  
FROM R  
WHERE not exists  
(SELECT S.B  
FROM S  
WHERE S.B = R.B)

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

R

A

B

S

B

=

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

351

# Online QueryVis

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

505 Abstract: Attribute comparisons inside a component.

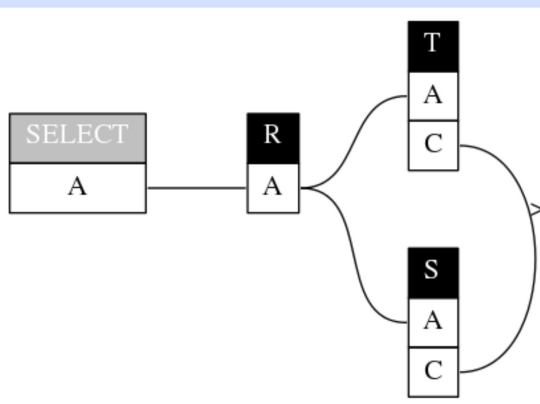
SELECT R.A  
FROM R, S, T  
WHERE R.A = S.A  
AND S.C > T.C  
And R.A = T.A

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result



### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

507 Abstract: Attribute comparisons inside a component.

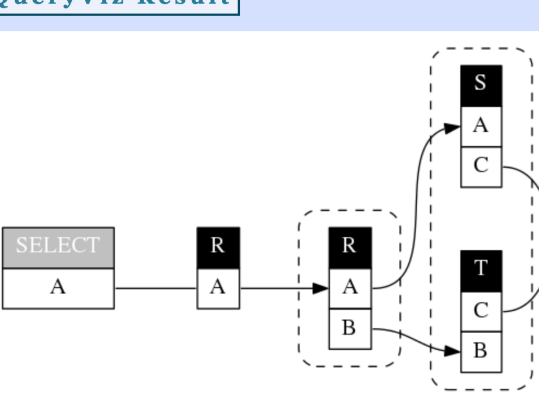
SELECT R.A  
FROM R  
WHERE not exists  
(SELECT \*  
FROM R R2  
WHERE R2.A = R.A  
AND not exists  
(SELECT \*  
FROM S, T  
WHERE T.C > S.C  
AND R2.A = S.A  
AND R2.B = T.B))

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result



### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

508 Abstract: Attribute comparisons between components.

SELECT R.A  
FROM R  
WHERE not exists  
(SELECT \*  
FROM S  
WHERE S.A = R.A  
AND not exists  
(SELECT \*  
FROM T  
WHERE S.C > T.C  
AND R.B = T.B))

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

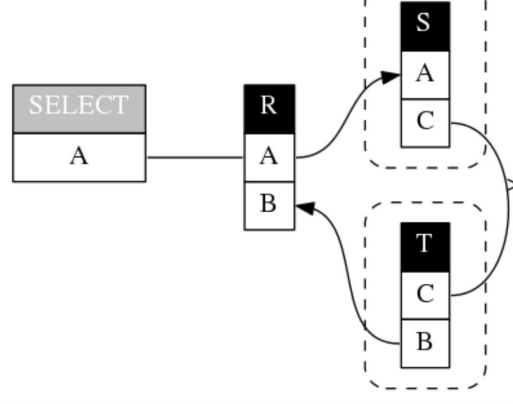


Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

352

# Online QueryVis

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

(clean)

select A, count(\*)  
from R  
group by A, B

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

COUNT(\*)

R

A

B

COUNT(\*)

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

(clean)

select A, count(\*)  
from R  
group by A, B  
having avg(C)>10

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

COUNT(\*)

R

A

B

COUNT(\*)

AVG(C) > 10

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

(clean)

select A, count(\*)  
from R  
group by A, B  
having count(\*)>10

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

COUNT(\*)

R

A

B

COUNT(\*)

COUNT(\*) > 10

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

353

# Online QueryVis

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

(clean)

```
select R.A, min(R.C)  
from R, S  
where R.C = S.C  
group by R.A, R.B  
having avg(R.C)>10
```

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

MIN(C)

R

A

C

B

MIN(C)

AVG(C) > 10

S

C

### SQL Query Visualization

Your Input

1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

2. Specify or choose a Query

Supported grammar

(clean)

```
select R.A, count(*)  
from R, S  
where R.C = S.C  
group by R.A, R.B  
having avg(R.C)>10
```

Submit

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

QueryViz Result

SELECT

A

COUNT(\*)

R

A

C

B

AVG(C) > 10

COUNT(\*)

S

C

Figure source: Online QueryVis (formerly known as Online QueryViz): <http://demo.queryvis.com>  
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

354



# Online QueryVis

# SQL Query Visualization

## Your Input

## 1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

## 2. Specify or choose a Query

## Supported grammar

(clean)

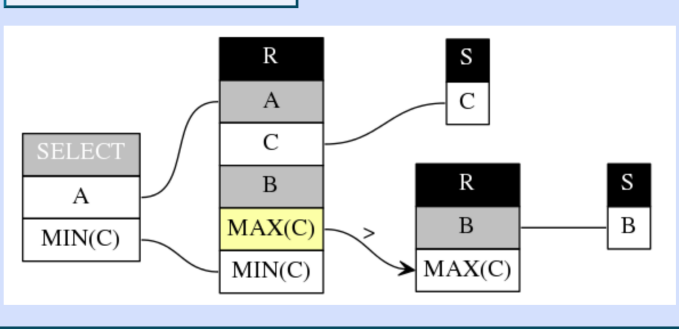
```
select R.A, min(R.C)
from R, S
where R.C = S.C
group by R.A, R.B
having max(R.C)>
(select max(R.C)
from R,S
where R.B=S.B
group by R.B)
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

**Image loaded.**

## QueryViz Result



## SQL Query Visualization

## Your Input

## 1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

## 2. Specify or choose a Query

### Supported grammar

(clean)

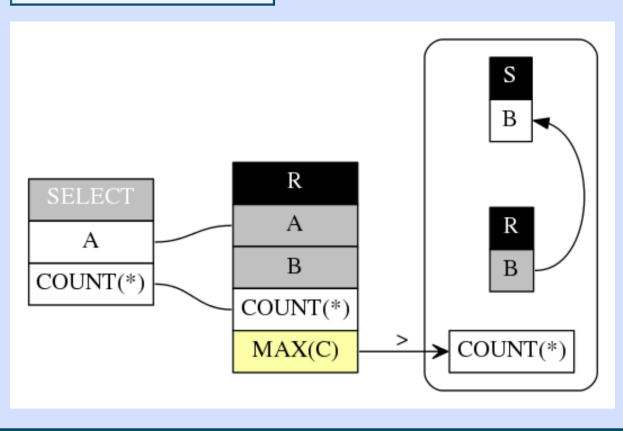
```
select R.A, count(*)
from R
group by R.A, R.B
having max(R.C)>
(select count(*)
from R,S
where R.B=S.B
group by R.B)
```

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



## SQL Query Visualization

## Your Input

## 1. Specify a Schema

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

## 2. Specify or choose a Query

### Supported grammar

(clean)

```
select R.A, count(*)
from R, S
where R.C = S.C
group by R.A, R.B
having max(R.C)>
(select count(*)
from R,S
where R.B=S.B
group by R.B)
```

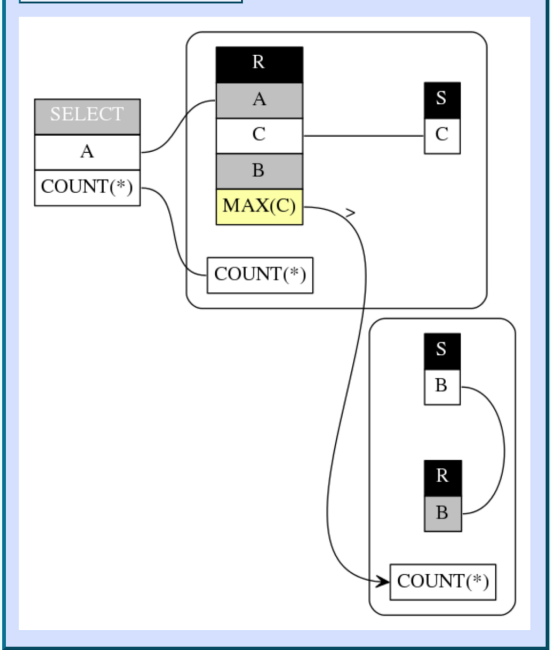
Submit Reset

Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result



# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# Dataplay (2012)

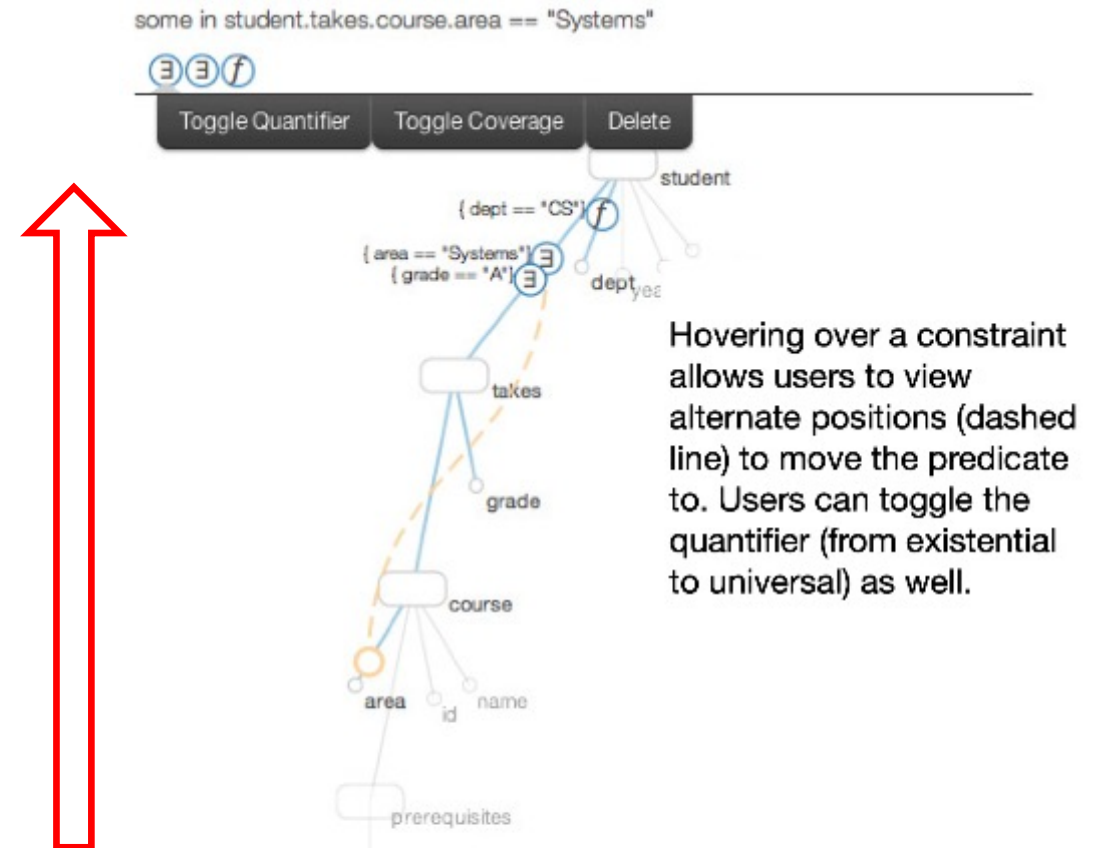
## Sources used:

- Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>
- Abouzied, Hellerstein, Silberschatz. Playful Query Specification with DataPlay. VLDB demo 2012. <https://doi.org/10.14778/2367502.2367542>
- Abouzied, DataPlay Tutorial, 2012. <https://vimeo.com/45918228>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay

- Dataplay allows users to interactively explore data starting from ERD-inspired tree representation of the database schema (similar in spirit to OO-VQL [Mohan, Kashyap'93])
- Goal is a representation that doesn't change too much with regard to simple syntactic changes like "find sailors who reserved a red boat" vs. "only red boats"
- Example of a system where the navigation path is implicitly expressed by transforming the query schema into a tree and tables appear in the selected order.
- The visualization is interpreted bottom-up
- Shows the query, and also the results
- Our focus here is on the visual abstractions and some of the advanced interactions and innovations (like hovering, brushing) are not reflected in the visualization

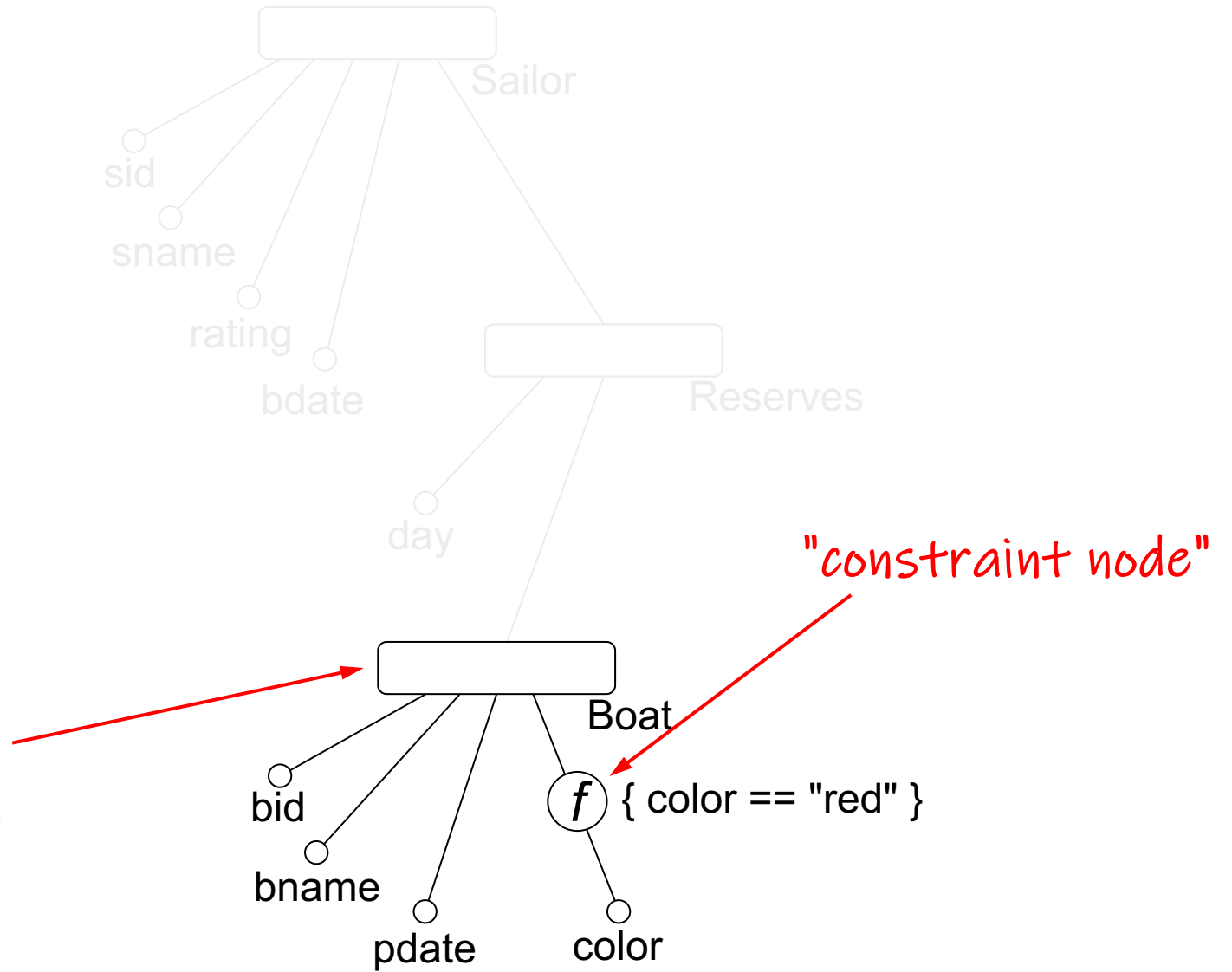


# DataPlay

Q1b: "Find boats  
that are not red."

```
select distinct bname  
from Boat  
where color = 'red'
```

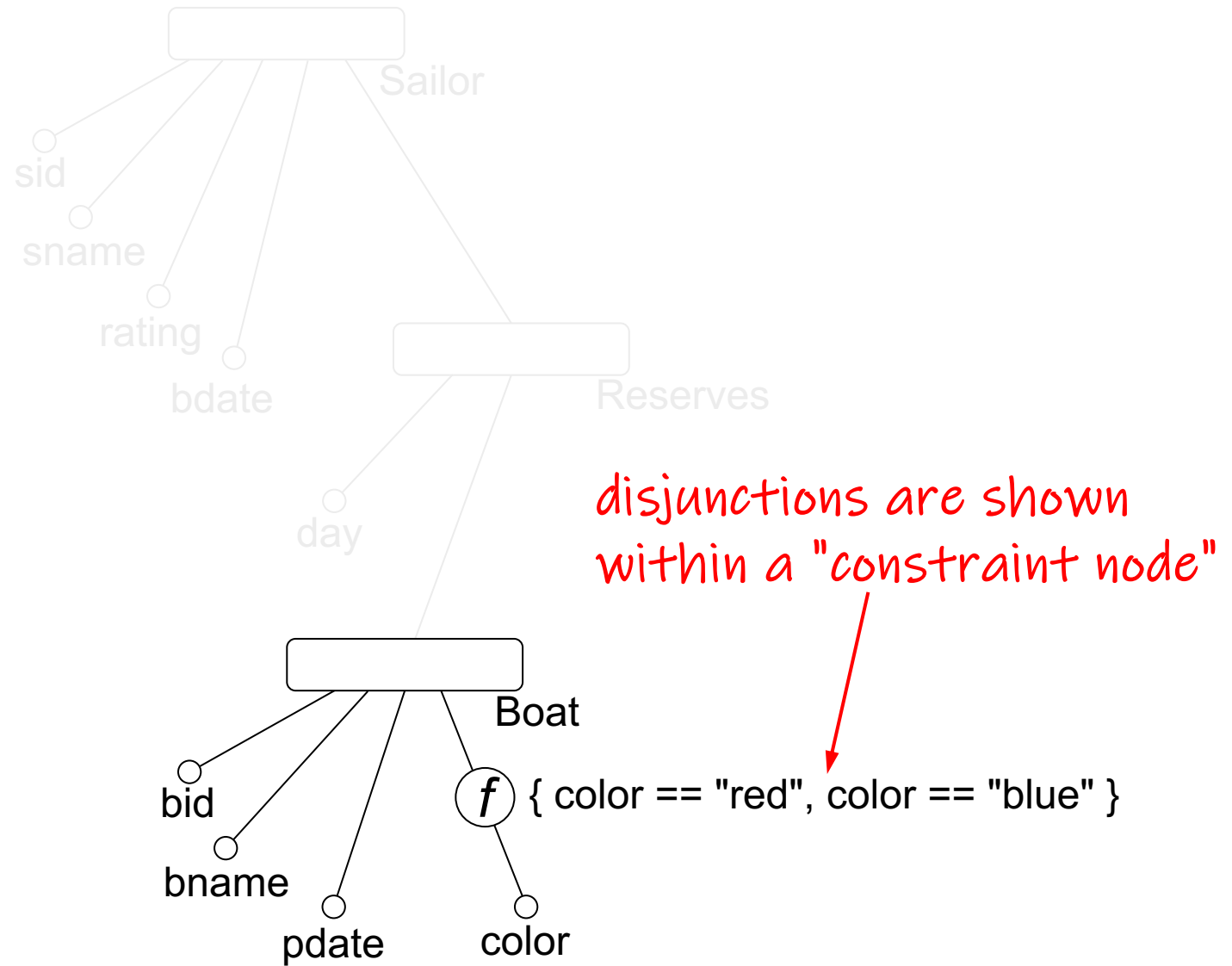
It has no visual  
symbol for selection



# Dataplay

Q1: "Find boats  
that are red or blue."

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```

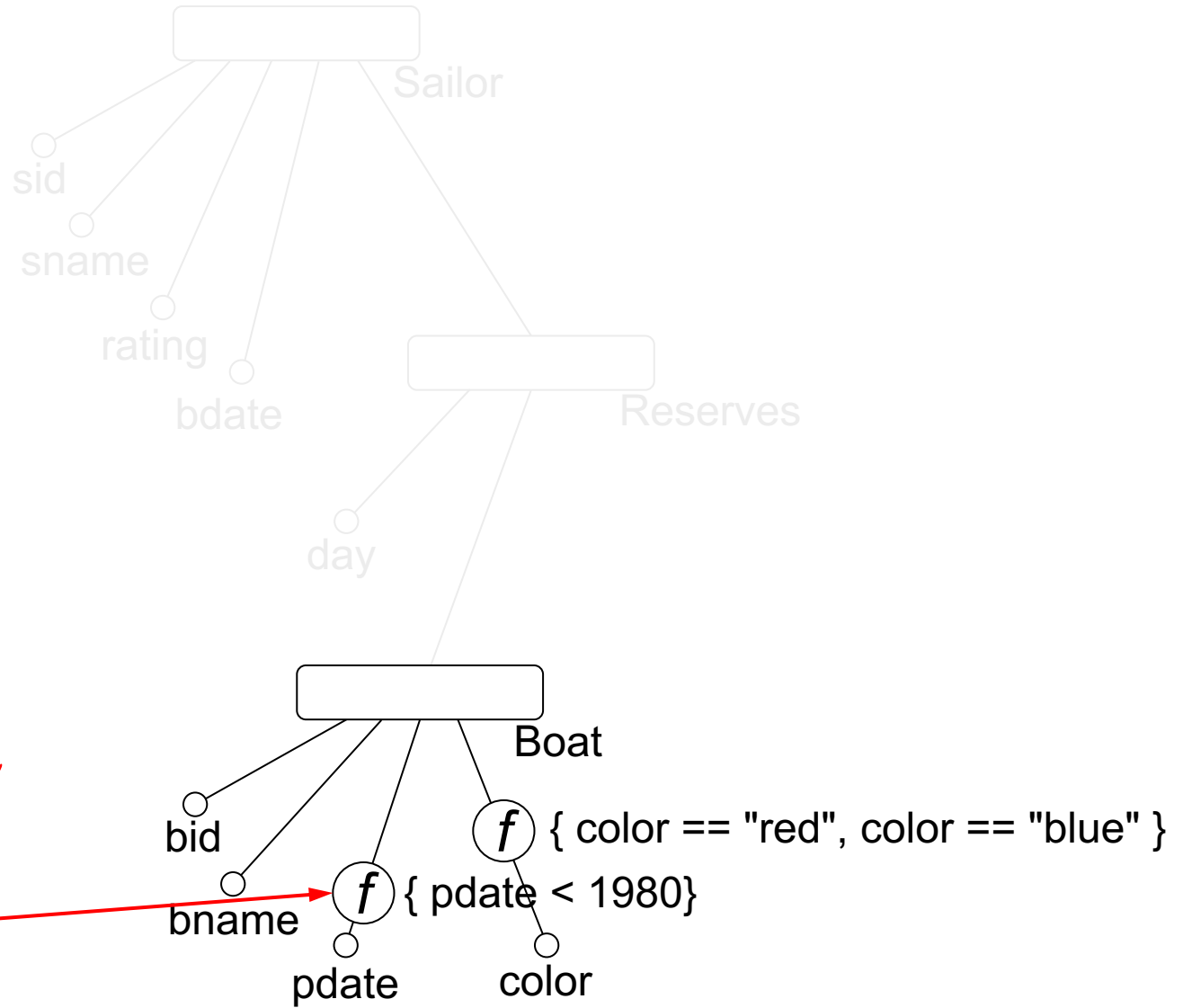


# Dataplay

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Conditions on separate attributes can be applied on each attribute separately.  
Not clear how to express disjunctions \*across\* attributes, such as: \_\_\_\_\_  
(color = 'red' or pdate < 1980)

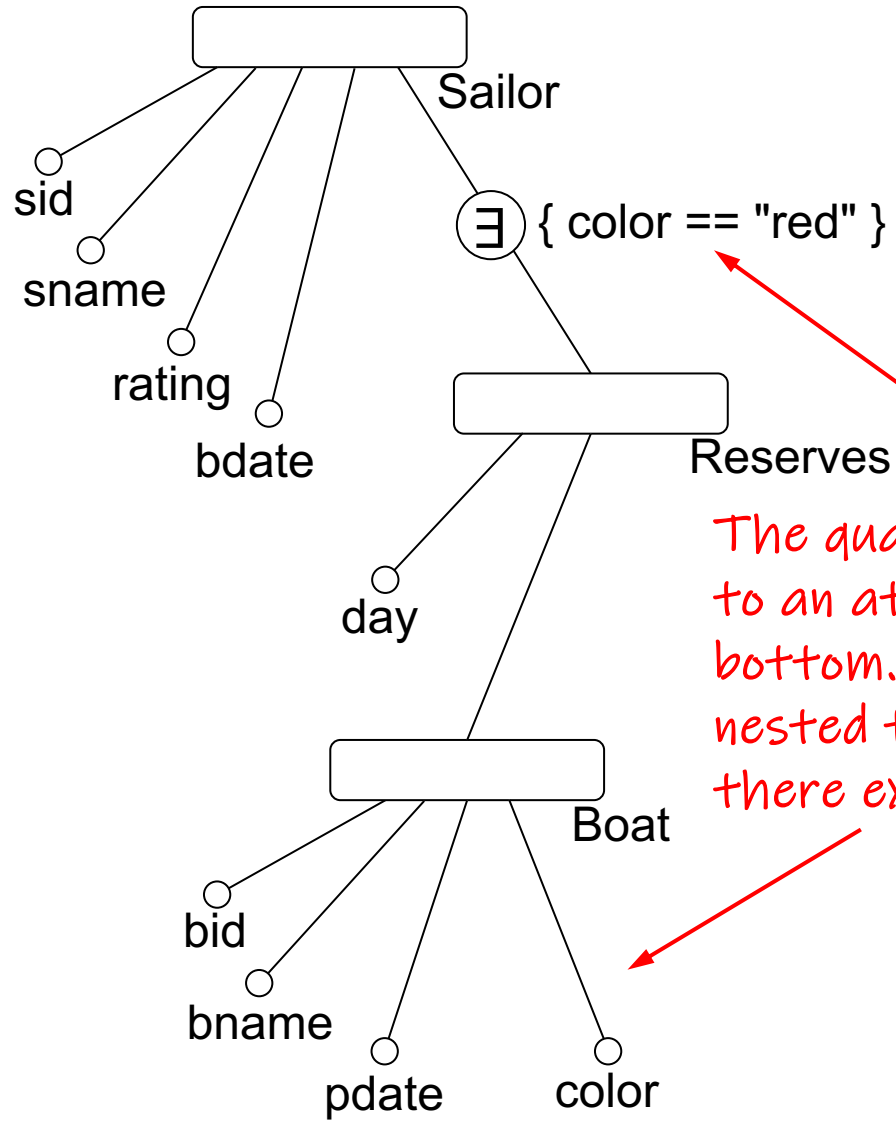


# Dataplay

*Q2: "Find sailors who reserved a red boat."*

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

The query tree can be interpreted as an evaluation tree but now bottom-up



The quantifier on top refers to an attribute at the bottom. It is read as: in the nested tuples for a sailor, there exists a red boat

## TRC (Tuple Relational Calculus)

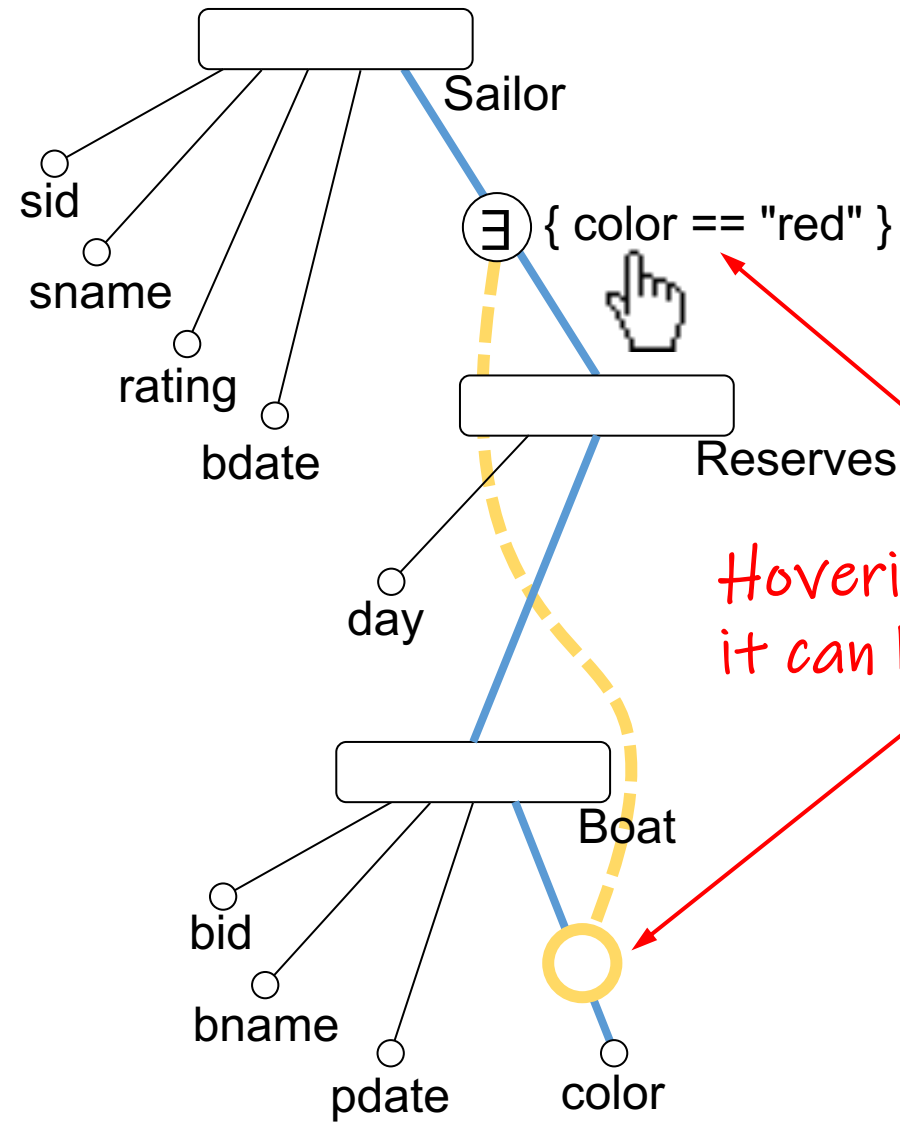
$$\{q.sname \mid \exists s \in \text{Sailor}[q.sname = s.sname \wedge \exists r \in \text{Reserves}[r.sid = s.sid \wedge \exists b \in \text{Boat}[b.bid = r.bid \wedge b.color = 'red']]]\}$$



# Dataplay

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}[q.sname = s.sname \wedge \exists r \in \text{Reserves}[r.sid = s.sid \wedge \exists b \in \text{Boat}[b.bid = r.bid \wedge b.color = 'red']]]\}$$

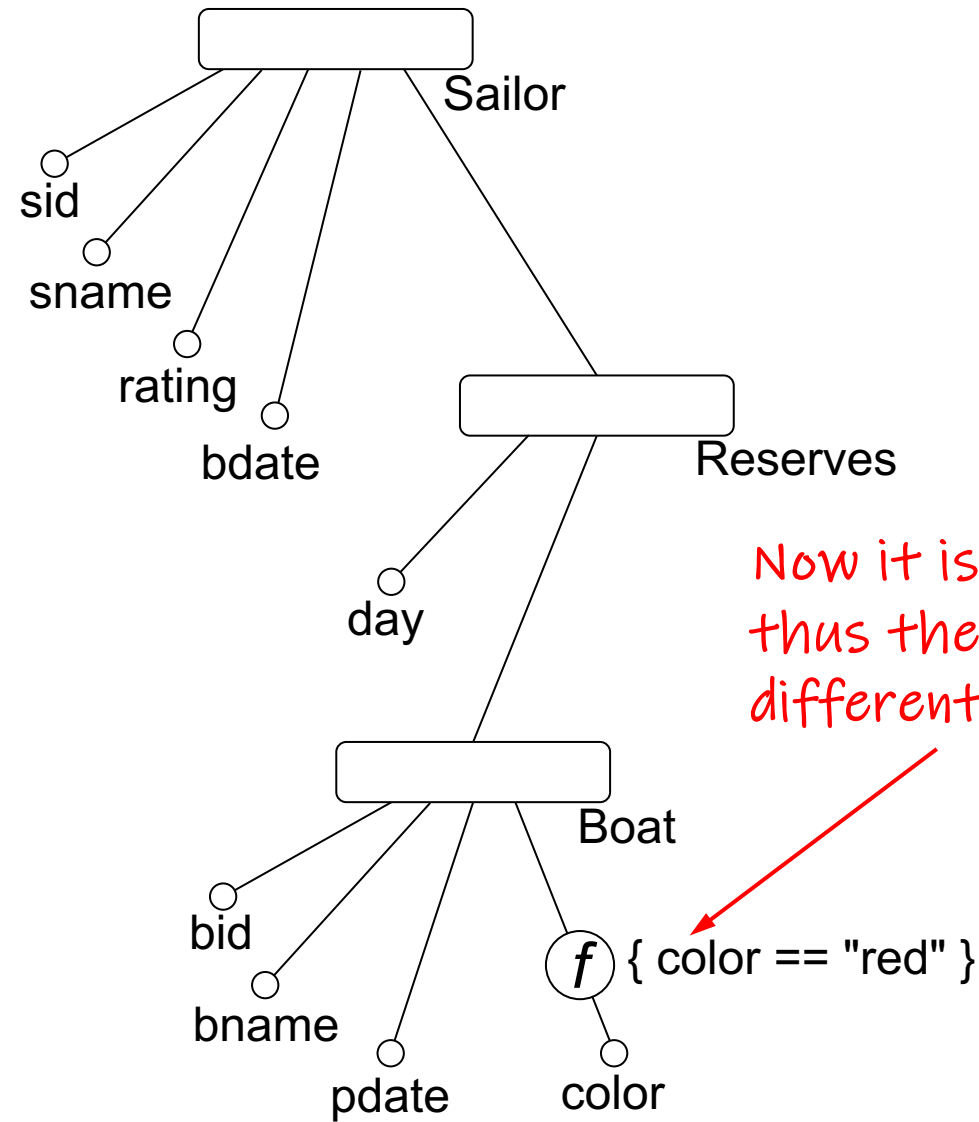
Figure drawn based on "Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge \exists r \in \text{Reserves} [r.sid = s.sid \wedge \exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = \text{'red'}]]]\}$$

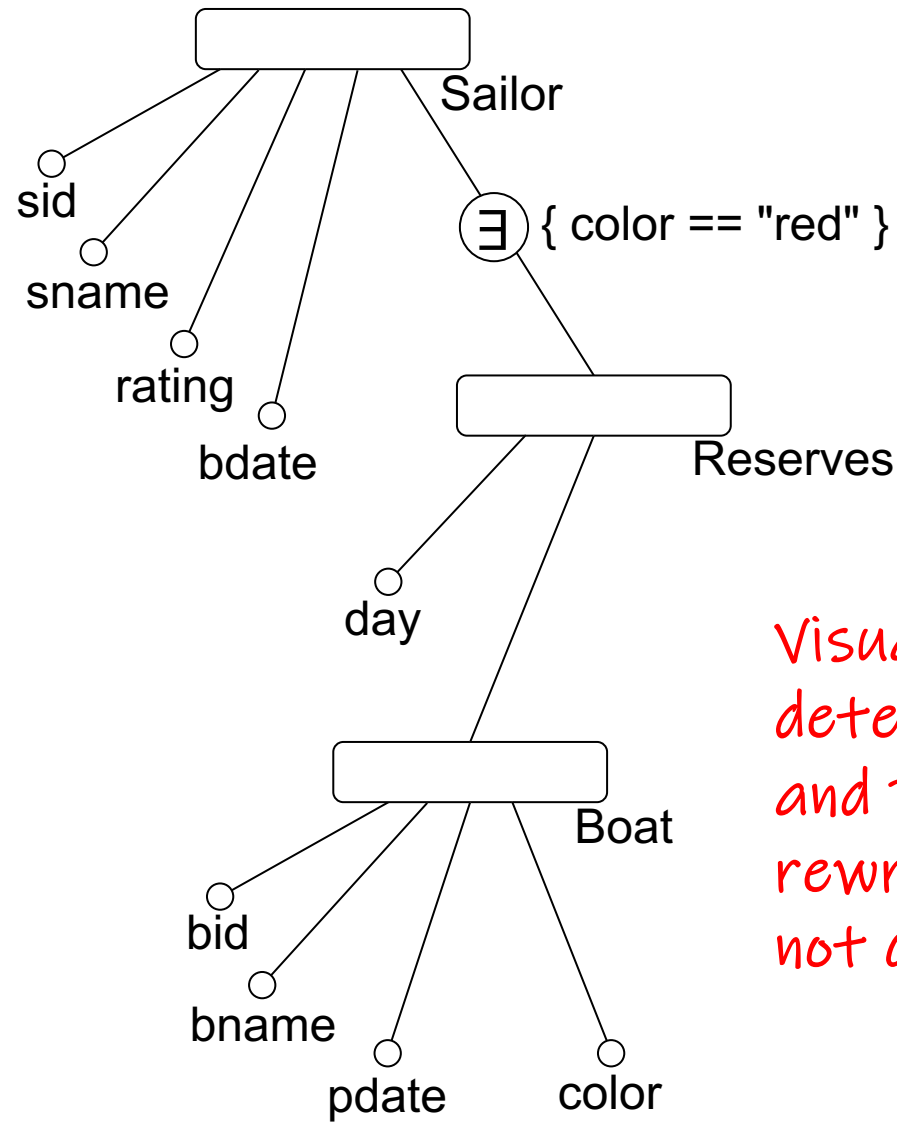
Figure drawn based on "Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
where exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



Visualization determined by schema and PK-FKs. Thus rewrite of query does not change the tree.

## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor}[q.sname = s.sname \wedge \exists r \in \text{Reserves}[r.sid = s.sid \wedge \exists b \in \text{Boat}[b.bid = r.bid \wedge b.color = 'red']]]\}$$

Figure drawn based on "Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>

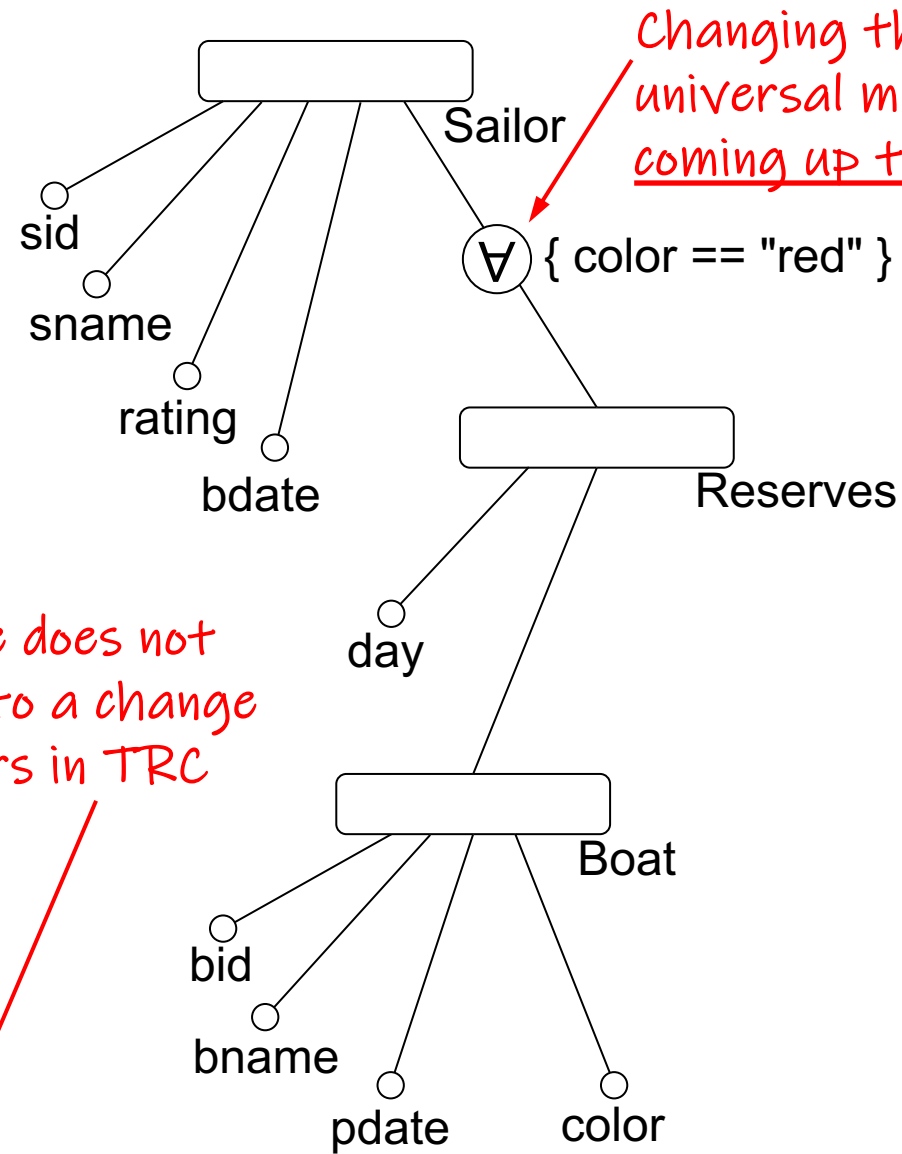
Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

This change does not correspond to a change in quantifiers in TRC



## TRC (Tuple Relational Calculus)

$$\{q.sname \mid \exists s \in \text{Sailor} [q.sname = s.sname \wedge (\forall r \in \text{Reserves} [r.sid = s.sid \rightarrow (\exists b \in \text{Boat} [b.bid = r.bid \wedge b.color = \text{'red'}])])]\}$$

Figure drawn based on "Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

- Cannot visualize correlated nested queries because the nesting hierarchy (and thus order of quantifiers) is predetermined
- However, Dataplay can express the query \*for a fixed database instance\* by interaction. As example:
  - create a bar chart of boat colors
  - brush bar for red (this creates a predicate expression of (bid='123', bid='236', bid='789', ...))
  - Add this predicate expression to an exists quantifier
  - cover the quantifier this becomes exists bid='123' AND exists bid='236' AND ...
  - The resulting query asks for sailors such there exist reservations for all these boats (which is an explicit list of the red boats in the current database)
- Unions (Query Q5) are not supported

## TRC (Tuple Relational Calculus)

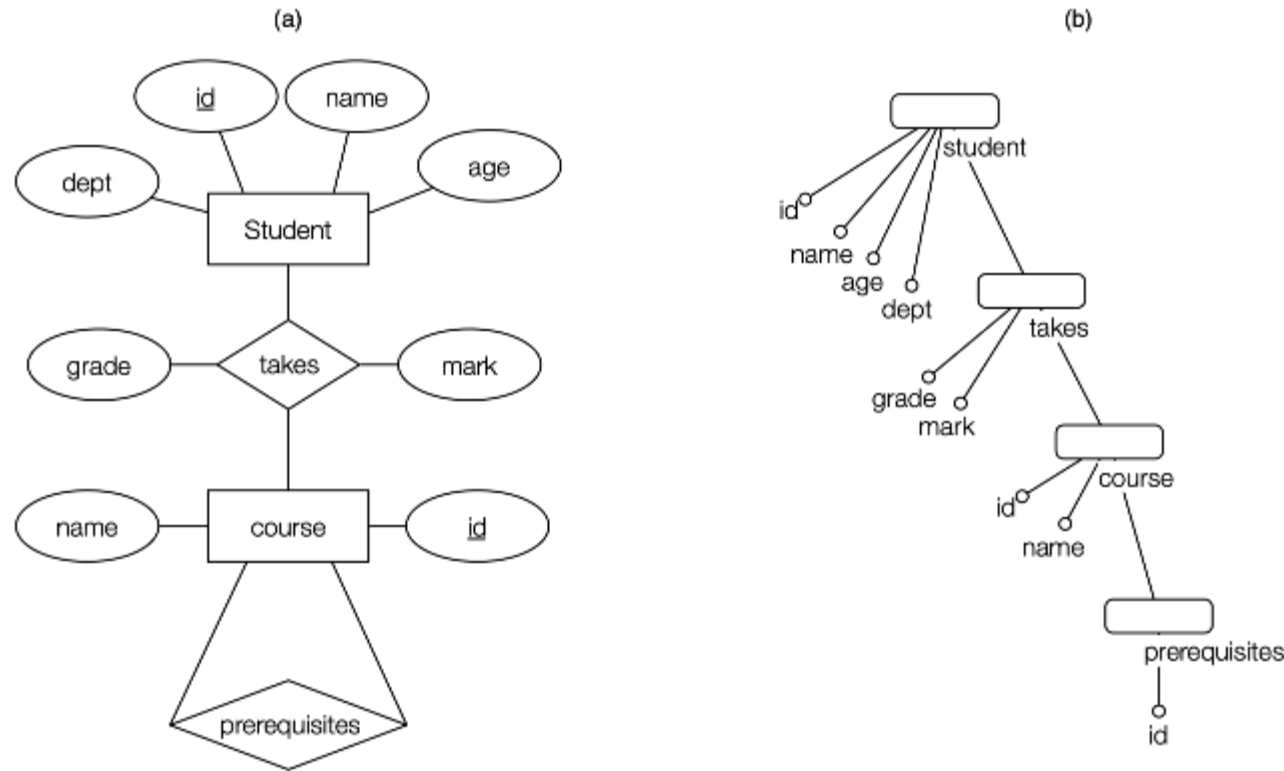
$$\{q.sname \mid \exists s \in \text{Sailor}[q.sname=s.sname \wedge (\forall b \in \text{Boat}[b.color='red' \rightarrow (\exists r \in \text{Reserves}[b.bid=r.bid \wedge r.sid=s.sid])])]\}$$

Figure drawn based on "Abouzied, Hellerstein, Silberschatz. DataPlay: interactive tweaking and example-driven correction of graphical database queries. UIST 2012. <https://doi.org/10.1145/2380116.2380144>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Dataplay (2012) Backup

# Dataplay



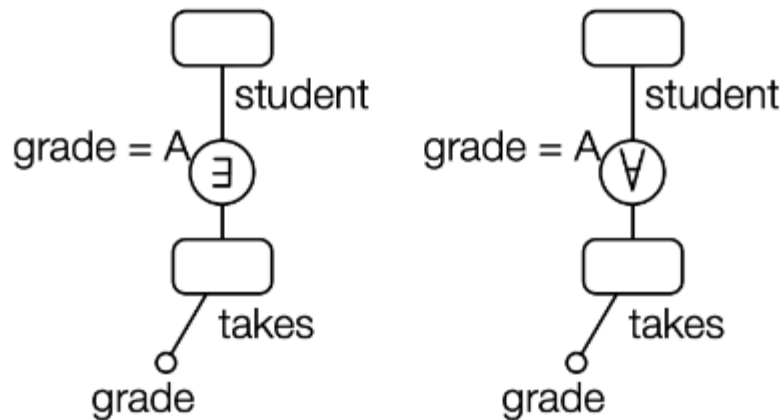
**Figure 1: (a) ER-diagram of a school database; (b) The nested-UR schema with student as pivot.**

Other observations:

1. Every query includes all tables from the schema. Thus querying one table (like red boats) requires showing all tables
2. Self-joins (one table appearing multiple times) seems not to be handled
3. Cyclic schemas are represented by using a spanning tree and a text-based join (reuse of variables)

# Dataplay

Figure 3 illustrates two QTs: one for finding students with at least one A and one for finding straight-A students. Since the nesting hierarchy for a query is predetermined, users do not need to specify how to group tuples for quantification. More importantly, modifying the quantifier type is localized to simply changing the symbol from  $\exists$  to  $\forall$  on the constraint node; the structure of the QT is preserved.



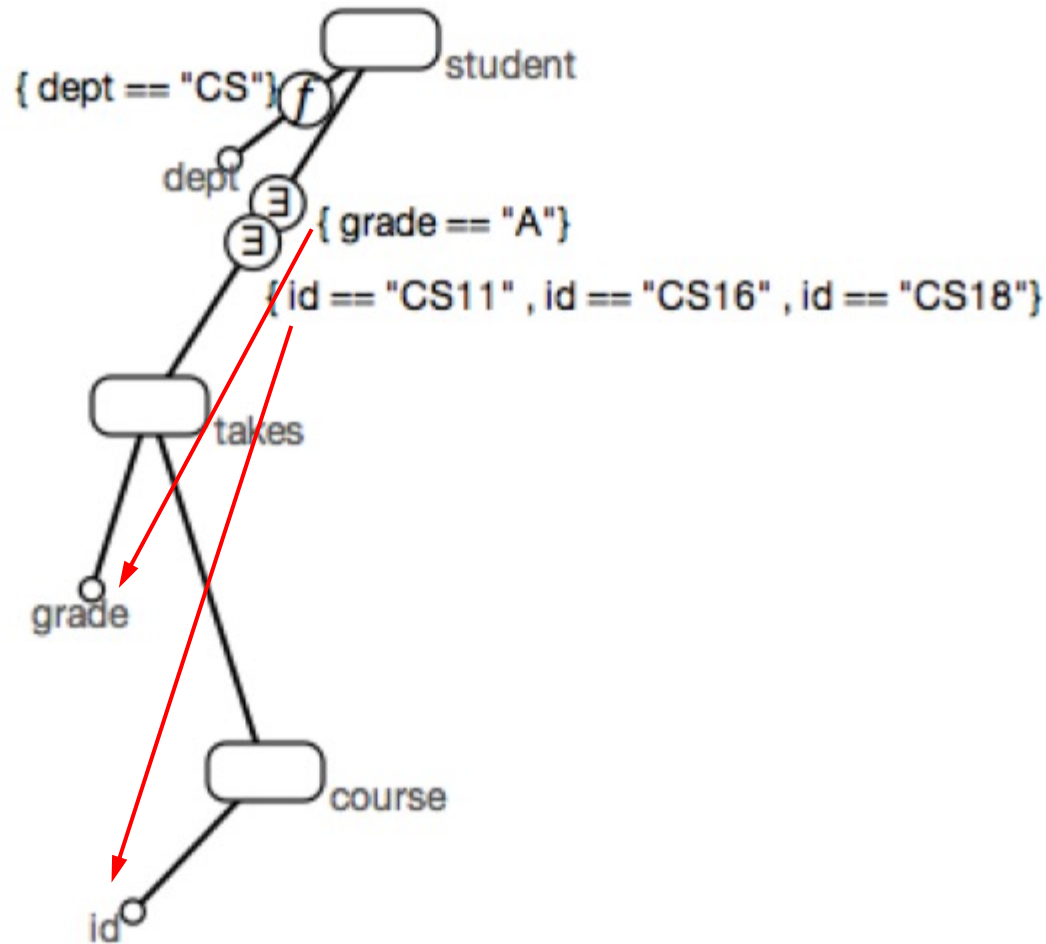
**Figure 3: (a) Students with some A's (b) Straight-A's**

Other observations:

1. Predetermined nesting hierarchy prevents correlated nested queries to be expressed (e.g. students who have taken all CS classes)



# DataPlay



Other observations:

1. Ambiguity if multiple tables contain an attribute named "id" (e.g. course id or prerequisite id)
2. All quantifiers are shown at the root of the tree, even if attributes appear in leaves. "Location" of attributes in the schema and their use can be separated (non-local)

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# SIEUFERD (2016)

Schema-Independent End-User Front-End  
for Relational Databases

Sources used:

- Bakke, Karger. Expressive query construction through direct manipulation of nested relational results. SIGMOD 2016. <https://doi.org/10.1145/2882903.2915210>
- Bakke. SIEUFERD: A Visual Query System. 2016. <https://www.youtube.com/watch?v=W6xmqcb8hFQ>
- Personal communication with Eirik Bakke. System reincarnated as Ultorg at <https://www.ultorg.com/>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# SIEUFERD

The crow's foot (one-to-many relationship between tables) is not necessary for understanding tables and we don't show it subsequently

- SIEUFERD is a direct manipulation spreadsheet-like interface that lets users manipulate the actual data. The interface consists of a "result header", optional popups, and the **result area**. We focus here only on the **result header**, which "encodes the structure of the query"

- The paper claims to be SQL-92-complete. The most interesting aspect for us here will be modeling negation with left joins and filters on null values

The screenshot displays the SIEUFERD interface with several key components labeled:

- Formula Bar**: Located at the top of the spreadsheet view.
- Result Header**: A red box highlights the header section of the spreadsheet, which includes table names and field names.
- Field Selector**: A popup window on the right showing a tree view of the database schema, including tables like `instructors_sections` and `instructors`, with fields like `last` and `first` selected.
- Filter Popup**: A popup window on the right showing a search filter for the `last` field, with a list of names and a checkbox for "(Include All)".
- Context Menu**: A menu is open over the spreadsheet data, showing options such as "Sort Ascending", "Sort Descending", "Filter...", "Hide Parent If Empty", "Collapse Duplicate Rows", and "One-to-Many".
- Result Area**: The main spreadsheet area containing data rows, with a red arrow pointing to it from the text "We focus here only on the result header".

# SIEUFERD

Q1b: "Find boats  
that are not red."

```
select distinct bid  
from Boat  
where color != 'red'
```

Boat	
bname	color ▼

Relation names are bold, (attributes are not bold)

Funnel icon (▼) indicates filter:  
actual filter condition is only shown in  
a separate "filter popup" window. In  
that popup window, all colors other  
than red are chosen.

All attributes that are visible are returned.  
Other attributes can be hidden in the "result  
header", but then the query logic is not visible

Recall that we are only focusing on the  
visual representation of the query. The  
actual system also displays the results  
(the goal is an interactive exploration).  
The backup shows screenshots from  
the actual system

# SIEUFERD

Q1: "Find boats  
that are red or blue."

```
select distinct bid  
from Boat  
where color = 'red'  
or color = 'blue'
```

Boat	
bname	color ▼

Header does not change:  
actual filter condition is only  
shown in a separate "filter  
pop" up window where colors  
"red" and "blue" are chosen

# SIEUFERD

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname  
from Boat  
where (color = 'red'  
or color = 'blue')  
and pdate < 1980
```

Boat	
bname	color ▼

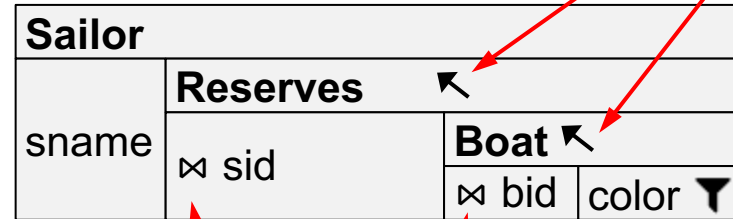
Header does not change

# SIEUFERD

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
join Reserves R
on S.sid=R.sid
join Boat B
on R.bid=B.bid
where color = 'red'
```

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```



"Nest equijoins" are by default treated like left joins (all tuples on the left of the join are shown even if there is no match on the right). To remove tuples on the left-hand side of the operator, a special "hide parent if empty" setting is required and indicated by the arrow-towards-root icon (↖)

Join conditions with attributes in outer scope are not visible and only shown in a separate "field selector" popup window. Both attributes Reserves.sid and Boat.bid could also be hidden.



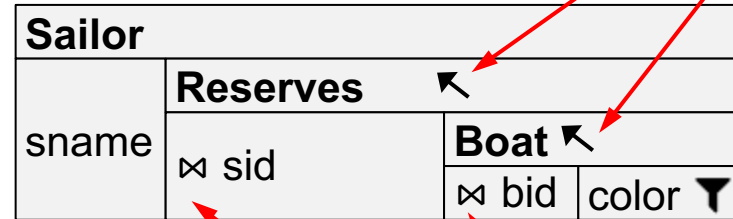
# SIEUFERD

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Intuitively, SIEUFERD expresses negation via left joins. We see here on the right a SQL variant that most closely mirrors that join-based semantics

```
select distinct S.sname
from Sailor S
join Reserves R
on S.sid=R.sid
join Boat B
on R.bid=B.bid
where color = 'red'
```



"Nest equijoins" are by default treated like left joins (all tuples on the left of the join are shown even if there is no match on the right). To remove tuples on the left-hand side of the operator, a special "hide parent if empty" setting is required and indicated by the arrow-towards-root icon (↖)

Join conditions with attributes in outer scope are not visible and only shown in a separate "field selector" popup window. Both attributes Reserves.sid and Boat.bid could also be hidden.

# SIEUFERD

Q3a: "Find sailors who reserved no boat."

```
select distinct S.sname
from Sailor S
where not exists
(select *
from Reserves R
where S.sid=R.sid)
```

Intuitively, SIEUFERD expresses negation via left joins. We see here on the right a SQL variant that most closely mirrors that join-based semantics

```
select distinct S.sname
from Sailor S
left join Reserves R
on S.sid = R.sid
where R.sid is null
```

Sailor		
sname	$f_x$ sid $\nabla$	Reserves
		$\bowtie$ sid

Since we need to use a left join the "hide parent if empty" setting is not used, thus no arrow-towards-root icon ( $\nabla$ )

Since the "is null" condition needs to be applied to the result of the left join (not the reserves table directly), we need to add a "reference formula" under the sailor relation that repeats the values of Reserves.sid *after* the join. And then apply a filter condition "is null"

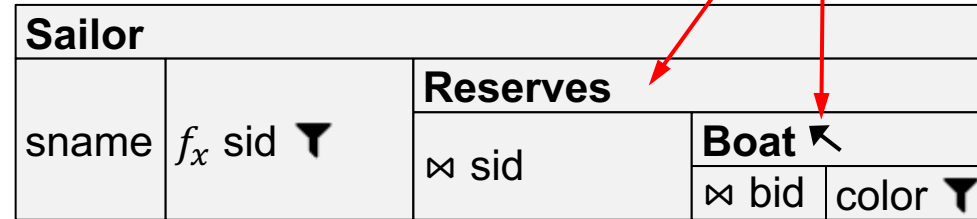
# SIEUFERD

Q3b: "Find sailors who reserved no red boat."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R, Boat B
   where S.sid=R.sid
   and R.bid=B.bid
   and B.color='red')
```

Intuitively, SIEUFERD expresses negation via left joins. We see here on the right a SQL variant that most closely mirrors that join-based semantics

We need to apply the "arrow-towards-root" icon ("hide parent if empty") for Boat, but must not apply it for Reserves! See SQL explanation below



```
select distinct S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid = B.bid
and color = 'red')
on S.sid = R.sid
where R.sid is null
```

The query needs to propagate the filter from Boats to Reserves (thus \*no\* left join) forming the right part of a left join from Sailor. This operation is \*not\* associative, thus the required parenthesis here (and "hide parent if empty" above)

# SIEUFERD

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

Sailor				
sname	$f_x$ count ▼	Reserves		
		∞ sid	Boat ↖	
			∞ bid	color ▼

An alternative syntax using aggregation and COUNT=0

```
select distinct S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid=B.bid
and color != 'red')
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) = 0
```

# SIEUFERD

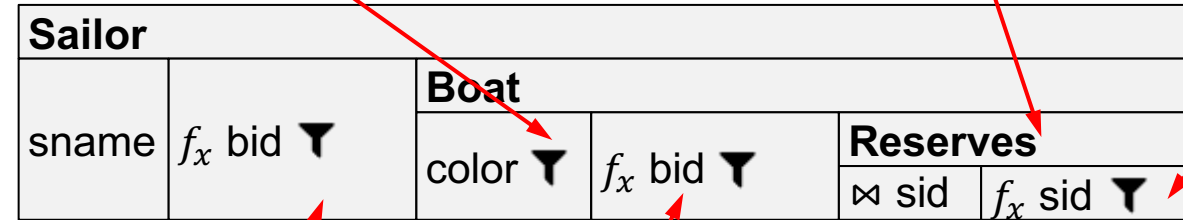
Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

2. Filter for  
color='red'

3. Left Join, thus no "arrow-towards-root"

1. Reference to Sailor.sid / filter  
for Sailor.sid=Reserves.sid is true



4. Reference to Reserves.bid / then filter "is null"

5. Red boats that are not reserved by each Sailor

6. References to Boat.bid / then filter "is null"

Notice how the query header by itself does not allow  
a user to understand a query's semantic.

# SIEUFERD

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

```
select distinct case when choice then R.bid
else B.bid end,
case when choice then R.bname
else B.bname end
from RedBoat R, BlueBoat B,
(select * from (values (true), (false)) V(choice) ) V
```

Temporary valuations table V contains values true and false

V
choice
true
false

RedBoat and BlueBoat tables cross joined (could also be nested)

V						
choice	$f_x$ bid reference	$f_x$ bname reference	RedBoat		BlueBoat	
			bid	bname	bid	bname

Conditional statement for bid (analog for bname) if V.choice then RedBoat.bid else BlueBoat.bid

This SQL query shows the logic that SIEUFERD would use if it were implemented in SQL.

Schema

RedBoat
bid
bname
pdate

BlueBoat
bid
bname
pdate

# SIEUFERD (2016)

## Backup

# SIEUFERD / Ultorg (actual screenshots)

*Q1b: "Find boats  
that are not red."*

```
select bid  
from Boat  
where color != 'red'
```

boat			
bid	bname	color ▼	pdate
101	Interlake	blue	2013-04-10
103	Clipper	green	2013-04-10

Filter

Find:

☐ (Select All)  
☒ blue  
☒ green  
☐ red

Excluding 1 value



# SIEUFERD / Ultorg (actual screenshots)

Q1: "Find boats  
that are red or blue."

```
select bid
from Boat
where color = 'red'
or color = 'blue'
```

boat			
bid	bname	color ▼	pdate
101	Interlake	blue	2013-04-10
102	Interlake	red	2013-04-10
104	Marine	red	2013-04-10

Filter

Find:

☐ (Select All)

☒ blue

☐ green

☒ red

Including 2 values

# SIEUFERD / Ultorg (actual screenshots)

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

boat			
bid	bname	color ▼	pdate ▼

Filter

Find: 1980

☐ (Select All)

☐ **From** >= 1980-01-01

☐ **Between** >= 1980-01-01 and < 1981-01-01

☒ **Before** < 1980-01-01

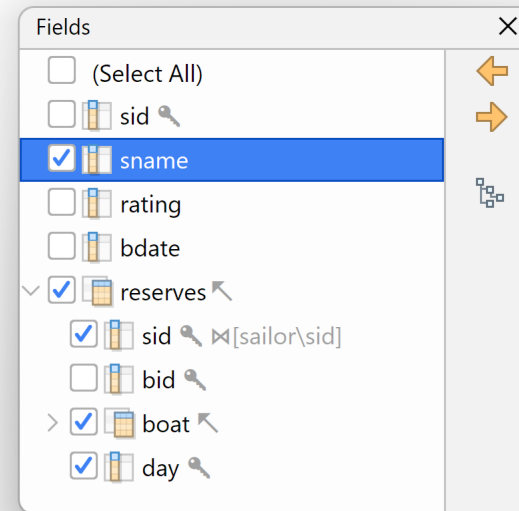
Including various conditions

# SIEUFERD / Ultorg (actual screenshots)

Q2: "Find sailors who reserved a red boat."

```
select S.sname
from Sailor S
join Reserves R
on S.sid=R.sid
join Boat B
on R.bid=B.bid
where color = 'red'
```

sailor					
sname	reserves				
	sid	boat			day
		bid	bname	color	
Dustin	22	102	Interlake	red	2018-10-10
	22	104	Marine	red	2018-10-07
Lubber	31	102	Interlake	red	2018-11-10
	31	104	Marine	red	2018-11-12



# SIEUFERD / Ultorg (actual screenshots)

Q3a: "Find sailors who reserved no boat."

```
select S.sname
from Sailor S
left join Reserves R
on S.sid = R.sid
where R.sid is null
```

Reference formula version (1/2)

sailor						
sname	$f_x$ sid	reserves				
		$\bowtie$ sid	boat			day
		$\bowtie$ bid	bname	color		
Dustin	22	22	101	Interlake	blue	2018-10-10
		22	102	Interlake	red	2018-10-10
		22	103	Clipper	green	2018-10-08
		22	104	Marine	red	2018-10-07
Brutus						
Lubber	31	31	102	Interlake	red	2018-11-10
		31	103	Clipper	green	2018-11-06
		31	104	Marine	red	2018-11-12
Andy						
Rusty						
Horatio	= [sid]	64	101	Interlake	blue	2018-09-05
		64	101	Interlake	blue	2018-09-08
Zorba						
Horatio	74	74	103	Clipper	green	2018-09-08
Art						
Bob						

# SIEUFERD / Ultorg (actual screenshots)

Q3a: "Find sailors who reserved no boat."

```
select S.sname
from Sailor S
left join Reserves R
on S.sid = R.sid
where R.sid is null
```

Reference formula version (2/2)

The screenshot shows the Ultorg interface with two tables: 'sailor' and 'reserves'. The 'sailor' table has columns 'sname' and 'sid'. The 'reserves' table has columns 'sid', 'boat', 'bid', 'bname', 'color', and 'day'. A blue box highlights the 'sid' column in the 'sailor' table, and a formula icon 'fx' is visible. A 'Filter' dialog box is open, showing a search bar with the text 'Enter one or two numbers (e.g. "25 50")'. Below the search bar, there is a list of values with checkboxes: '(Select All)', 'null' (checked), '22', '31', '64', and '74'. At the bottom of the dialog, it says 'Including 1 value'.

sailor	reserves
sname	sid boat day
	bid bname color
Brutus	
Andy	
Rusty	
Zorba	
Art	
Bob	

# SIEUFERD / Ultorg (actual screenshots)

Q3a: "Find sailors who reserved no boat."

```
select S.sname
from Sailor S
left join Reserves R
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) = 0
```

Count formula version (1/2)

sailor						
sname	$f_x$ count	reserves				
		⌞ sid	boat			day
		⌞ bid	bname	color		
Dustin	4	22	101	Interlake	blue	2018-10-10
		22	102	Interlake	red	2018-10-10
		22	103	Clipper	green	2018-10-08
		22	104	Marine	red	2018-10-07
Brutus	0					
Lubber	3	31	102	Interlake	red	2018-11-10
		31	103	Clipper	green	2018-11-06
		31	104	Marine	red	2018-11-12
Andy	0					
Rusty	0					
Horatio	=count ( [ boat ] )		01	Interlake	blue	2018-09-05
			01	Interlake	blue	2018-09-08
Zorba	0					
Horatio	1	74	103	Clipper	green	2018-09-08
Art	0					
Bob	0					

# SIEUFERD / Ultorg (actual screenshots)

Q3a: "Find sailors who reserved no boat."

```
select S.sname
from Sailor S
left join Reserves R
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) = 0
```

Count formula version (2/2)

sailor		reserves			
sname	fx $\nabla$ count	sid	boat		day
		bid	bname	color	
Brutus	0				
Andy	0				
Rusty	0				
Zorba	0				
Art	0				
Bob	0				

Filter

Find:

☐ (Select All)

☒ 0

☐ 1

☐ 2

☐ 3

☐ 4

Including 1 value

# SIEUFERD / Ultorg (actual screenshots)

Q3b: "Find sailors who reserved no red boat."

```
select S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid = B.bid
and color = 'red')
on S.sid = R.sid
where R.sid is null
```

sailor		reserves					
sname	fx sid	sid	boat	bid	bname	color	day
Dustin	22	22	102	Interlake	red	2018-10-10	
		22	104	Marine	red	2018-10-07	
Brutus Lubber	31	31	102	Interlake	red	2018-11-10	
		31	104	Marine	red	2018-11-12	
Andy							
Rusty							
Horatio							
Zorba							
Horatio							
Art							
Bob							

Filter

Find: Enter one or two numbers (e.g. "25 50")

☐ (Select All)

☐ null

☐ 22

☐ 31

Including all values



# SIEUFERD / Ultorg (actual screenshots)

Q3b: "Find sailors who reserved no red boat."

```
select S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid = B.bid
and color = 'red')
on S.sid = R.sid
where R.sid is null
```

sailor		reserves					
sname	fx sid	sid	boat	bid	bname	color	day
Brutus							
Andy							
Rusty							
Horatio							
Zorba							
Horatio							
Art							
Bob							

Filter

Find: Enter one or two numbers (e.g. "25 50")

☐ (Select All)

☒ null

☐ 22

☐ 31

Including 1 value

# SIEUFERD / Ultorg (actual screenshots)

Q3: "Find sailors who reserved only red boats."

```
select S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid=B.bid
and color != 'red')
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) = 0
```

sailor		reserves					
sname	fx count([re	sid	boat	bid	bname	color	day
Dustin	2	22	101	Interlake	blue	2018-10-10	
		22	103	Clipper	green	2018-10-08	
Brutus	0						
Lubber	1	31					
Andy	0						
Rusty	0						
Horatio	2	64					
		64					
Zorba	0						
Horatio	1	74					
Art	0						
Bob	0						

Filter

Find:

☐ (Select All)

☐ 0

☐ 1

☐ 2

Including all values

# SIEUFERD / Ultorg (actual screenshots)

Q3: "Find sailors who reserved only red boats."

```
select S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid=B.bid
and color != 'red')
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) = 0
```

sailor		reserves					
sname	fx count	sid	boat	bid	bname	color	day
Brutus	0						
Andy	0						
Rusty	0						
Zorba	0						
Art	0						
Bob	0						

Filter

Find:

☐ (Select All)

☒ 0

☐ 1

☐ 2

Including 1 value

# SIEUFERD / Ultorg (actual screenshots)

Q4: "Find sailors who reserved all red boats."

```
select S.sname
from Sailor S
left join (Reserves R
join Boat B
on R.bid=B.bid
and color = 'red')
on S.sid = R.sid
group by S.sid, S.sname
having count(R.sid) =
(select count(*)
from Boat B
where color = 'red')
```

sailor		reserves					all red boats	
sname	$f_x$ count([re	sid	bid	bname	color	day	bname	color
Dustin	<input checked="" type="checkbox"/>	22	102	Interlake	red	2018-10-10	Interlake	red
		22	104	Marine	red	2018-10-07	Marine	red
Brutus	<input type="checkbox"/>						Interlake	red
							Marine	red
Lubber	<input checked="" type="checkbox"/>	31	102	Interlake	red	2018-11-10	Interlake	red
		31	104	Marine	red	2018-11-12	Marine	red
Andy	<input type="checkbox"/>						Interlake	red
							Marine	red
Rusty		=count ( [ reserved red boats ] ) = count ( [ all red boats ] )					Interlake	red
Horatio	<input type="checkbox"/>						Marine	red
							Interlake	red
Zorba	<input type="checkbox"/>						Marine	red
							Interlake	red
Horatio	<input type="checkbox"/>						Marine	red
							Interlake	red
Art	<input type="checkbox"/>						Marine	red
							Interlake	red
Bob	<input type="checkbox"/>						Marine	red
							Interlake	red

# SIEUFERD / Ultorg (actual screenshots)

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

tworows_truefalse {							
Choice	fx	bid	bname	RedBoat		BlueBoat	
	reference		reference fx	Bid	Bname	Bid	Bname
<input type="checkbox"/>		101	Titanic	201	Mardi Gras	101	Titanic
				202	MS Iona		
				203	Queen Mary		
<input type="checkbox"/>		102	Carpathia	201	Mardi Gras	102	Carpathia
				202	MS Iona		
				203	Queen Mary		
<input checked="" type="checkbox"/>		201	Mardi Gras	201	Mardi Gras	101	Titanic
						102	Carpathia
<input checked="" type="checkbox"/>		202	MS Iona	202	MS Iona	101	Titanic
						102	Carpathia
<input checked="" type="checkbox"/>		203	=if ( [Choice], [RedBoat\Bname], [BlueBoat\Bname] )				

## Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

```
select distinct case when choice then R.bid
else B.bid end,
case when choice then R.bname
else B.bname end
from RedBoat R, BlueBoat B,
(select * from (values (true), (false)) V(choice) ) V
```

# SIEUFERD

**Filter.** Using the filter popup (Figure 2), a filter can be defined on any field, indicated by the filter icon (▼). Filters on relation fields restrict the set of tuples retrieved in that relation, while filters on primitive fields restrict the tuples of the parent relation. In the following example, the MEETINGS relation is filtered to show only tuples for which the DAY is W:

courses ⏪		readings ⏪		sections ⏪⏩					
title	max_enroll	author_name	title	type	num	meetings ⏪⏩			
						day ⏴	start	end	
Comedy	99	Moliere	The Miser	L	01	W	11:00	11:50	
		Feydeau	A Flea in Her Ear	P	01	W	12:30	13:20	
		Reza	Art	P	02	W	12:30	13:20	
				P	03	W	13:30	14:20	
				P	05	W	14:30	15:20	
American Politics	78			L	01	W	11:00	11:50	
				P	01	W	13:30	14:20	
				P	01	W	13:30	14:20	
				P	04	W	14:30	15:20	
Judicial Politics	24	Rosenberg, Gerald		The Hollow Hope	L	01	W	11:00	11:50
		Lazarus	Closed	P	02	W	13:30	14:20	
				P	04	W	11:00	11:50	

Filter icon (▼) indicates filter. Here the meetings relation is filtered to show only tuples with day = W (actual filter condition only shown in separate "filter popup" window)

"Nest equijoins" are by default treated like left joins (all tuples on the left of the join are shown even if there is no match on the right). To remove tuples on the left-hand side of the operator, a special "hide parent if empty" setting is required and indicated by the arrow-towards-root icon (↖)

Notice that filters are applied to the relation, not the result of a join. This is important for modeling negation

# SIEUFERD

**Flat joins.** Traditional flat joins can be expressed by referencing a descendant relation from a formula without enclosing the reference in an aggregate function. In the following example, each course title is repeated once for each distinct author name in the reading list, because the AUTHOR REFERENCE field in the COURSES relation references the READINGS relation without the use of an aggregate function:

courses <-			readings <-	
title	exam_type	author_reference f <sub>x</sub>	author_name	title
Roman Art	Other	Gombrich	Gombrich	Art and Illusion
Roman Art	Other	Ramage	Ramage	Roman Art
Comedy	Final	Feydeau	Feydeau	A Flea in Her Ear
Comedy	Final	= [author_name]		The Miser
Comedy	Final	Reza	Reza	Art
Russian Drama	Other	Chekhov	Chekhov	The Seagull
Russian Drama	Other	Pushkin	Pushkin	Little Tragedies
Russian Drama	Other	Vampilov	Vampilov	The Duck Hunt
American Politics	Final			
Junior Seminars	Other	Pierre Loti	Pierre Loti	India
Judicial	Final	Lazarus	Lazarus, Edward	Closed Chambers

The actual behavior is that of a left join, with a null value being returned for the course AMERICAN POLITICS, which has no readings in its reading list. To express an inner join instead, the HIDE

In order to apply a filter *after* a left join, a "reference formula" needs to be added that represents a "reference" to an attribute in the right side of the left join

**Filters and aggregate functions.** When an aggregate function references a relation with a filter applied to it, the filter is evaluated before the aggregate.

It is equally valid to define a filter on the output side of an aggregate, e.g. on TITLE or TOTAL DURATION in the example above.



# SIEUFERD

- Set difference. Here, we can filter for null values generated by a left join. If  $e = e_a - e_b$ , with  $n = N(e)$ , then  $t(e) = t(\pi_{\langle e_a[1] \rangle \rightarrow e[1], \dots, \langle e_a[n] \rangle \rightarrow e[n]}(\sigma_{\langle M \text{ IS NULL} \rangle}(e_a \bowtie_C e'_b)))$  where  $\bowtie$  is a left outer join,  $C = \langle e_a[1] = e'_b[1] \wedge \dots \wedge e_a[n] = e'_b[n] \rangle$ , and  $e'_b$  adds an arbitrary non-nullable attribute  $M$  to  $e_b$ , e.g.  $e'_b = \pi_{\langle e_b[1] \rangle \rightarrow e'_b[1], \dots, \langle e_b[n] \rangle \rightarrow e'_b[n], \langle 42 \rangle \rightarrow M}(e_b)$ . Another approach would be to COUNT values in  $e_b$  and filter for zero.

Negation (set difference) is modeled via a left join. Since filters are by applied to the relation, not the result of a join, one needs to add a "reference formula" to the relation on the left side of the join, followed by a filter

Here the filter "is null" needs to be applied to the relation resulting from the join, not the relation on the right side



# SIEUFERD

- *Set union.* A conditional formula can be used with a Cartesian product to produce the desired effect. If  $e = e_a \cup e_b$ , with  $n = N(e)$ , then  $t(e) = t(\pi_{F_1 \rightarrow e[1], \dots, F_n \rightarrow e[n]}(e_a \times e_b \times V))$  where  $V$  is the constant relation  $\{(\text{FALSE}), (\text{TRUE})\}$  and  $F_i$  denotes the formula  $\langle V[1] ? e_a[i] : e_b[i] \rangle$ . In the future, we might introduce an explicit UNION function as syntactic sugar for this kind of construction; see Figure 7 for an example.

Conditional statement:  
if  $V.\text{choice}$  then  $A.i$  else  $B.i$

Union is modeled via a Cartesian Product between the two input tables, and then condition statements that leverage a table " $V(\text{choice})$ " that contains tuples true and false.

# SIEUFERD

The following is a simple query that instantiates the table called COURSES and displays a selection of its fields:

courses ⌵					
id	area_id	title	may_pdf	may_audit	exam_type
56	2	Roman Art	N	Y	Other
177	2	Comedy	Y	Y	Final
845	2	Russian Drama	N	N	Other
1795	4	American Politics	Y	Y	Final
2566		Junior Seminars	N	N	Other
3921	4	Judicial Politics	Y	Y	Final

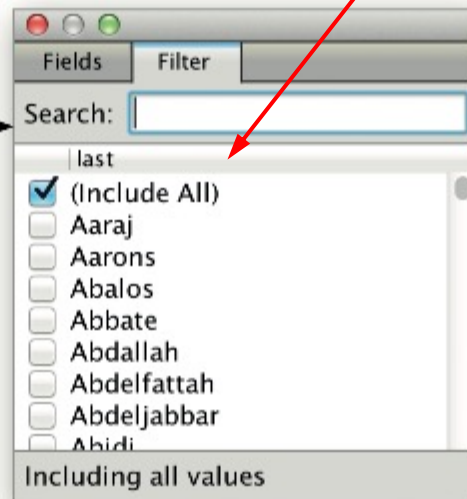
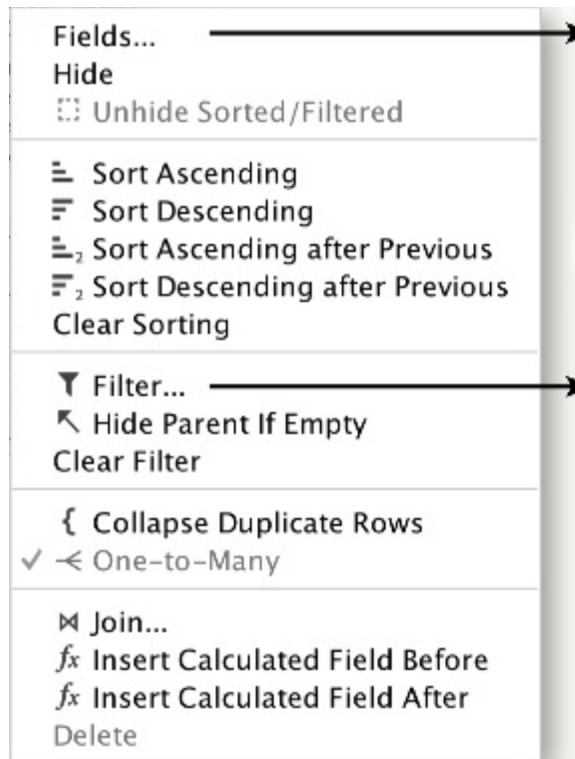
Crow's foot is shown for single table.  
The symbol is not needed for understanding a query, and was also removed from later systems by the authors.

# SIEUFERD

Negation of a filter `color = 'red'` to instead `color != 'red'` requires choosing all other values. But it is achieved with a sequence of:

- first choosing "include all",
- then unselecting "red"

This translates into a filter `color <> 'red'`, which makes the query resilient to changes in data: thus it still works after adding a new color, say "frog-green"



**Filter popup:** Allows the user to associate a filter with the currently selected field. The list of values available to filter on is generated automatically using a separate database query. Filters may be associated with either primitive fields or relation fields.

# SIEUFERD

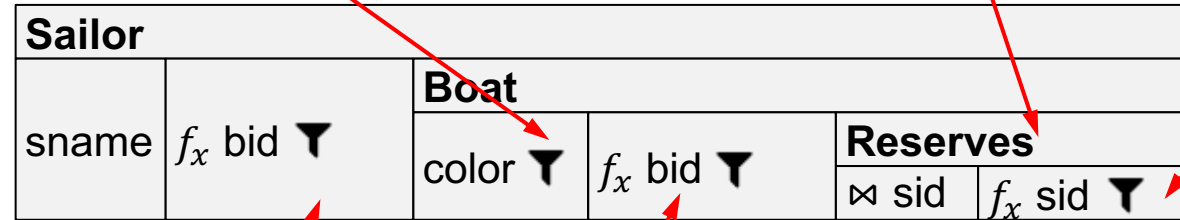
Q: "Find sailors who reserved all red boats."

```
select S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

2. Filter for  
color='red'

1. Reference to Sailor.sid / filter  
for Sailor.sid=Reserves.sid is true

3. Left Join, thus no "arrow-towards-root"



4. Reference to Reserves.bid / then filter "is null"

5. Red boats that are not reserved by each Sailor

6. References to Boat.bid / then filter "is null"

Notice how the query header by itself does not allow a user to understand a query's semantic.

# SIEUFERD

Q: "Find sailors who reserved all red boats."

```
select S.sname
from Sailor S
where not exists
(select *
from Boat B
where color = 'red'
and not exists
(select *
from Reserves R
where S.sid=R.sid
and R.bid=B.bid))
```

```
select S.sname
from Sailor S, Boat B, Reserves R
where R.sid=S.sid
and R.bid=B.bid
and color = 'red'
group by S.sid
having count(distinct B.bid) =
(select count(B2.bid)
from boat B2
where B2.color='red')
```

$f_x$  =countd ([Bid]) = count ([All Red Boats])

Sailor		$f_x$ countd	Reserves			All Red Boats	
Sid	Sname		Boat	Bname	Color	Bname	Color
1	Popeye	true	52	Staatsraaden	Red	Staatsraaden	Red
			56	Unsinkable II	Red	Unsinkable II	Red
3	Dylan	true	52	Staatsraaden	Red	Staatsraaden	Red
			56	Unsinkable II	Red	Unsinkable II	Red

The preferred way of expressing universally quantified queries in SIEUFERD is via GROUP BY and COUNTING

# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)

# SQLVis (2021)

## Sources used:

- Miedema. Towards successful interaction between humans and databases. Master thesis. Eindhoven University of Technology. 2019. <https://research.tue.nl/en/studentTheses/towards-successful-interaction-between-humans-and-databases>
- Miedema, Fletcher. SQLVis: Visual Query Representations for Supporting SQL Learners. VL/HCC 2021. <https://doi.org/10.1109/VL/HCC51201.2021.9576431>
- SQLVis library: <https://github.com/Giraphne/sqlvis> (8/2023)

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# SQLVis

- SQLVis represents SQL queries visually while a user is composing a query.
- The goal is thus to closely capture the actual syntax of SQL (possibly also for debugging)

The screenshot displays the SQL visualizer interface. On the left, a text area contains the following SQL query:

```
multipleWhere  
  
select MAX(quantity)  
from purchase AS pur, product as p  
WHERE p.pID = pur.pID  
AND p.pID < 50  
AND pur.price > 10;
```

Below the text area are two buttons: "Execute" and "Visualize".

To the right of the text area is a visual representation of the query. It shows two tables: "purchase pur" and "product p". The "purchase pur" table has columns: tiD, ciD, siD, piD, date, quantity, and price. The "product p" table has columns: piD, pName, and suffix. A line connects the piD column of the "product p" table to the piD column of the "purchase pur" table, with the text "product.piD = purchase.piD" above the line. The "quantity" column in the "purchase pur" table is highlighted in orange, and the "price" column is highlighted in green. The "piD" column in the "product p" table is highlighted in green.

Below the visual representation is a results table with the following data:

MAX(quantity)
11

On the right side of the interface is a "Query History" panel. It lists the following queries: "multipleSubquery", "multipleWhere" (highlighted in green), "subquery", "simple", "whereString", "multipleConditions", "multipleNumbers", and "multipleNumbersSub". Each query has a trash icon next to it.

At the bottom right of the interface are three buttons: "Store", "Clear & New", and "Database Schema".

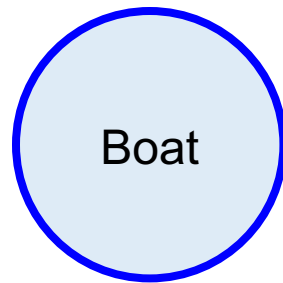


# SQLVis

*Q1b: "Find boats  
that are not red."*

```
select distinct bname  
from Boat  
where color != 'red'
```

Tables are by default "collapsed".



Schema

Boat
<u>bid</u>
bname
color
pdate

Boat
<u>bid</u>
bname
color
pdate

Q1b: "Find boats  
that are not red."

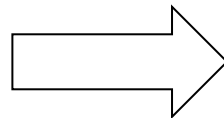
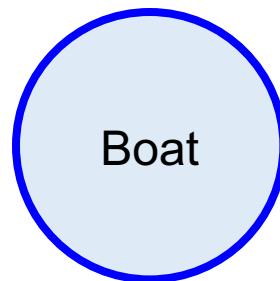
```
select distinct bname  
from Boat  
where color != 'red'
```

Tables are by default "collapsed".

The expanded view shows all attributes  
horizontally, in a tabular form inspired by QBE

Returned attributes in orange  
(alias not possible)

Selections in green.



Boat			
<b>bid</b>	<b>bname</b>	<b>color</b>	<b>pdate</b>
		!=red	

# SQLVis

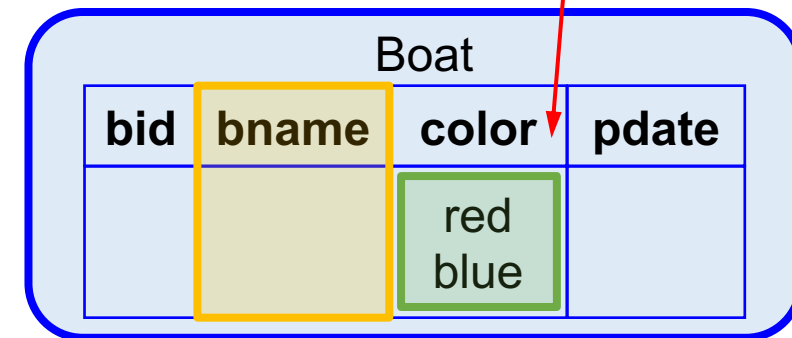
*Q1: "Find boats  
that are red or blue."*

```
select distinct bname  
from Boat  
where color = 'red'  
or color = 'blue'
```

Schema

Boat
<u>bid</u>
bname
color
pdate

Like QBE, disjunctions are  
written in different rows



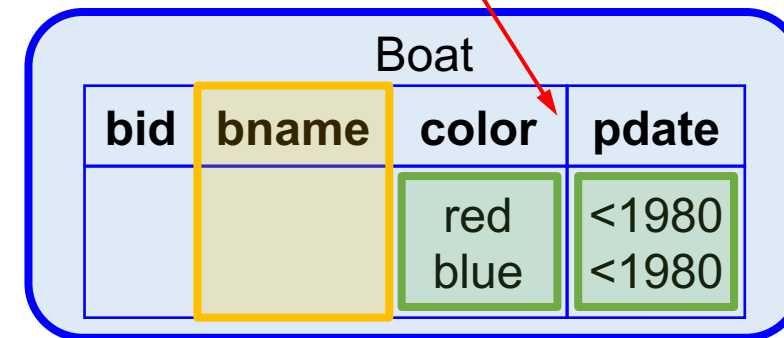
Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```

Like QBE, more complicated Boolean expressions are written in DNF: Conditions in the same row are connected by "AND", Conditions in distinct rows are connected by "OR"

```
... where (color = 'red' and pdate < 1980)
or (color = 'blue' and pdate < 1980)
```

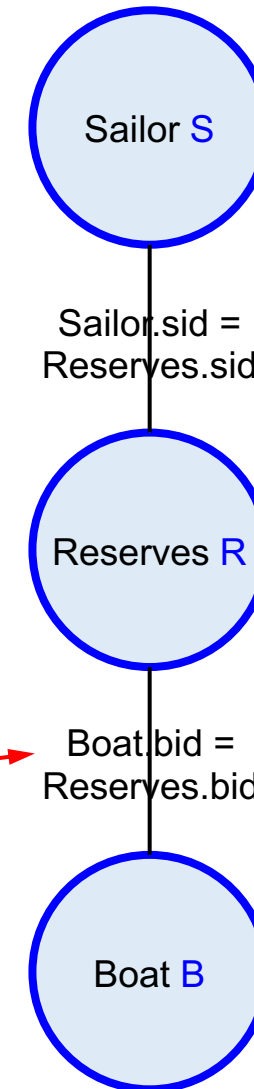


# SQLVis

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Join conditions shown as  
atomic label (text) on  
line between tables

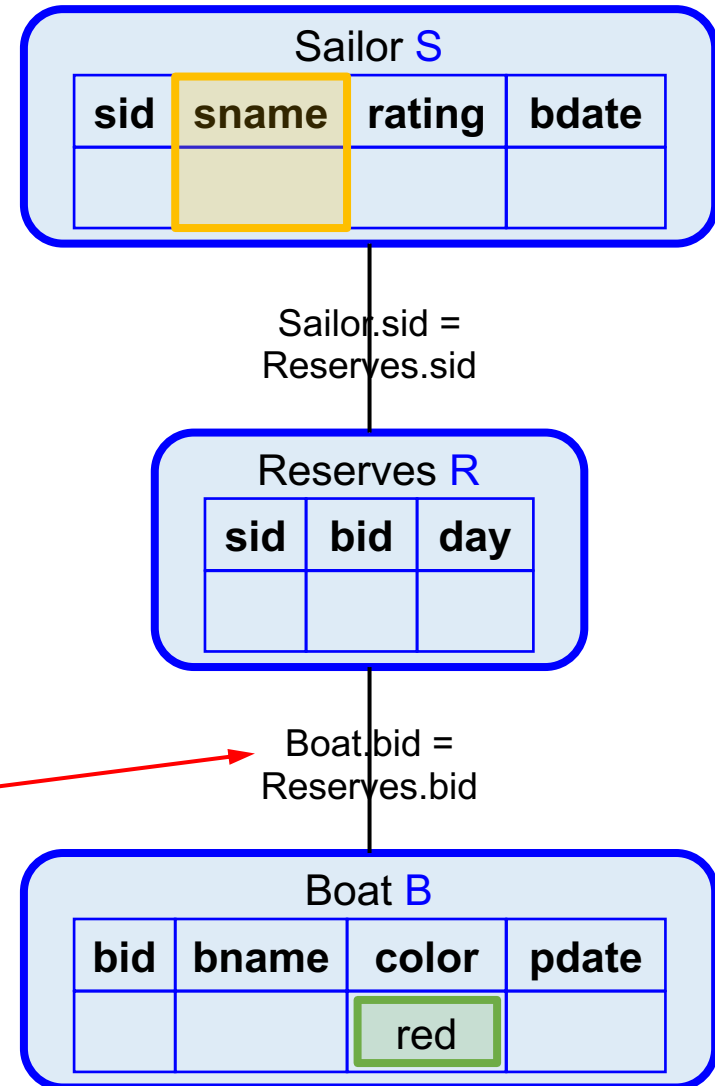


# SQLVis

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Join conditions shown as  
atomic label (text) on  
line between tables



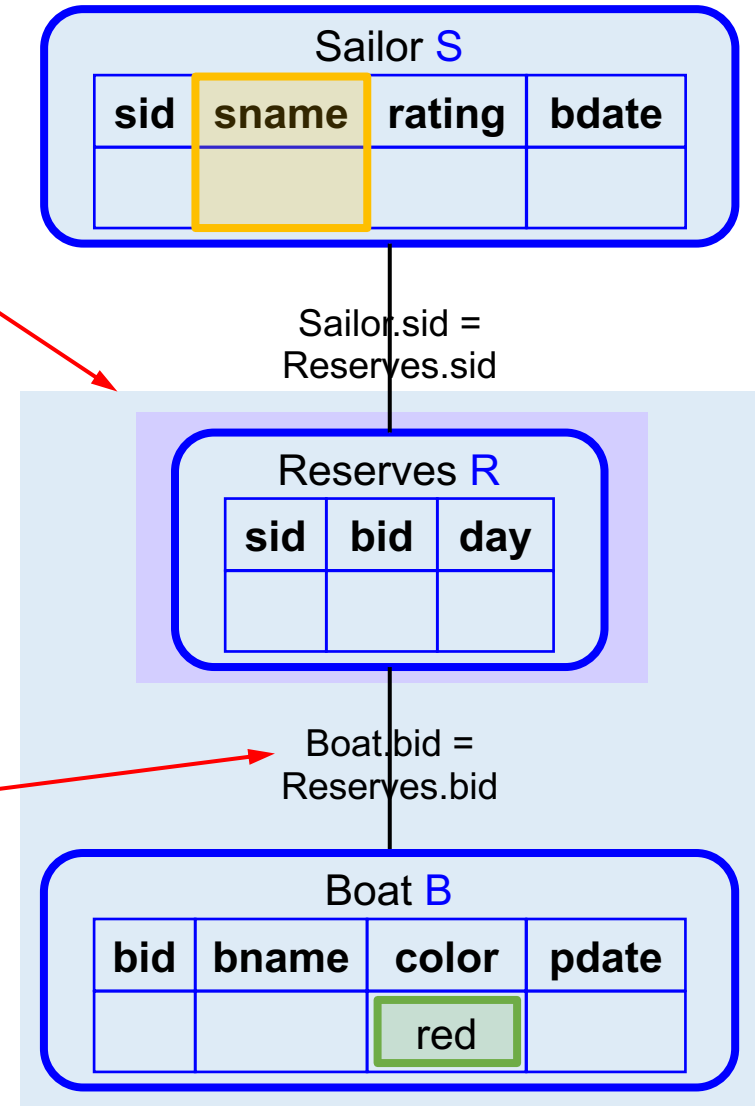
# SQLVis

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S
where exists
  (select *
   from Boat B
   where color = 'red'
   and exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

boxes with different  
saturation drawn for  
subqueries

Join conditions shown as  
atomic label (text) on  
line between tables



# SQLVis

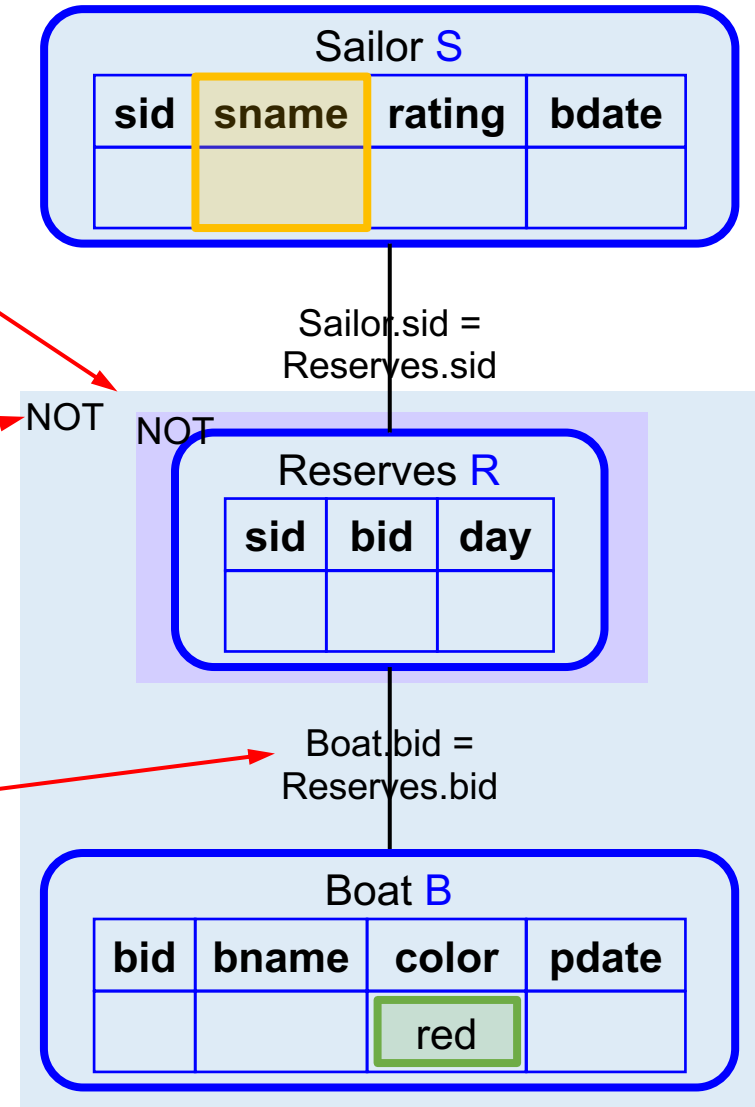
Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and R.bid=B.bid))
```

boxes with different saturation drawn for subqueries

negation for negated subqueries are expressed in words

Join conditions shown as atomic label (text) on line between tables

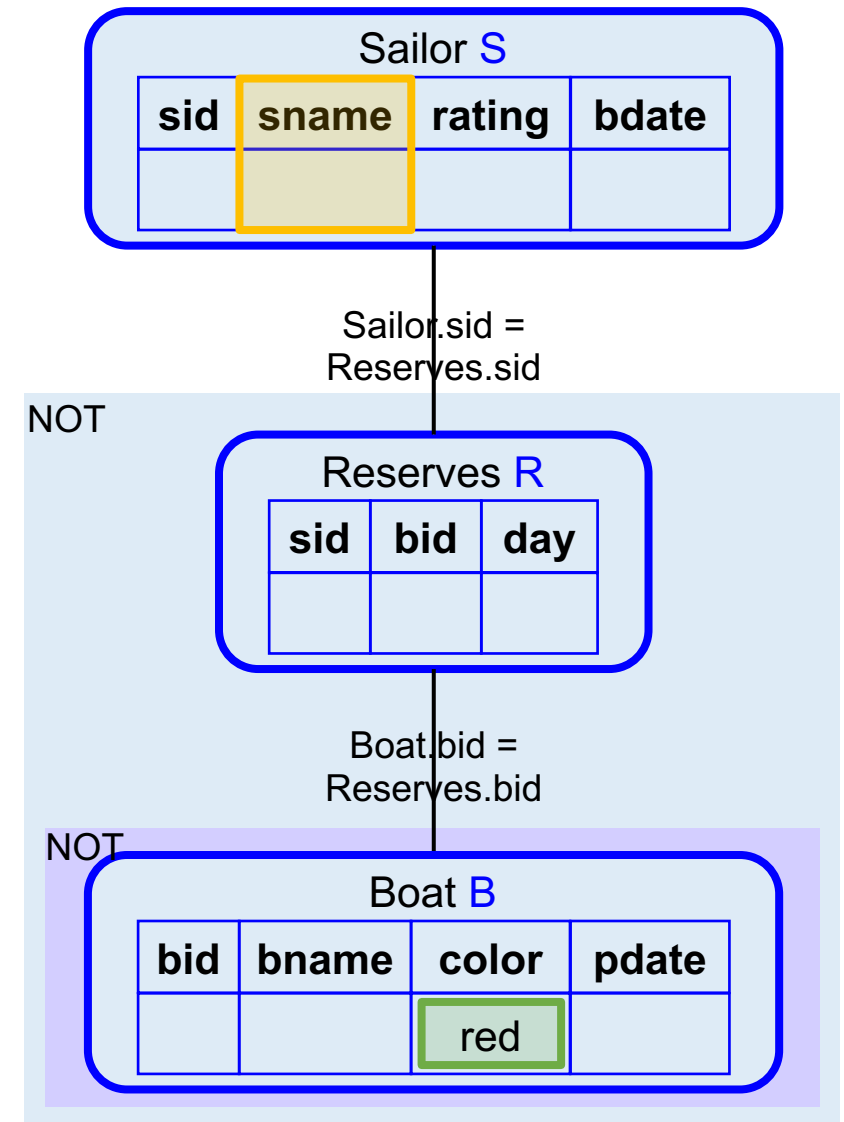




# SQLVis

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid = R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



# SQLVis

Q5: "Find boats  
that are red or blue."

```
select bid, bname  
from RedBoat R  
union  
select bid, bname  
from BlueBoat B
```

A union of queries is  
not supported

## Schema

RedBoat	
<u>bid</u>	
bname	
pdate	

BlueBoat	
<u>bid</u>	
bname	
pdate	

# SQLVis (2021)

## Backup

# SQLVis

```
SELECT *  
FROM store  
WHERE city != London;
```



Fig. 3: SQLVis representation for a simple query (collapsed on the left, expanded in the middle).

# SQLVis

```
SELECT *  
FROM customer AS c  
WHERE city = "Amsterdam" OR city = "Utrecht";
```

customer c			
cID	cName	street	city
			Amsterdam Utrecht

# SQLVis

```
SELECT c.cName  
FROM customer AS c, purchase AS p  
WHERE p.cID = c.cID;
```

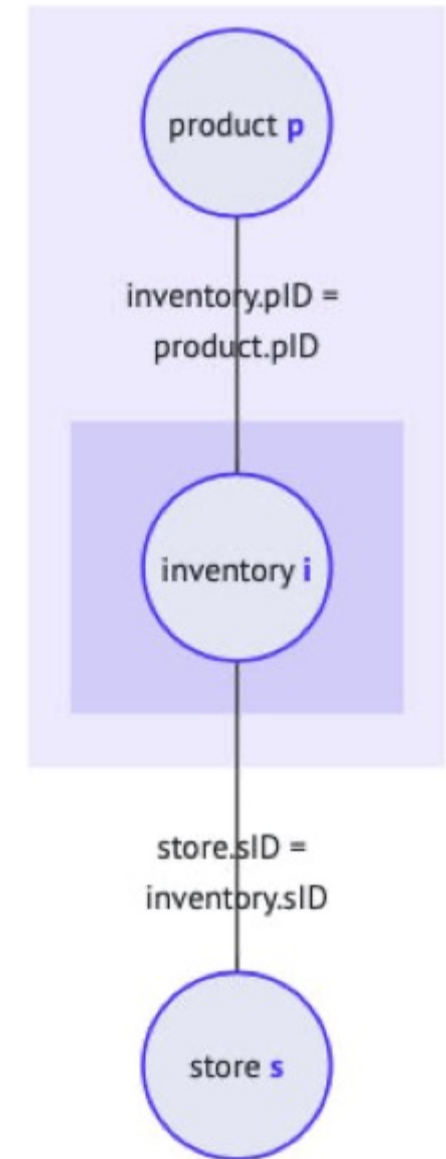


# SQLVis

All complex SQL queries contain subqueries and other types of nesting. To visualize these subqueries in the most intuitive way, SQLVis draws boxes around these subqueries as suggested by Thalheim [38]. To distinguish between different subqueries on the same level, and nested subqueries on different levels, SQLVis draws each level of nesting in a different saturation (see Figure 4). The use of these different colors helps to give an immediate overview of the level of nesting in the query. In case a subquery is negated, for example by using NOT EXISTS or NOT IN, SQLVis displays this negation in words. Other options, such as a different background color or a border for the box led to a very cluttered representation.

```
SELECT s.sID, s.sName
FROM store AS s
WHERE NOT EXISTS (
  SELECT p.pID
  FROM product AS p
  WHERE NOT EXISTS (
    SELECT *
    FROM inventory AS i
    WHERE s.sID = i.sID
    AND i.pID = p.pID))
```

(b) A query to find stores with all items in stock.



# Part 5: Modern Visual Query Representations (after 1970)

1. QBE (1977): Query-By-Example
2. QBD (1990): Query By Diagram
3. TableTalk (1991)
4. OO-VQL (1993): "Object-Oriented" VQL
5. DFQL (1994): DataFlow QL
6. Visual SQL (2003)
7. QueryVis (2011)
8. Dataplay (2012)
9. SIEUFERD (2016)
10. SQLVis (2021)
11. Relational Diagrams (2024)



# Relational Diagrams (2024)

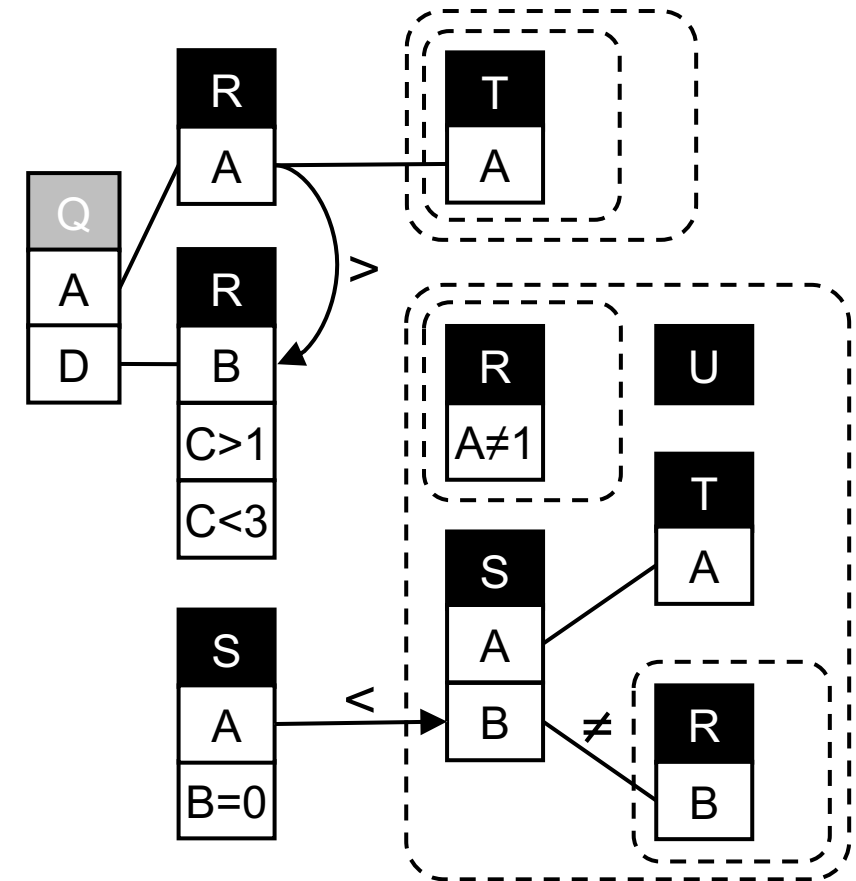
Sources used:

- Gatterbauer, Dunne. On the Reasonable Effectiveness of Relational Diagrams: Explaining Relational Query Patterns and the Pattern Expressiveness of Relational Languages. SIGMOD 2024. <https://dl.acm.org/doi/pdf/10.1145/3639316>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# Relational Diagrams

- "Relational Diagrams" are a variant of QueryVis, that resolves prior ambiguities and that adds expressivity.
- Two key design decisions are: 1) to use Peirce's **nested negation boxes** (instead of using arrow directions), and 2) to add **union boxes**.
- Both together makes Relational Diagrams relationally complete and allows an unambiguous interpretation for any valid Relational diagram. It can also represent Boolean queries (= logical sentences)



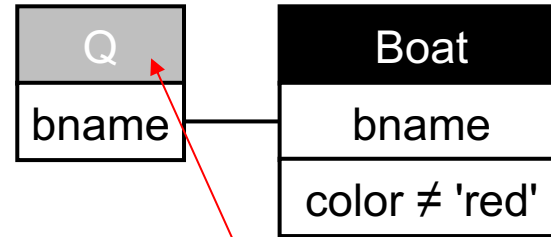
# Relational Diagrams

*Q1b: "Find boats  
that are not red."*

```
select distinct bname  
from Boat  
where color <> 'red'
```

Schema

Boat
<u>bid</u>
bname
color
pdate



The visual formalism for CQs is quasi identical to QueryVis (the Q instead of SELECT on the output table is inspired by TRC)

## TRC (Tuple Relational Calculus)

$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge b.\text{color} \neq \text{'red'}]\}$

# Relational Diagrams

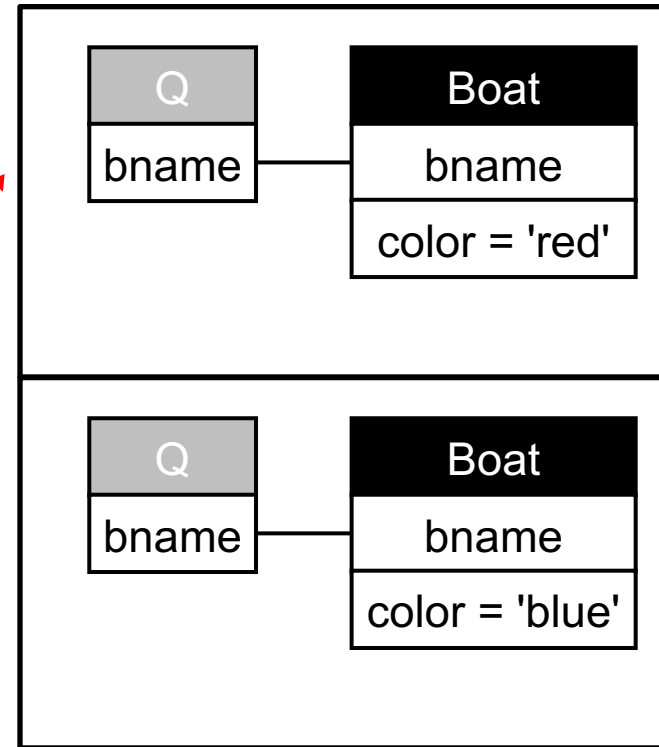
Q1: "Find boats that are red or blue."

```
select distinct bname
from Boat
where color = 'red'
or color = 'blue'
```

Disjunctions are represented via "union cells": Each cell of the canvas then represents only conjunctive information, yet the relation among the different cells is disjunctive (a union of the outputs).

Schema

Boat
<u>bid</u>
bname
color
pdate



inspired by Venn-Peirce graphs

Strongly inspired by handling of disjunctions in Datalog

## TRC (Tuple Relational Calculus)

$$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge (b.\text{color} = \text{'red'} \vee b.\text{color} = \text{'blue'})]\}$$
$$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge b.\text{color} = \text{'red'}] \vee \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge b.\text{color} = \text{'blue'}]\}$$

## Datalog

$Q(x) \text{ :- Boat}(\_, x, \text{'red'}, \_)$   
 $Q(x) \text{ :- Boat}(\_, x, \text{'blue'}, \_)$

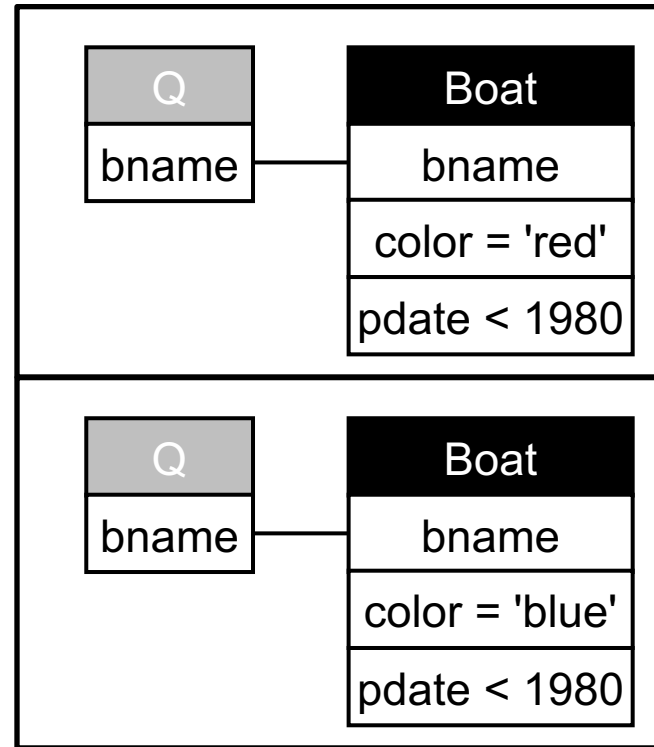
# Relational Diagrams

Schema

Boat
<u>bid</u>
bname
color
pdate

*Q1c: "Find boats that are red or blue and purchased before 1980."*

```
select distinct bname
from Boat
where (color = 'red'
or color = 'blue')
and pdate < 1980
```



## TRC (Tuple Relational Calculus)

$$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge (b.\text{color} = \text{'red'} \vee b.\text{color} = \text{'blue'}) \wedge b.\text{pdate} < 1980]\}$$
$$\{q(\text{bname}) \mid \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge b.\text{color} = \text{'red'} \wedge b.\text{pdate} < 1980]$$
$$\vee \exists b \in \text{Boat} [q.\text{bname} = b.\text{bname} \wedge b.\text{color} = \text{'blue'} \wedge b.\text{pdate} < 1980]\}$$

## Datalog

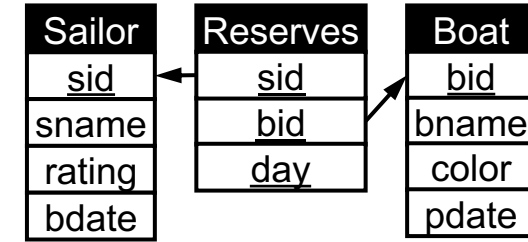
$$Q(x) \text{ :- Boat}(\_, x, \text{'red'}, y), y < 1980$$
$$Q(x) \text{ :- Boat}(\_, x, \text{'blue'}, y), y < 1980$$

# Relational Diagrams

Q2: "Find sailors who reserved a red boat."

```
select distinct S.sname
from Sailor S, Reserves R, Boat B
where S.sid=R.sid
and B.bid=R.bid
and color = 'red'
```

Schema



Relational Diagrams (just like QueryVis) show conjunctive queries just like relational schemas

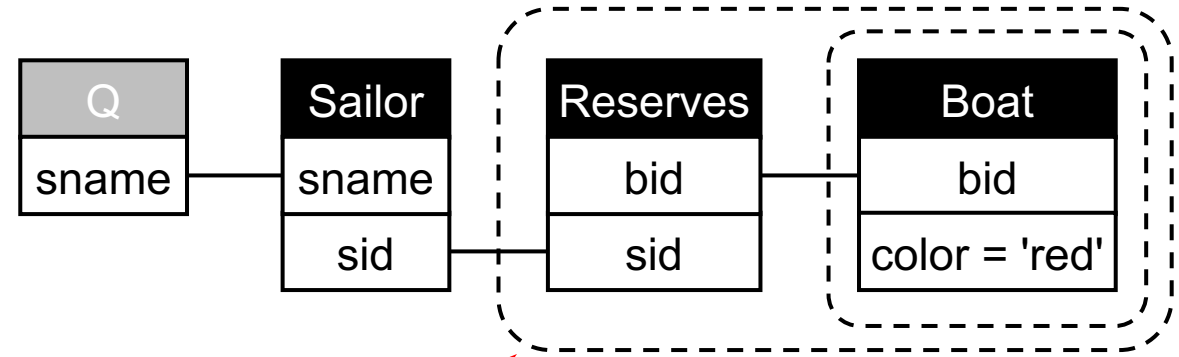
## TRC (Tuple Relational Calculus)

$\{q(\text{sname}) \mid \exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [q.\text{sname} = s.\text{sname} \wedge r.\text{sid} = s.\text{sid} \wedge b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}]\}$

# Relational Diagrams

Q3: "Find sailors who reserved only red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```



Nested dashed boxes represent "not exists" ( $\neg$ ). Similar to Peirce (and in contrast to QueryVis), these boxes are nested, and the nesting represents the negation hierarchy

## TRC (Tuple Relational Calculus)

$\{q(\text{sname}) \mid \exists s \in \text{Sailor}[q.\text{sname} = s.\text{sname} \wedge \neg(\exists r \in \text{Reserves}[r.\text{sid} = s.\text{sid} \wedge \neg(\exists b \in \text{Boat}[b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}])])]\}$

# Relational Diagrams

Q3: "Find sailors who reserved only red boats."

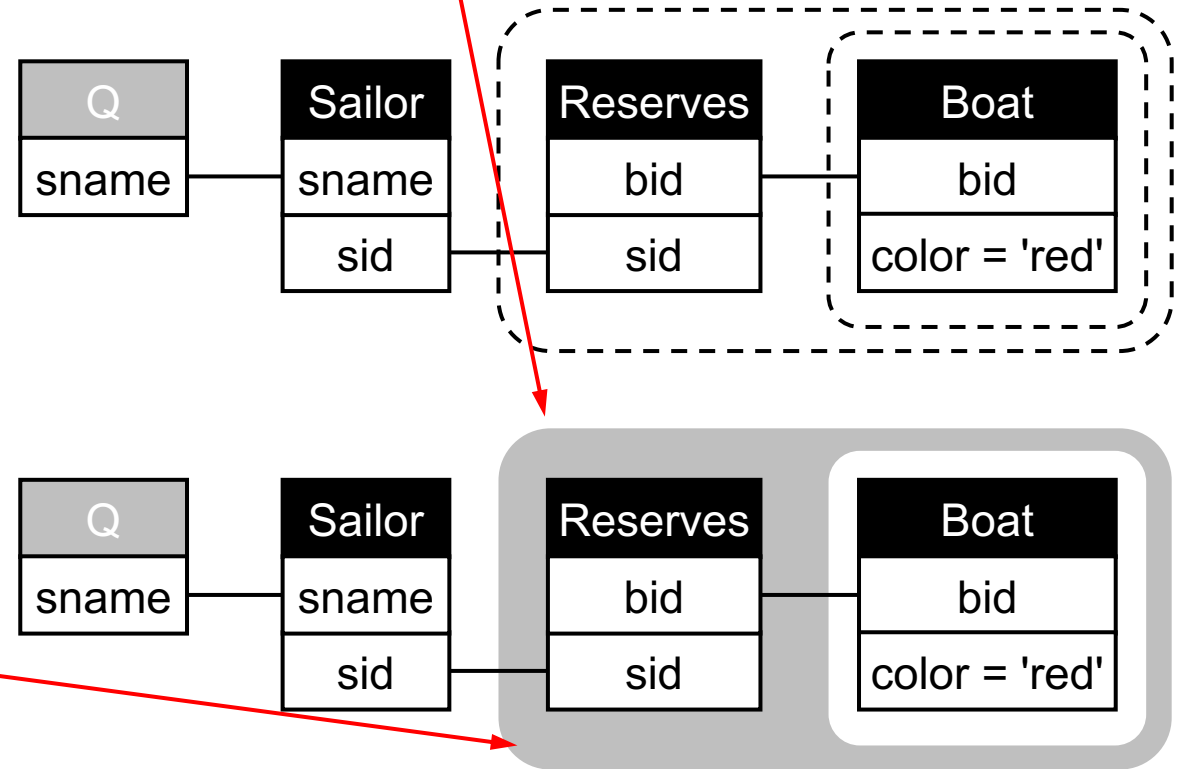
```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Reserves R
   where S.sid=R.sid
   and not exists
     (select *
      from Boat B
      where R.bid=B.bid
      and color = 'red'))
```

A shaded partition that contains a nested white area (called a "scroll" by Peirce) can now be read faster as an "if (shaded) then (nested unshaded)" statement.

Here: "sailors s.t. if they reserved a boat, then it is red"

Relational Diagrams with "Peirce shading":

- Call "negative" (shaded) a partition that is nested in an odd number of negation boxes: 1, 3, 5, ...
- Call "positive" (not shaded) a partition that is nested in an even number of negation boxes, including zero: 0, 2, 4, ...



## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}[q.\text{sname} = s.\text{sname} \wedge \neg(\exists r \in \text{Reserves}[r.\text{sid} = s.\text{sid} \wedge \neg(\exists b \in \text{Boat}[b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}])])]\}$$

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}[q.\text{sname} = s.\text{sname} \wedge (\forall r \in \text{Reserves}[r.\text{sid} = s.\text{sid} \rightarrow (\exists b \in \text{Boat}[b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}])])]\}$$



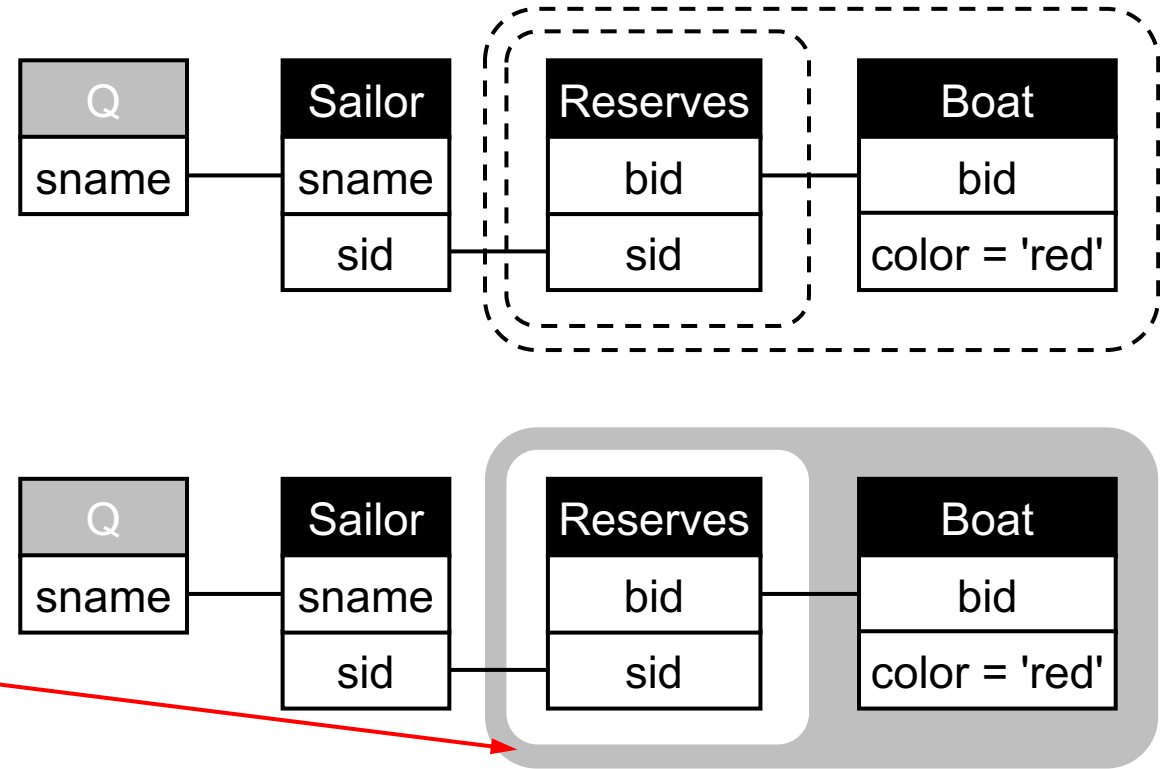
# Relational Diagrams

Q4: "Find sailors who reserved all red boats."

```
select distinct S.sname
from Sailor S
where not exists
  (select *
   from Boat B
   where color = 'red'
   and not exists
     (select *
      from Reserves R
      where S.sid=R.sid
      and B.bid=R.bid))
```

A shaded partition that contains a nested white area (called a "scroll" by Peirce) can now be read faster as an "if (shaded) then (nested unshaded)" statement.

Here: "sailors s.t. if there is a red boat, then they have reserved it"



## TRC (Tuple Relational Calculus)

$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}[q.\text{sname} = s.\text{sname} \wedge \neg(\exists b \in \text{Boat}[b.\text{color} = \text{'red'} \wedge \neg(\exists r \in \text{Reserves}[b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])))]\}$$

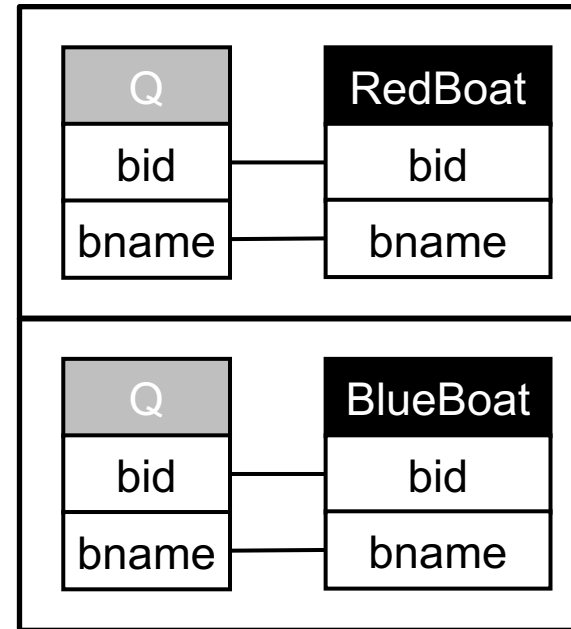
$$\{q(\text{sname}) \mid \exists s \in \text{Sailor}[q.\text{sname} = s.\text{sname} \wedge (\forall b \in \text{Boat}[b.\text{color} = \text{'red'} \rightarrow (\exists r \in \text{Reserves}[b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])))]\}$$

# Relational Diagrams

Q5: "Find boats that are red or blue."

```
select bid, bname
from RedBoat R
union
select bid, bname
from BlueBoat B
```

Unions are represented via "union cells": Each cell of the canvas represents only conjunctive information, yet the relation among the different cells is disjunctive (a union of the outputs).



Schema

RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

Strongly inspired by handling of disjunctions in Datalog

## TRC (Tuple Relational Calculus)

$$\{q(\text{bid}, \text{bname}) \mid \exists b \in \text{RedBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}] \vee \exists b \in \text{BlueBoat} [q.\text{bid} = b.\text{bid} \wedge q.\text{bname} = b.\text{bname}]\}$$

## Datalog

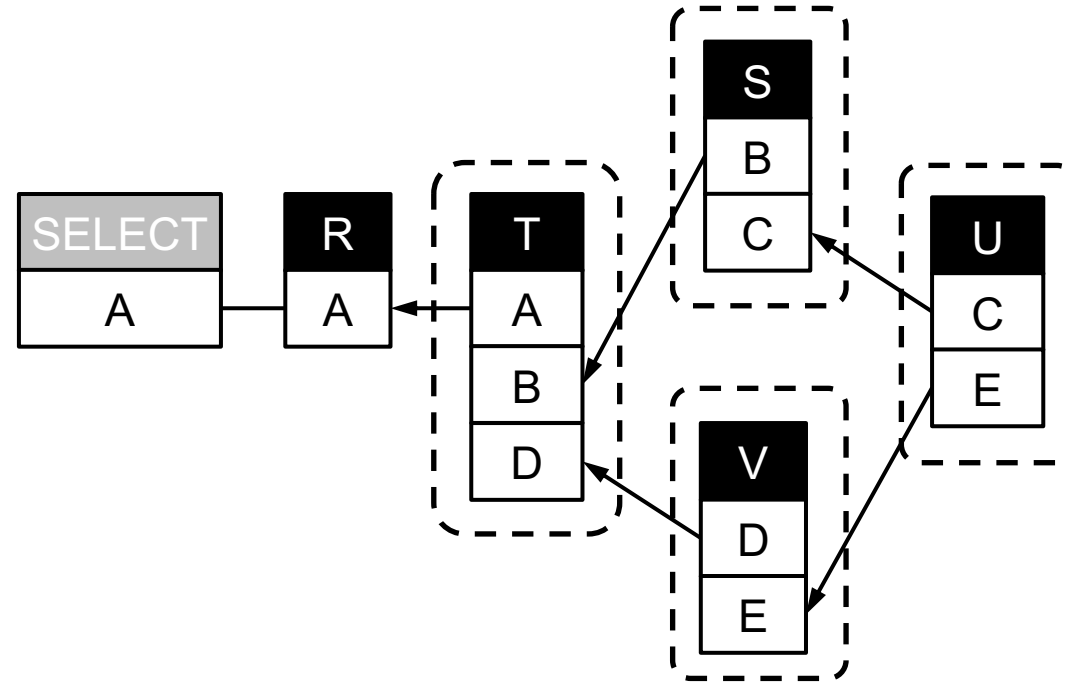
$Q(x, y) \text{ :- RedBoat}(x, y, \_)$   
 $Q(x, y) \text{ :- BlueBoat}(x, y, \_)$

## QueryVis: With nesting depth 4, arrows can become ambiguous

```

select distinct A
from R
where not exists
  (select *
   from S
   where not exists
     (select *
      from T
      where T.A = R.A
      and T.B = S.B
      and not exists
        (select *
         from U
         where U.C = S.C
         and not exists
           (select *
            from V
            where V.D = T.D
            and V.E = U.E))))))

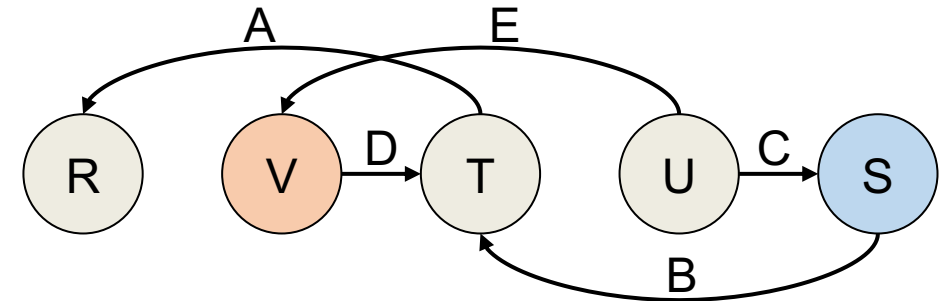
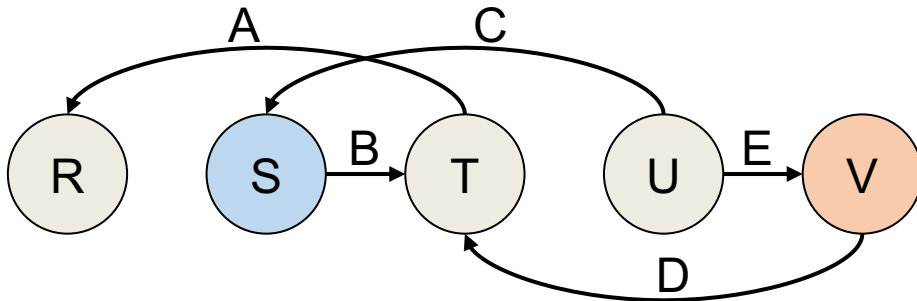
```



```

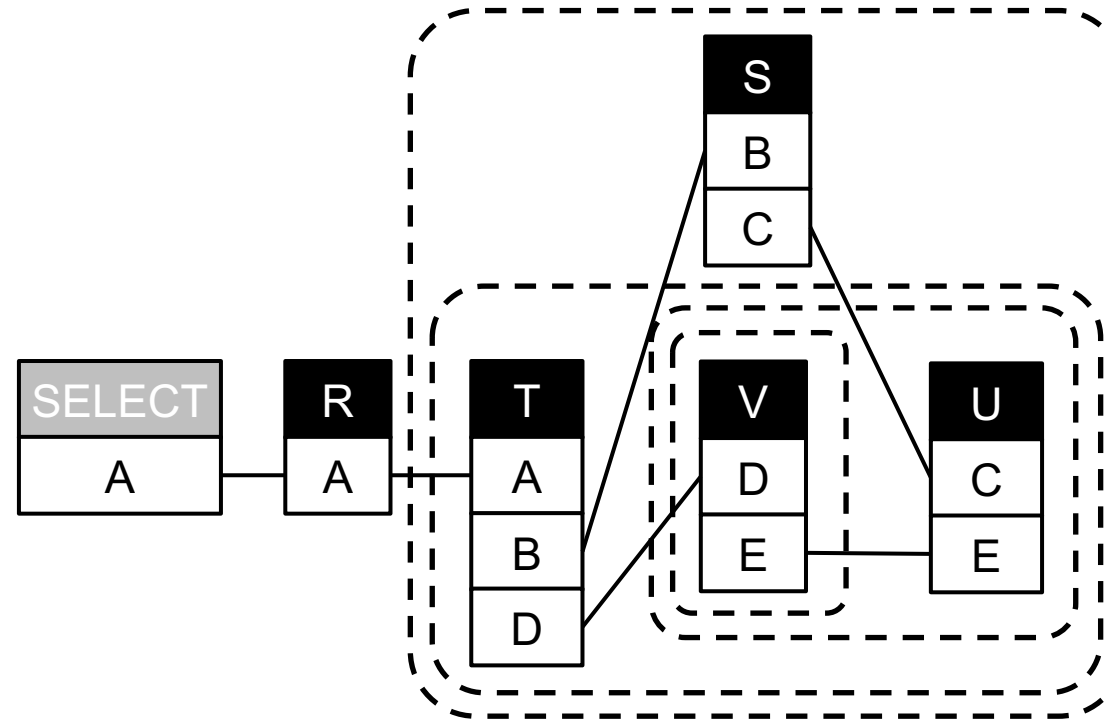
select distinct A
from R
where not exists
  (select *
   from V
   where not exists
     (select *
      from T
      where T.A = R.A
      and T.D = V.D
      and not exists
        (select *
         from U
         where U.E = V.E
         and not exists
           (select *
            from S
            where S.B = T.B
            and S.C = U.C))))

```



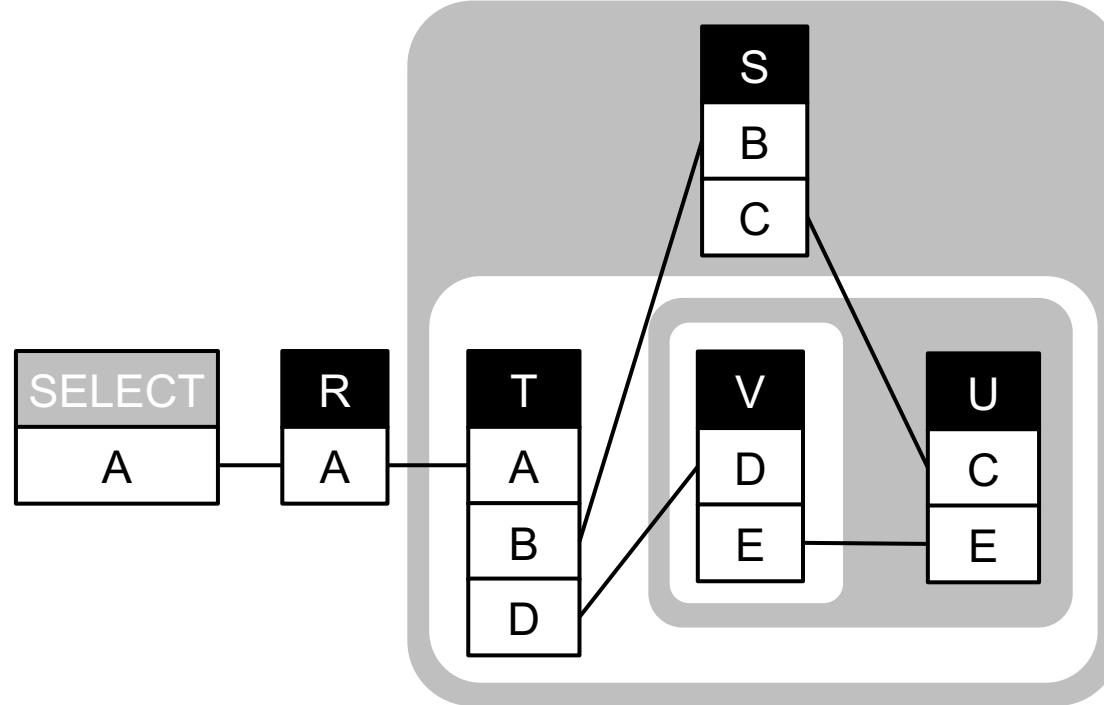
# Relational Diagrams are unambiguous

```
select distinct A
from R
where not exists
  (select *
   from S
   where not exists
     (select *
      from T
      where T.A = R.A
        and T.B = S.B
        and not exists
          (select *
           from U
           where U.C = S.C
            and not exists
              (select *
               from V
               where V.D = T.D
                and V.E = U.E))))))
```



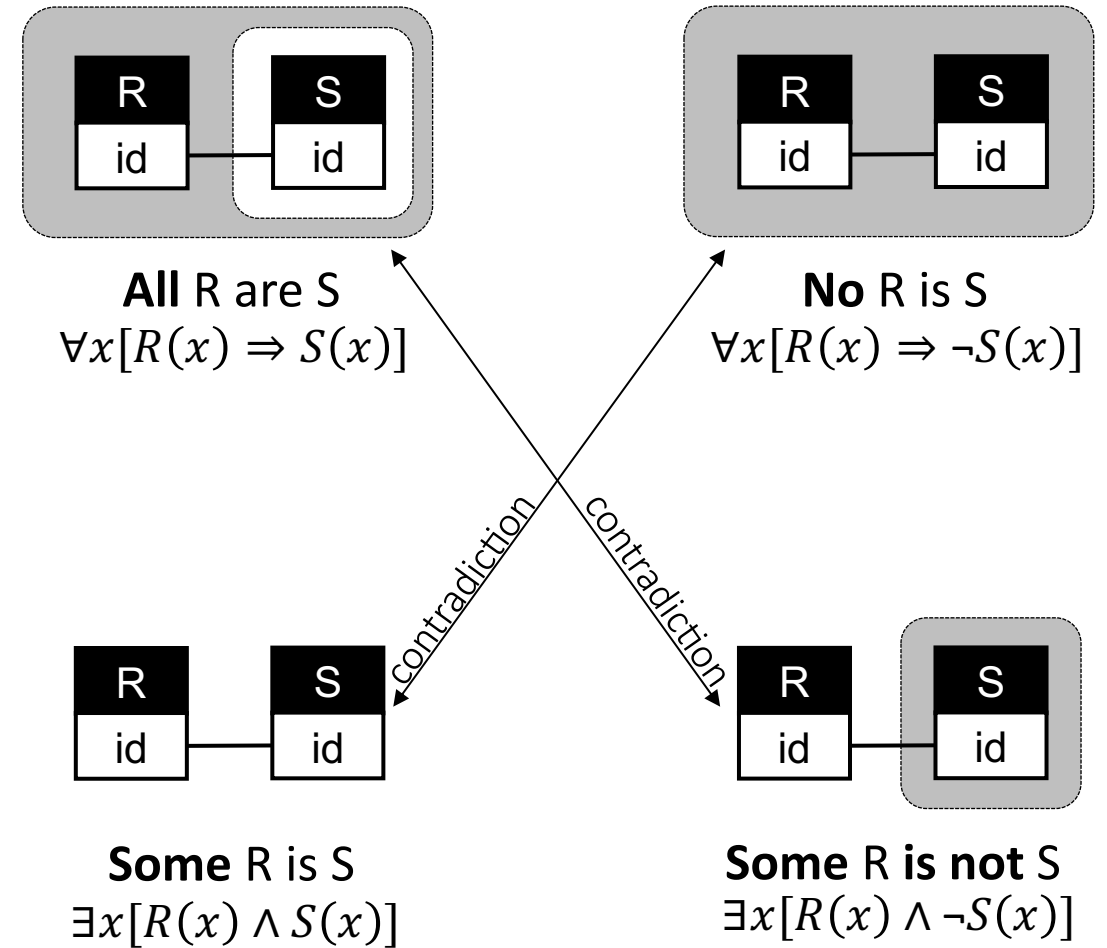
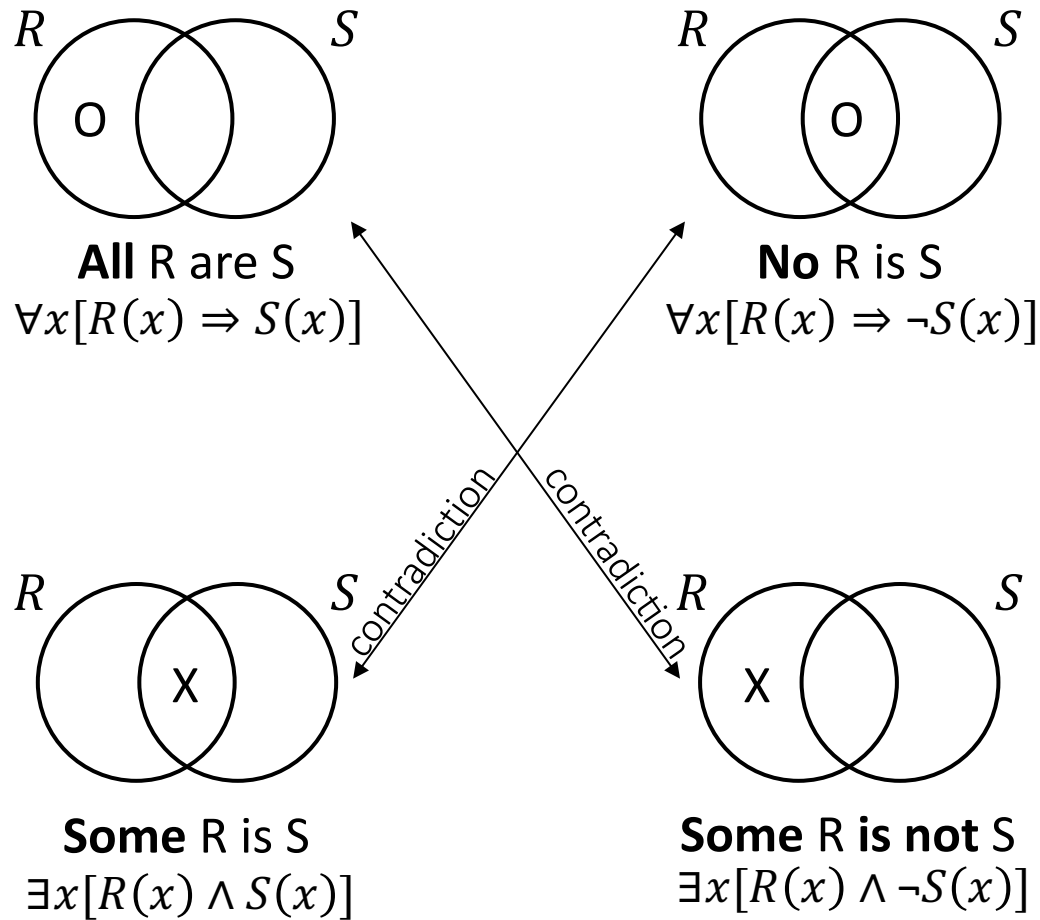
# Relational Diagrams are unambiguous

```
select distinct A
from R
where not exists
  (select *
   from S
   where not exists
     (select *
      from T
      where T.A = R.A
            and T.B = S.B
            and not exists
              (select *
               from U
               where U.C = S.C
                     and not exists
                       (select *
                        from V
                        where V.D = T.D
                              and V.E = U.E))))))
```

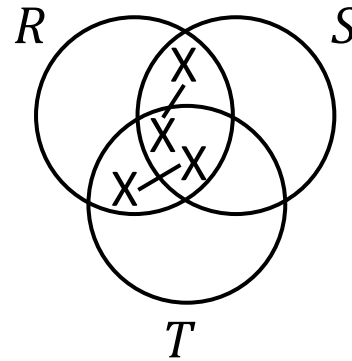


# Relational Diagrams vs. Venn-Peirce

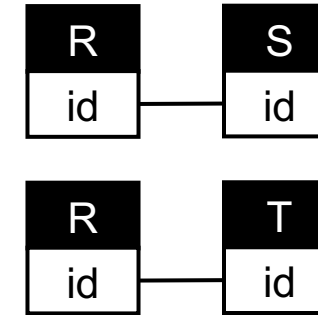
# Venn-Peirce vs. Relational Diagrams



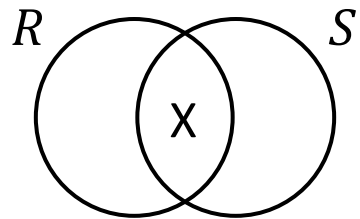
# Venn-Peirce vs. Relational Diagrams



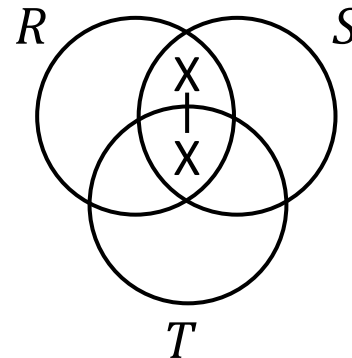
**Some R is S, and some R is T**  
 $\exists x[R(x) \wedge S(x)] \wedge \exists z[R(z) \wedge T(z)]$



**Some R is S, and some R is T**  
 $\exists x[R(x) \wedge S(x)] \wedge \exists z[R(z) \wedge T(z)]$



**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$



**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$



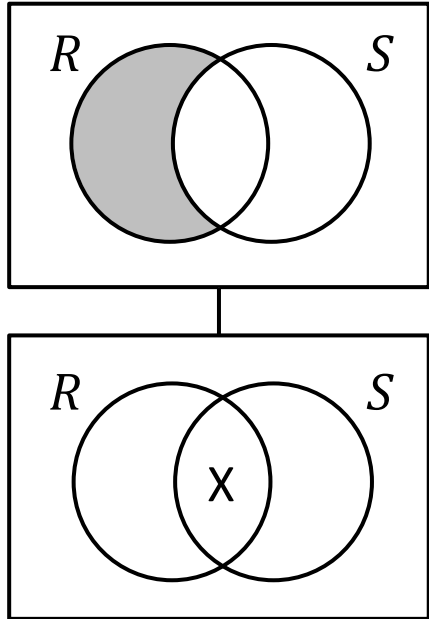
**Some R is S**  
 $\exists x[R(x) \wedge S(x)]$

Relational Diagrams don't show  
 predicates that are not used

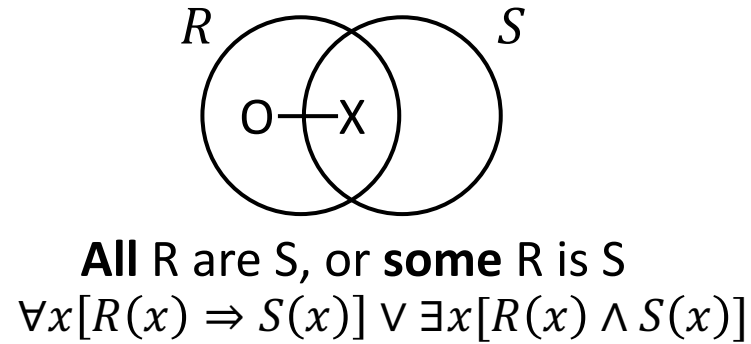


# Venn-Peirce vs. Relational Diagrams

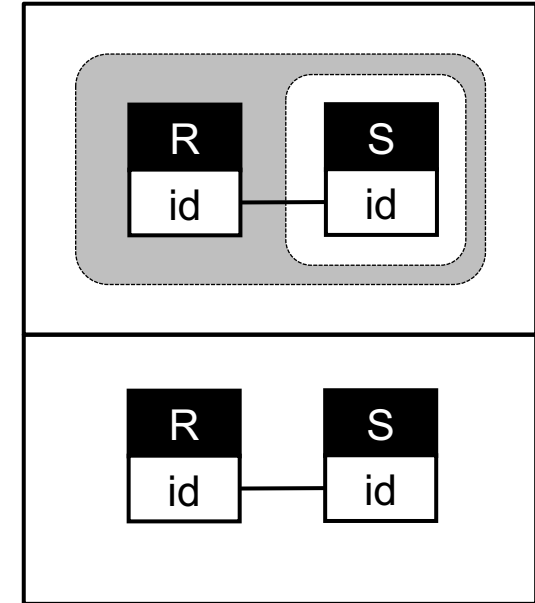
Venn-Peirce-Shin ("Venn-2")



Venn-Peirce

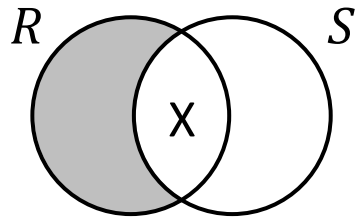


Relational Diagrams

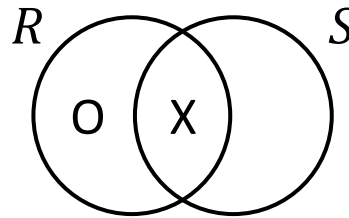


# Venn-Peirce vs. Relational Diagrams

Venn-Peirce-Shin ("Venn-2")

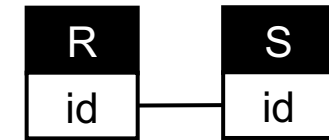
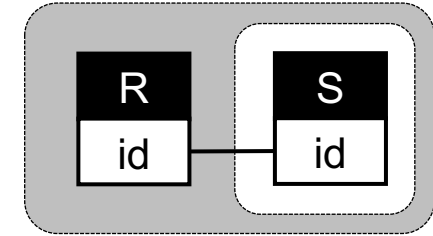


Venn-Peirce



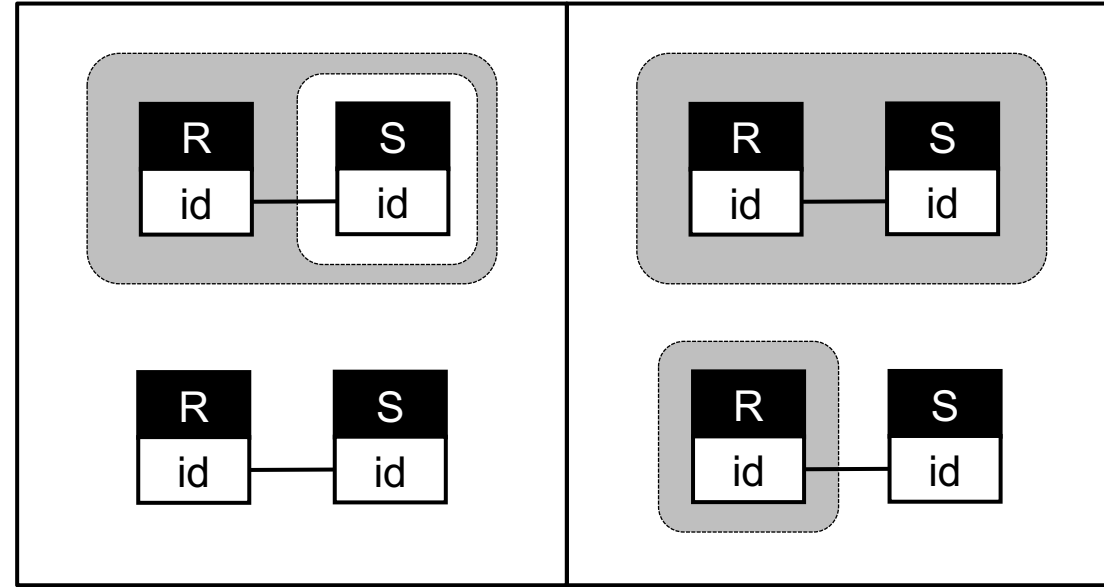
**All R are S, and some R is S**  
 $\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]$

Relational Diagrams



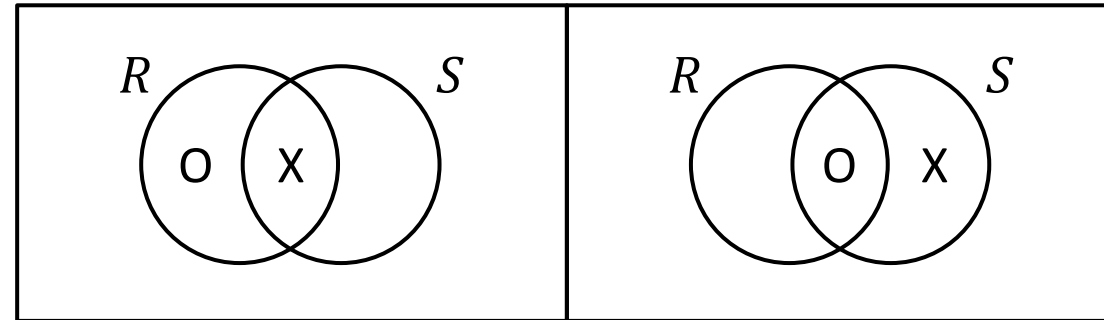
Relational Diagrams are "isomorphic" to non-disjunctive Relational Tuple Calculus. For a formal definition of "pattern isomorphisms" and "non-disjunctive Calculus" see [Gatterbauer,Dunne'24]

# Venn-Peirce vs. Relational Diagrams



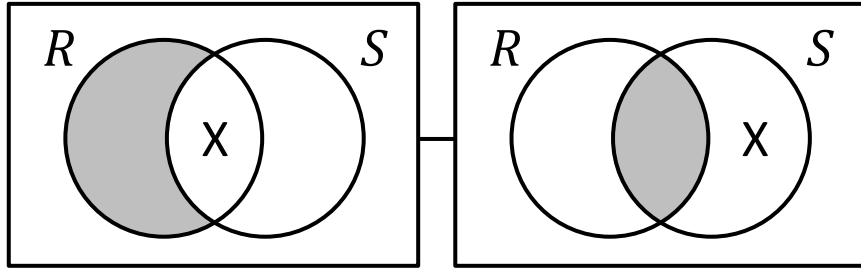
DNF

$$(\forall x[R(x) \Rightarrow S(x)] \wedge \exists x[R(x) \wedge S(x)]) \vee (\forall x[R(x) \Rightarrow \neg S(x)] \wedge \exists x[S(x) \wedge \neg R(x)])$$

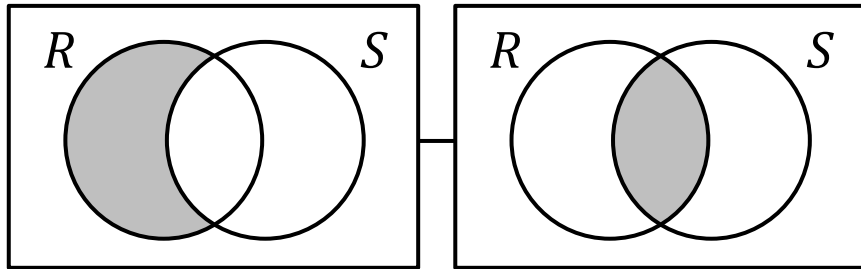


# Venn-Peirce-Shin (Venn-II) vs. Relational Diagrams

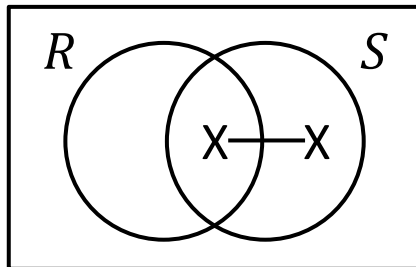
## Venn-Peirce-Shin ("Venn-II")



(**All** R are S, and **some** R is S) or (**No** R is S, and **some** S is **not** R)

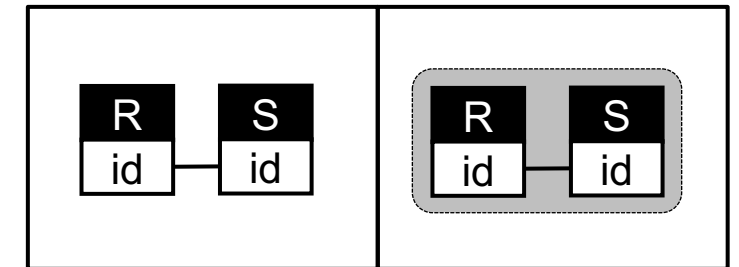
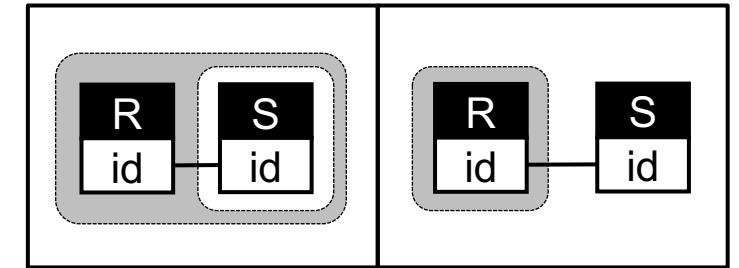
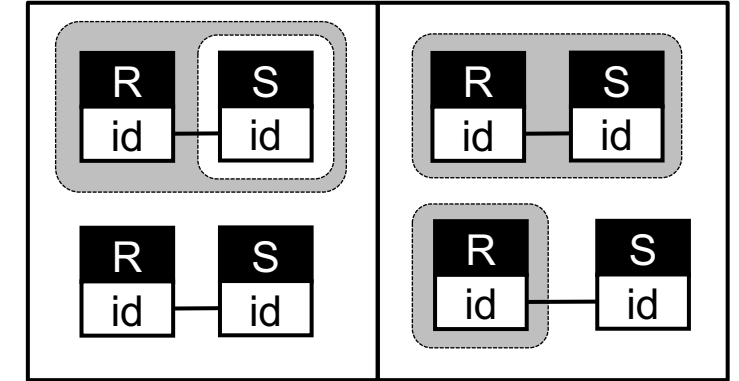


(**All** R are S) or (**no** R is S)

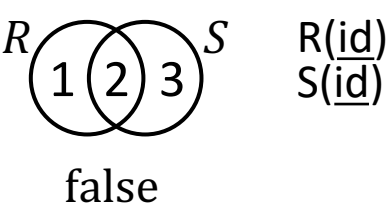


(**Some** R is S) or (**some** S is **not** R)

## Relational Diagrams



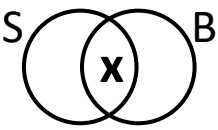
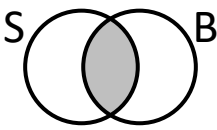
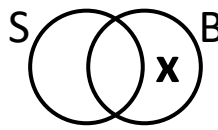
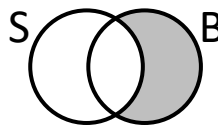
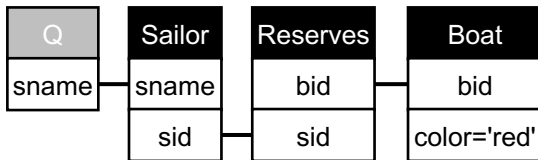
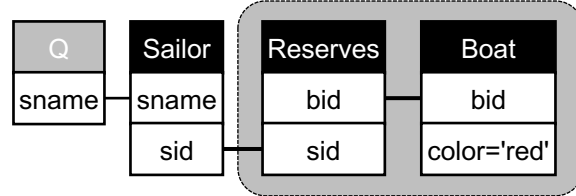
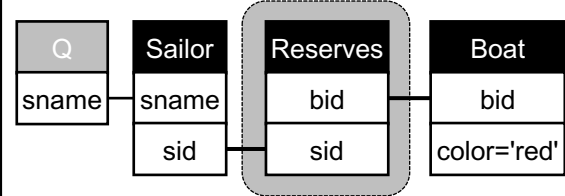
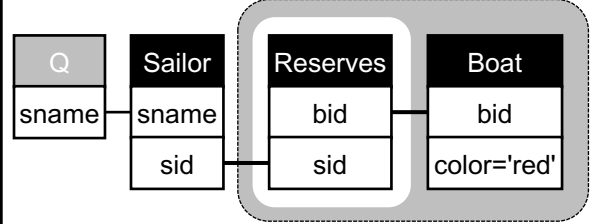
# 4 categorical propositions w/ Relational Diagrams



	true	false	true	false
Venn-Peirce				
Relational Calculus	$\exists x[R(x) \wedge S(x)]$	$\neg \exists x[R(x) \wedge S(x)]$	$\exists x[R(x) \wedge \neg S(x)]$	$\neg \exists x[R(x) \wedge \neg S(x)]$
NL	Some $R$ is $S$ .	No $R$ is $S$ . (All $R$ are not $S$ )	Some $R$ is not $S$ .	All $R$ are $S$ .
SQL	<pre>SELECT EXISTS(   SELECT *   FROM R, S   WHERE R.id = S.id)</pre>	<pre>SELECT NOT EXISTS(   SELECT *   FROM R, S   WHERE R.id = S.id)</pre>	<pre>SELECT EXISTS(   SELECT *   FROM R   WHERE NOT EXISTS(     SELECT *     FROM S     WHERE R.id = S.id))</pre>	<pre>SELECT NOT EXISTS(   SELECT *   FROM R   WHERE NOT EXISTS(     SELECT *     FROM S     WHERE R.id = S.id))</pre>
Relational Diagram				

# 4 categorical propositions with Sailors

Sailor (sid, sname, rating, age)  
Reserves (sid, bid, day)  
Boat (bid, bname, color)

Cat.	 <p>Some <math>S</math> is <math>B</math>. <math>\exists x[S(x) \wedge B(x)]</math></p>	 <p>No <math>S</math> is <math>B</math>. (All <math>S</math> are not <math>B</math>) <math>\neg \exists x[S(x) \wedge B(x)]</math></p>	 <p>Some <math>B</math> is not <math>S</math>. <math>\exists x[B(x) \wedge \neg S(x)]</math></p>	 <p>All <math>B</math> are <math>S</math>. <math>\neg \exists x[B(x) \wedge \neg S(x)]</math></p>
NL	Sailors who reserved <b>some</b> red boat	Sailors who did <b>not</b> reserve <b>any</b> red boat	Sailors who did <b>not</b> reserve <b>all</b> red boats	Sailors who reserved <b>all</b> red boats
SQL	<pre>SELECT S.sname FROM Sailor S WHERE EXISTS(   SELECT *   FROM Reserves R   WHERE R.sid = S.sid   AND EXISTS(     SELECT *     FROM Boat B     WHERE B.color = 'red'     AND B.bid = R.bid))</pre>	<pre>SELECT S.sname FROM Sailor S WHERE NOT EXISTS(   SELECT *   FROM Reserves R   WHERE R.sid = S.sid   AND EXISTS(     SELECT *     FROM Boat B     WHERE B.color = 'red'     AND B.bid = R.bid))</pre>	<pre>SELECT S.sname FROM Sailor S WHERE EXISTS(   SELECT *   FROM Boat B   WHERE B.color = 'red'   AND NOT EXISTS(     SELECT *     FROM Reserves R     WHERE R.bid = B.bid     AND R.sid = S.sid))</pre>	<pre>SELECT S.sname FROM Sailor S WHERE NOT EXISTS(   SELECT *   FROM Boat B   WHERE B.color = 'red'   AND NOT EXISTS(     SELECT *     FROM Reserves R     WHERE R.bid = B.bid     AND R.sid = S.sid))</pre>
RD				

# Relational Diagrams vs. Beta EGs

# Beta EGs vs. Relational Diagrams

*S: "There is a red boat."*

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)]$

$\exists b \in \text{Boat} [b.\text{color} = \text{'red'}]$

?

?

Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate



# Beta EGs vs. Relational Diagrams

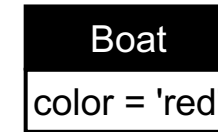
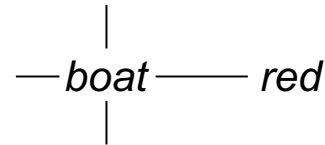
Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

*S: "There is a red boat."*

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)]$

$\exists b \in \text{Boat} [b.\text{color} = \text{'red'}]$



*S: "There is a boat."*

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$

$\exists b \in \text{Boat}$



# Beta EGs vs. Relational Diagrams

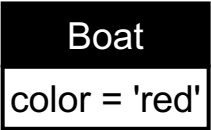
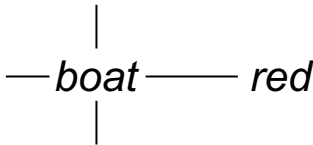
Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

*S: "There is a red boat."*

$\exists x,y,u [\text{Boat}(x,y,\text{'red'},u)]$

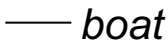
$\exists b \in \text{Boat} [b.\text{color}=\text{'red'}]$



*S: "There is a boat."*

$\exists x,y,z,u [\text{Boat}(x,y,z,u)]$

$\exists b \in \text{Boat}$



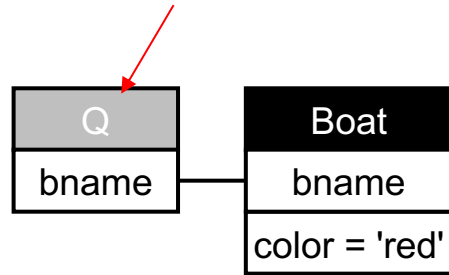
In Relational Diagrams, lines (of identity) are  
\*not\* necessary for existential quantification

# Beta EGs vs. Relational Diagrams

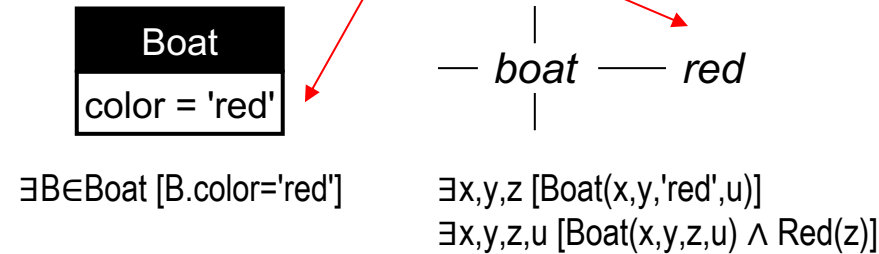
Schema

Boat
bid
bname
color
pdate

1. Beta EGs cannot represent queries (lines represent quantified variables)

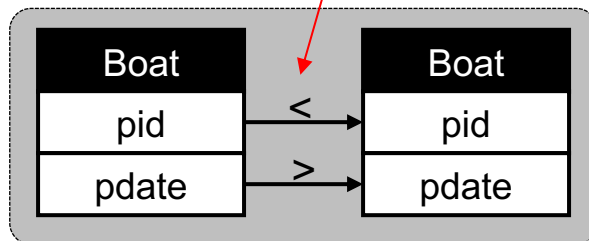


2. Beta EGs cannot represent constants (need dedicated predicates)



3. Beta EGs follow the convention of standard FOL, which corresponds to DRC (unnamed perspective). Thus all attributes need to be quantified and shown as lines.

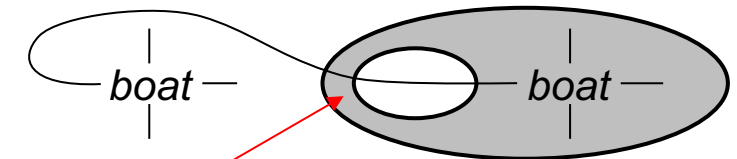
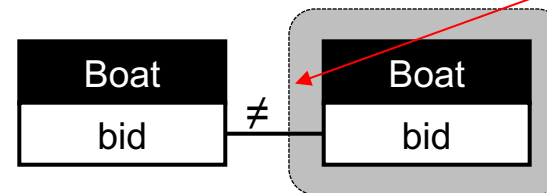
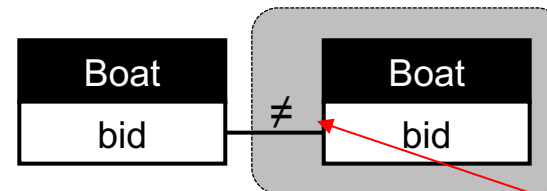
4. Beta EGs cannot represent comparison predicates (only equality = identity)



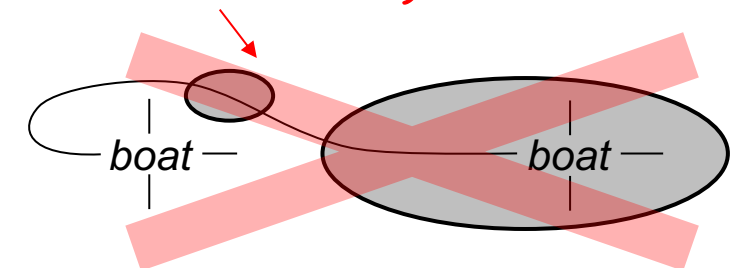
S: "The boat ids are in ascending order the purchase dates."

5. Lines of Identify (LIs) in Beta EGs have multiple meanings: existential quantification and identity = equality. This makes interpretation error-prone

S: "There is only one boat."



Position of inequality does not matter for Relational Diagrams. But the two shown Beta EGs have *different* meanings



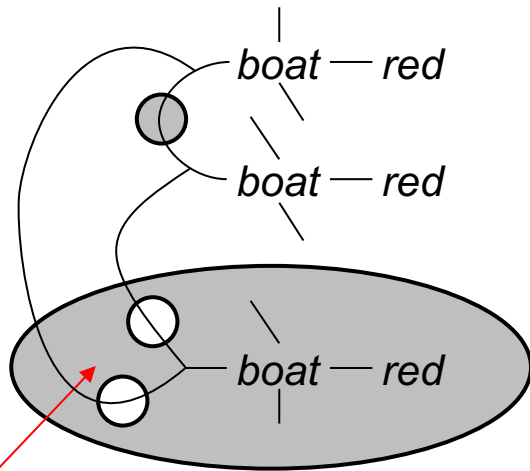
# Beta EGs vs. Relational Diagrams

Schema

	Boat
1	<u>bid</u>
2	bname
3	color
4	pdate

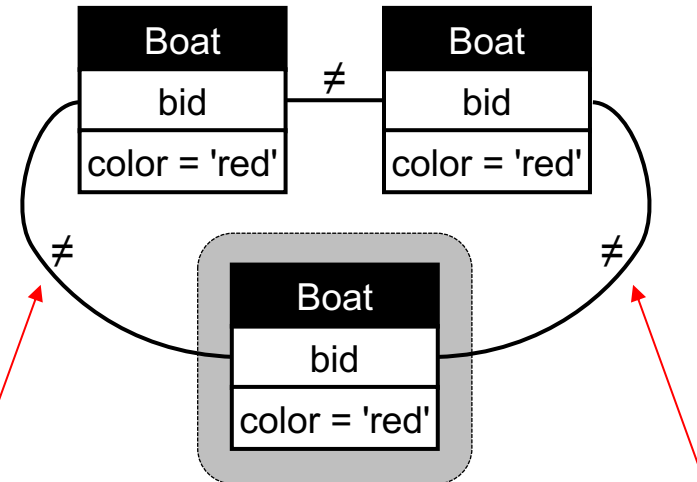
*S: "There are exactly two red boats."*

$$\exists x,y,z,s,t,p [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,\text{'red'},p) \wedge x \neq s \wedge \neg(\exists u,v,w, [\text{Boat}(u,v,\text{'red'},w) \wedge u \neq x \wedge u \neq s])]$$

$$\exists x,y,z,s,t,p [\text{Boat}(x,y,\text{'red'},z) \wedge \text{Boat}(s,t,\text{'red'},p) \wedge x \neq s \wedge \forall u,v,w, [\text{Boat}(u,v,\text{'red'},w) \rightarrow (u=x \vee u=s)]]$$


The placement of the two cuts *\*inside\** the larger one is important; placing them outside instead would give an incorrect semantics.

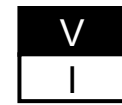
$$\exists b_1 \in \text{Boat}, \exists b_2 \in \text{Boat} [b_1.\text{color} = \text{'red'} \wedge b_2.\text{color} = \text{'red'} \wedge b_1.\text{bid} \neq b_2.\text{bid} \wedge \neg(\exists b_3 \in \text{Boat} [b_3.\text{color} = \text{'red'} \wedge b_1.\text{bid} \neq b_3.\text{bid} \wedge b_2.\text{bid} \neq b_3.\text{bid}])]$$

$$\exists b_1 \in \text{Boat}, \exists b_2 \in \text{Boat} [b_1.\text{color} = \text{'red'} \wedge b_2.\text{color} = \text{'red'} \wedge b_1.\text{bid} \neq b_2.\text{bid} \wedge \forall b_3 \in \text{Boat} [b_3.\text{color} = \text{'red'} \rightarrow (b_1.\text{bid} = b_3.\text{bid} \vee b_2.\text{bid} = b_3.\text{bid})]]$$


The inequality signs are labels of their respective lines; thus their placement inside or outside negation boxes does *\*not\** affect the interpretation of the diagram

# Beta EGs vs. Relational Diagrams

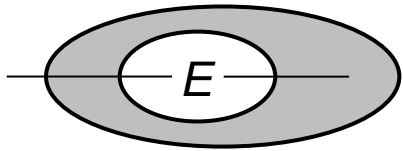
Directed (E)dgges with  
(S)ource and (T)arget



Schema  
(V)ertices contain  
the domain = union of  
values in E.S and E.T

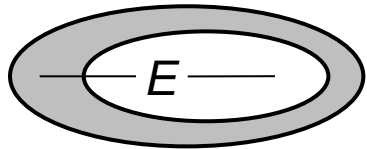
## Beta EGs and Domain Relational Calculus

S: "There is a node that points to all nodes."



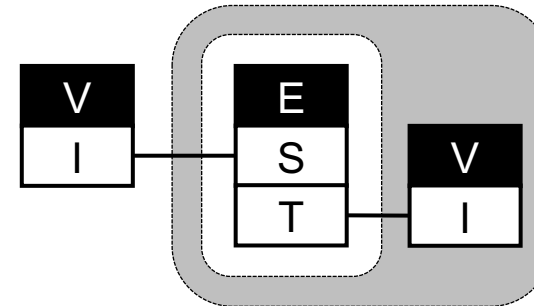
$$\begin{aligned} \exists x \quad \forall y [E(x,y)] \\ \exists x [\neg(\exists y [E(x,y)])] \end{aligned}$$

S: "All nodes are connected to some node."



$$\begin{aligned} \forall x \quad \exists y [E(x,y)] \\ \neg(\exists x [\neg(\exists y [E(x,y)])]) \end{aligned}$$

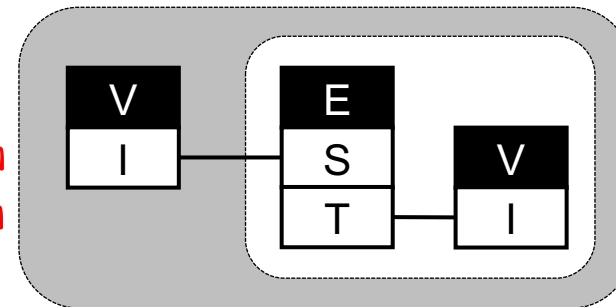
## Relational Diagrams and Tuple Relational Calculus



Notice that both TRC  
and RD make the  
domains always explicit

$$\begin{aligned} \exists v_1 \in V [ \quad \forall v_2 \in V [ \quad \exists e \in E [e.S=v_1.I \wedge e.T=v_2.I] \quad ] \\ \exists v_1 \in V [ \neg(\exists v_2 \in V [ \neg(\exists e \in E [e.S=v_1.I \wedge e.T=v_2.I]) ) ] \\ \exists e_1 \in E [ \neg(\exists e_2 \in V [ \neg(\exists e \in E [e.S=e_1.S \wedge e.T=e_2.S]) ) ] \end{aligned}$$

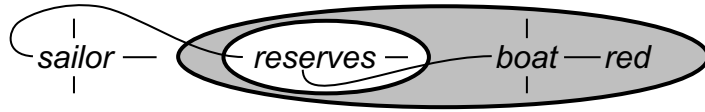
Variant without  
the vertex relation  
if all nodes have an  
outgoing edge



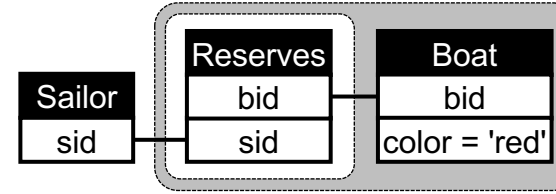
$$\begin{aligned} \neg(\exists v_1 \in V [ \quad \forall v_2 \in V, \forall e \in E [e.S=v_1.I \wedge e.T=v_2.I] \quad ] \\ \neg(\exists v_1 \in V [ \neg(\exists v_2 \in V, \exists e \in E [e.S=v_1.I \wedge e.T=v_2.I]) ) ] \\ \neg(\exists e_1 \in V [ \neg(\exists e_2 \in V, \exists e \in E [e.S=e_1.S \wedge e.T=e_2.S]) ) ] \end{aligned}$$

# Beta EGs vs. Relational Diagrams

~Q4: "There is a sailor who reserved all red boats."



$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \neg(\exists y, u, s [Boat(y, u, 'red', s) \wedge \neg(\exists t [Reserves(v, y, t)])])]$$

$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \forall y, u, s [Boat(y, u, 'red', s) \rightarrow (\exists t [Reserves(v, y, t)])]]$$


$$\exists s \in \text{Sailor} [\neg(\exists b \in \text{Boat} [b.\text{color} = 'red' \wedge \neg(\exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}]) )]$$

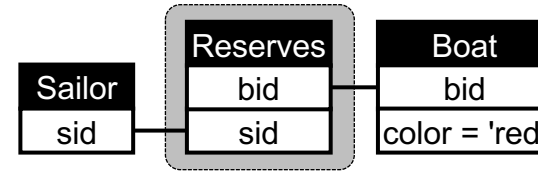
$$\exists s \in \text{Sailor} [ \forall b \in \text{Boat} [b.\text{color} = 'red' \rightarrow \exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid} ] ] ]$$

Schema

Sailor	Reserves	Boat
1 sid	sid	bid
2 sname	bid	bname
3 rating	day	color
4 bdate		pdate

"There is a sailor who did not reserve all red boats."



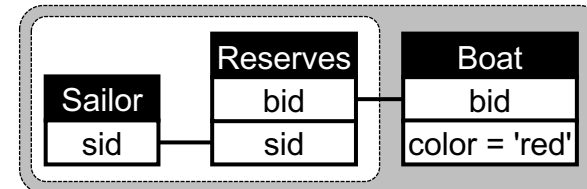
$$\exists x, v, z, w, y, u, s [Sailor(v, x, z, w) \wedge Boat(y, u, 'red', s) \wedge \neg(\exists t [Reserves(v, y, t)])]$$


$$\exists s \in \text{Sailor}, \exists b \in \text{Boat} [b.\text{color} = 'red' \wedge \neg(\exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])]$$

"All red boats were reserved by some sailors."



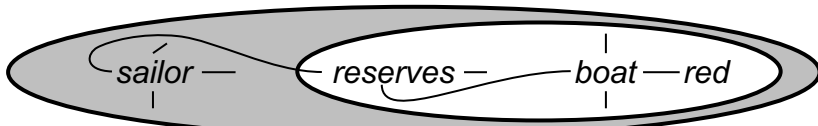
$$\neg(\exists y, u, s [Boat(y, u, 'red', s) \wedge \neg(\exists v, t, x, z, w [Reserves(v, y, t) \wedge Sailor(v, x, z, w)])])$$

$$\forall y, u, s [Boat(y, u, 'red', s) \rightarrow (\exists v, t, x, z, w [Reserves(v, y, t) \wedge Sailor(v, x, z, w)])]$$


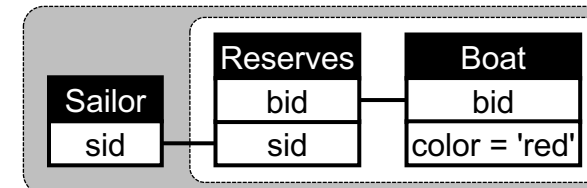
$$\neg(\exists b \in \text{Boat} [b.\text{color} = 'red' \wedge \neg(\exists s \in \text{Sailor}, \exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])])$$

$$\forall b \in \text{Boat} [b.\text{color} = 'red' \rightarrow \exists s \in \text{Sailor}, \exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}]]$$

"All sailors have reserved some red boat."



$$\neg(\exists x, v, z, w [Sailor(v, x, z, w) \wedge \neg(\exists y, u, s, t [Reserves(v, y, t) \wedge Boat(y, u, 'red', s)])])$$

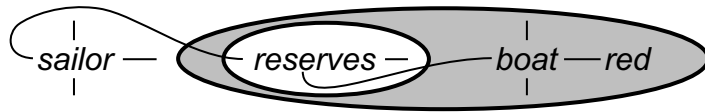
$$\forall x, v, z, w [Sailor(v, x, z, w) \rightarrow (\exists y, u, s, t [Reserves(v, y, t) \wedge Boat(y, u, 'red', s)])]$$


$$\neg(\exists s \in \text{Sailor} [\neg(\exists b \in \text{Boat}, \exists r \in \text{Reserves} [b.\text{color} = 'red' \wedge b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}])])$$

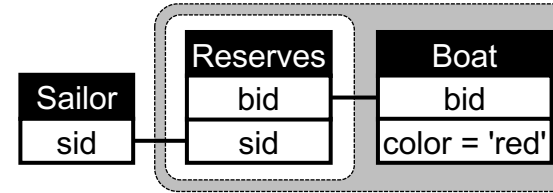
$$\forall s \in \text{Sailor} [ \exists b \in \text{Boat}, \exists r \in \text{Reserves} [b.\text{color} = 'red' \wedge b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}]]$$

# Beta EGs vs. Relational Diagrams

~Q4: "There is a sailor who reserved all red boats."



$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \neg(\exists y, u, s [Boat(y, u, 'red', s) \wedge \neg(\exists t [Reserves(v, y, t)])])]$$

$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \forall y, u, s [Boat(y, u, 'red', s) \rightarrow (\exists t [Reserves(v, y, t)])]]$$


$$\exists s \in \text{Sailor} [\neg(\exists b \in \text{Boat} [b.\text{color} = 'red' \wedge \neg(\exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid}]) )]$$

$$\exists s \in \text{Sailor} [ \forall b \in \text{Boat} [b.\text{color} = 'red' \rightarrow \exists r \in \text{Reserves} [b.\text{bid} = r.\text{bid} \wedge r.\text{sid} = s.\text{sid} ] ] ]$$

Schema

Sailor	Reserves	Boat
1 sid	sid	bid
2 sname	bid	bname
3 rating	day	color
4 bdate		pdate

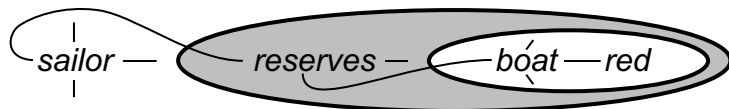
~Q2: "There is a sailor who reserved a red boat."



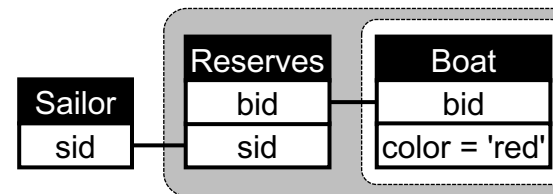
$$\exists x, v, z, w, y, t, u, s [Sailor(v, x, z, w) \wedge \exists y, t [Reserves(v, y, t) \wedge \exists u, s [Boat(y, u, 'red', s)]]]$$


$$\exists s \in \text{Sailor}, \exists r \in \text{Reserves}, \exists b \in \text{Boat} [s.\text{sid} = r.\text{sid} \wedge r.\text{bid} = b.\text{bid} \wedge b.\text{color} = 'red']]$$

~Q3: "There is a sailor who reserved only red boats."



$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \neg(\exists y, t [Reserves(v, y, t) \wedge \neg(\exists u, s [Boat(y, u, 'red', s)])])]$$

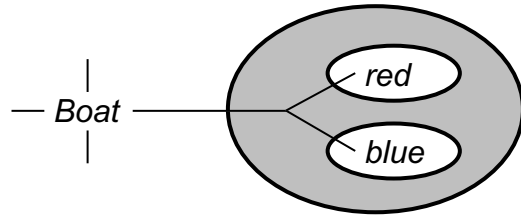
$$\exists x, v, z, w [Sailor(v, x, z, w) \wedge \forall y, t [Reserves(v, y, t) \rightarrow (\exists u, s [Boat(y, u, 'red', s)])]]$$


$$\exists s \in \text{Sailor} [\neg(\exists r \in \text{Reserves} [s.\text{sid} = r.\text{sid} \wedge \neg(\exists b \in \text{Boat} [b.\text{color} = 'red' \wedge r.\text{bid} = b.\text{bid}]) )]$$

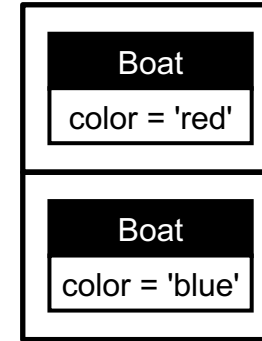
$$\exists s \in \text{Sailor} [ \forall b \in \text{Boat} [b.\text{color} = 'red' \rightarrow \exists r \in \text{Reserves} [r.\text{bid} = b.\text{bid} \wedge s.\text{sid} = r.\text{sid} ] ] ]$$

# Beta EGs vs. Relational Diagrams

~Q1: "There is a boat that is red or blue."



$$\exists y,z,u [Boat(z,x,y,u) \wedge (y='red' \vee y='blue')]$$

$$\exists y,z,u [Boat(z,x,y,u) \wedge \neg(\neg(y='red') \wedge \neg(y='blue'))]$$


$$\exists b \in Boat [q.bname=b.bname \wedge (b.color='red' \vee b.color='blue')]$$

$$\exists b \in Boat [q.bname=b.bname \wedge b.color='red'] \vee \exists b \in Boat [q.bname=b.bname \wedge b.color='blue']$$

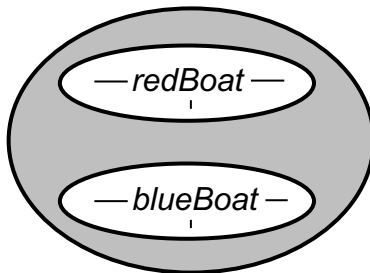
## Schemas

Boat
<u>bid</u>
bname
color
pdate

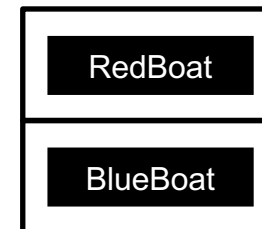
RedBoat
<u>bid</u>
bname
pdate

BlueBoat
<u>bid</u>
bname
pdate

~Q5: "There is a red boat or a blue boat."



$$\exists x \exists y \exists z [RedBoat(x,y,z) \vee BlueBoat(x,y,z)]$$

$$\neg(\neg(\exists x \exists y \exists z [RedBoat(x,y,z)]) \wedge \neg(\exists z [BlueBoat(x,y,z)]))$$


$$\exists b \in RedBoat [q.bid=b.bid \wedge q.bname=b.bname] \vee$$

$$\exists b \in BlueBoat [q.bid=b.bid \wedge q.bname=b.bname]$$

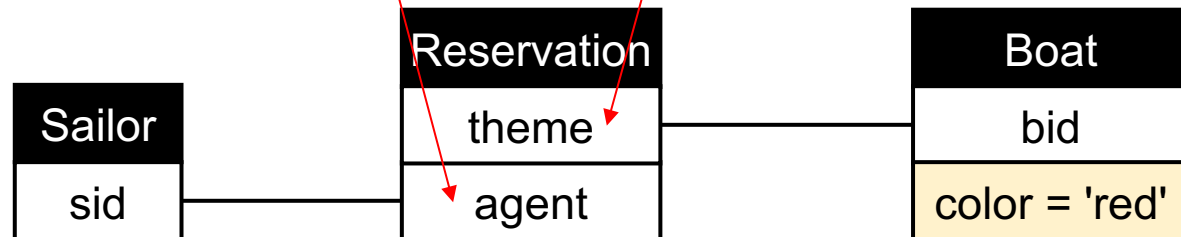


# Relational Diagrams vs. Conceptual Graphs

# Conceptual Graphs vs. Relational Diagrams



$\exists x: \text{Sailor}, \exists y: \text{Boat}, \exists z: \text{Reservation} [\text{Agent}(z, x) \wedge \text{Theme}(z, y) \wedge \text{Color}(\text{red}) \wedge \text{Attribute}(x, \text{red})]$

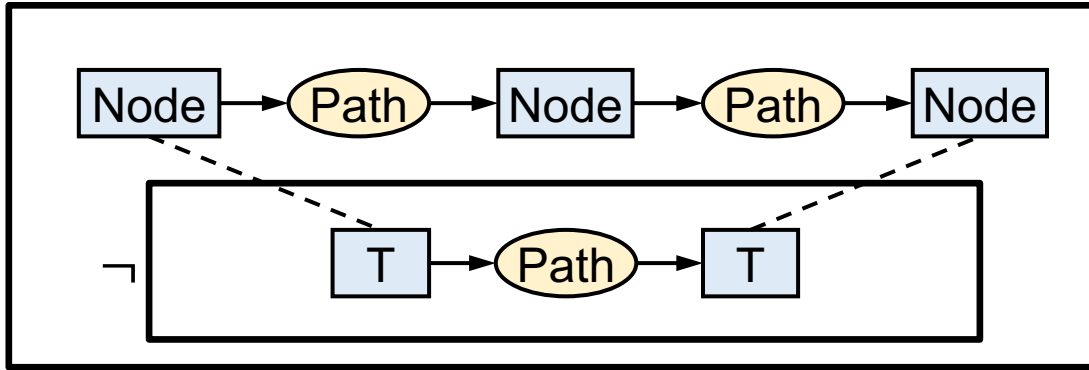


agent and theme  
really "belong to"  
Reservation

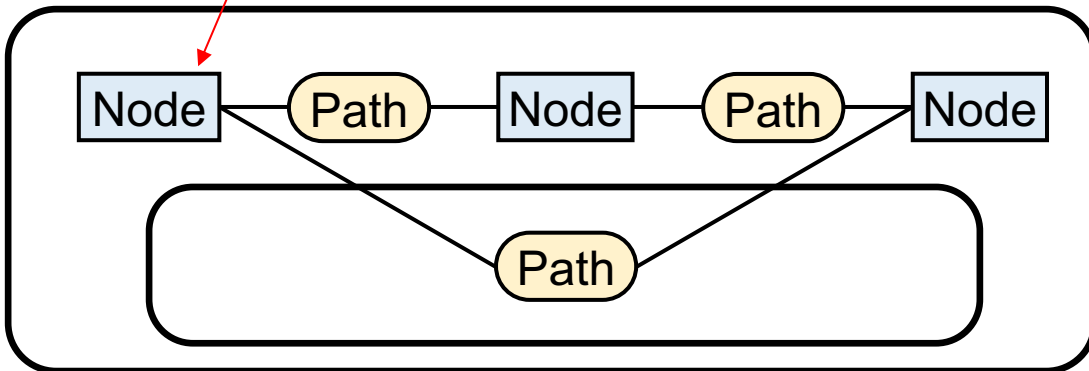
"Relational Diagrams" uses a UML-inspired  
representation that is consistent with  
familiar relational schema notation

$\exists x \in \text{Sailor}, \exists y \in \text{Boat}, \exists z \in \text{Reserves} [x.\text{sid} = y.\text{agent} \wedge y.\text{theme} = z.\text{bid} \wedge z.\text{color} = \text{'red'}]$

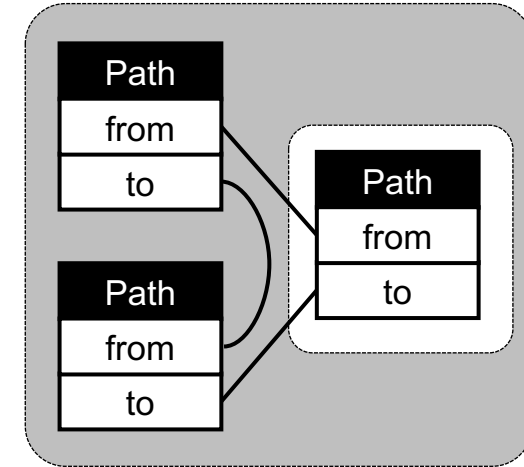
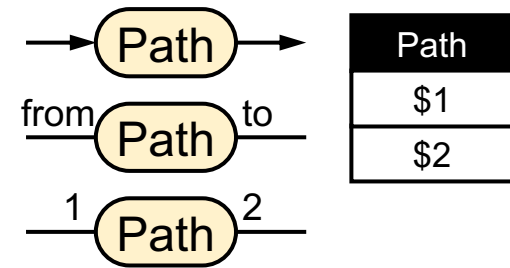
# Conceptual Graphs vs. Relational Diagrams



Even with Dau's simplification, conceptual graphs still require concepts *\*in addition\** to relations



"Paths are transitive."



Relational Diagrams follow tuple relational calculus and thus don't need concept nodes

Translation to (domain relational) calculus:

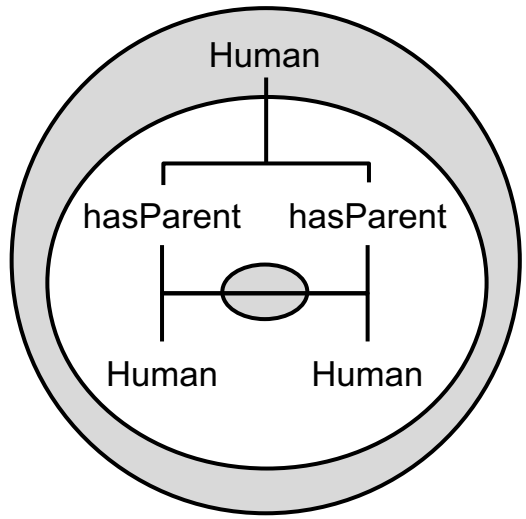
$$\neg(\exists x: \text{Node}, \exists y: \text{Node}, \exists z: \text{Node}[\text{Path}(x, y) \wedge \text{Path}(y, z) \wedge \neg(\text{Path}(x, z))])$$

Translation to (tuple relational) calculus:

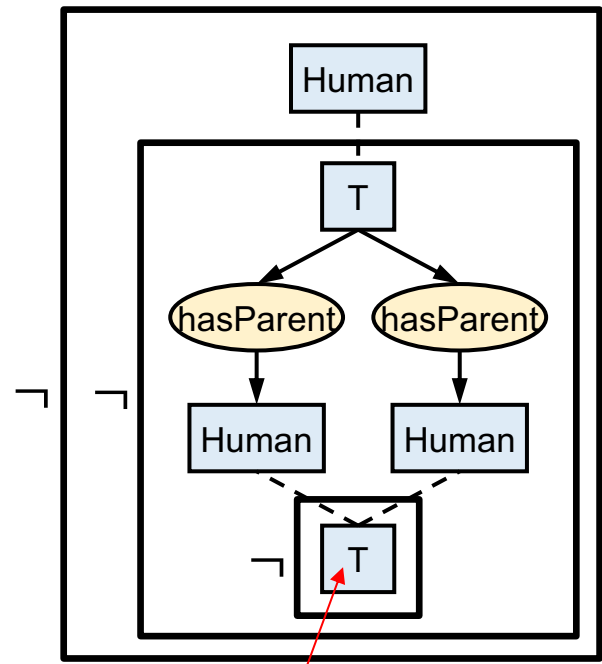
$$\neg(\exists r_1 \in R, \exists r_2 \in R[r_1.\text{to} = r_2.\text{from} \wedge \neg(\exists r_3 \in R[r_3.\text{from} = r_1.\text{from} \wedge r_3.\text{to} = r_2.\text{to}])])$$

# Beta Existential Graph

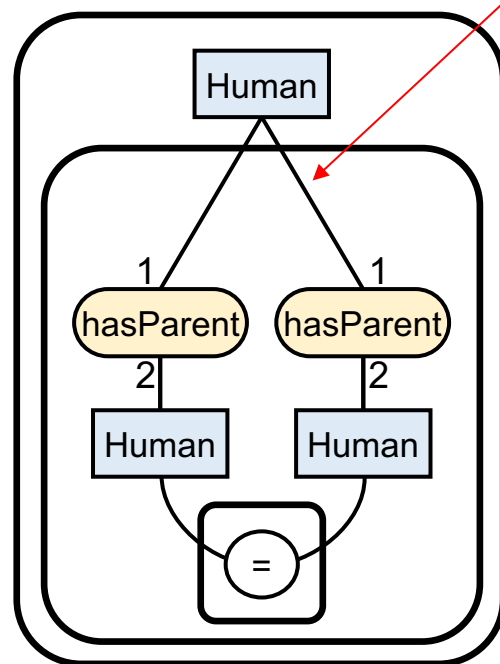
"Every Human has at least two parents who are Human."



# Conceptual Graph

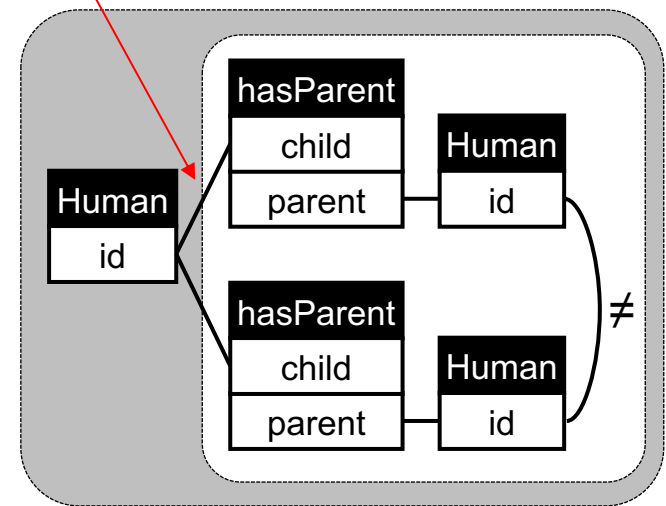


# Conceptual Graphs (Dau variant)



# Relational Diagram

Lines are used to connect arguments of predicates, not for existential quantification. The position of the "fork" does not matter



To express that  $y \neq z$ , we have to say "No entity exists that is equal to both  $y$  and  $z$ ."

## Translation:

DRC:  $\neg(\exists x[\text{Human}(x) \wedge \neg(\exists y, \exists z[\text{hasParent}(x, y) \wedge \text{Human}(y) \wedge \text{hasParent}(x, z) \wedge \text{Human}(z) \wedge \neg(y = z)])])$

TRC:  $\neg(\exists h_1 \in \text{Human}[\neg(\exists p_1 \in \text{hasParent}, \exists p_2 \in \text{hasParent}, \exists h_2 \in \text{Human}, \exists h_3 \in \text{Human}[p_1.\text{child} = h_1.\text{id} \wedge p_2.\text{child} = h_1.\text{id} \wedge p_1.\text{parent} = h_2.\text{id} \wedge p_2.\text{parent} = h_3.\text{id} \wedge h_2.\text{id} \neq h_3.\text{id}])])$

# Beta Existential Graph

# Conceptual Graph

# Relational Diagram

Logic

domain relational calculus (DRC)

DRC

tuple relational calculus (TRC)

Visual element  
for existential  
quantification

Line (of Identity)

— Human

Concept box

Human

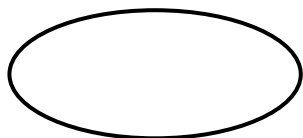
Relation box

Human

Key difference of relational diagrams

Visual negation

Oval / Cut



Annotated Box / Cut



Dashed rounded box

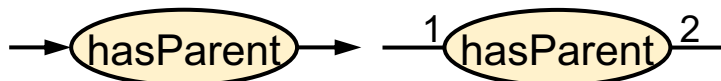


Order or names  
of relational  
attributes

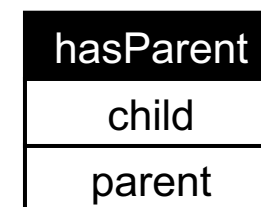
not specified

— hasParent —

arc (arrowhead) / numbers



attribute names (named perspective)



Queries

No

Human: ?



# Intended Agenda today

Please leave  
feedback 😊

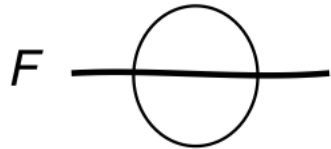
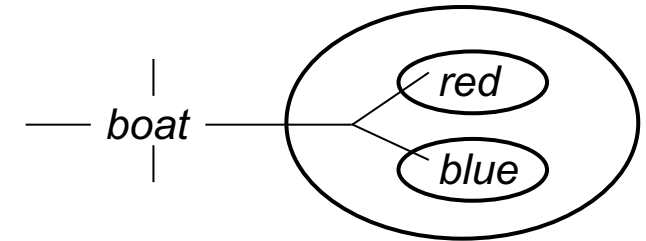
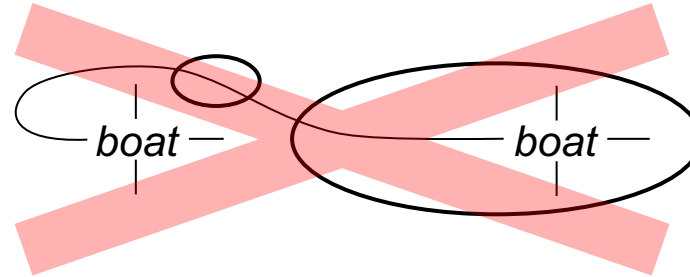
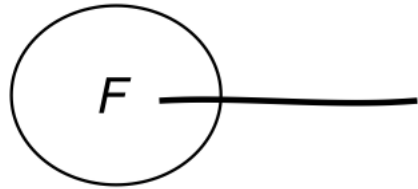
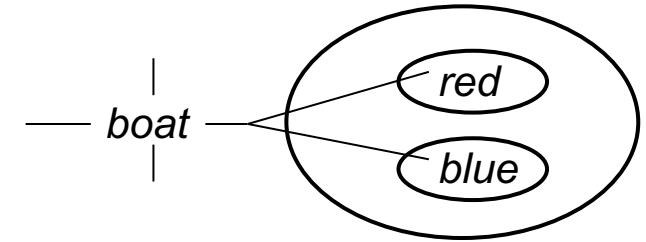
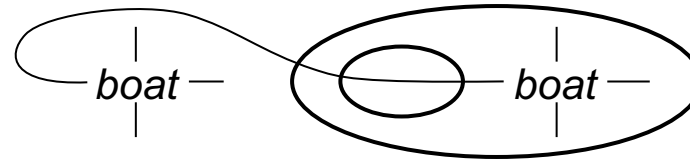
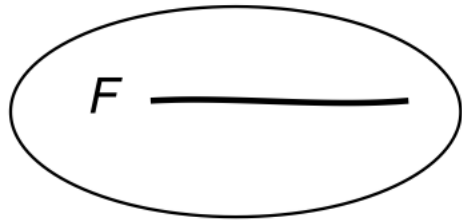


1. Why visualizing queries and why now?
2. Principles of Query Visualization
3. Logical foundations of relational query languages
4. (Early) Diagrammatic representations
5. Visual Query Representations (from DB community)
6. Lessons Learned and Open Challenges

# 3 Abuses of the Line

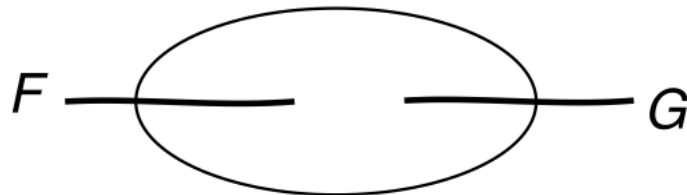
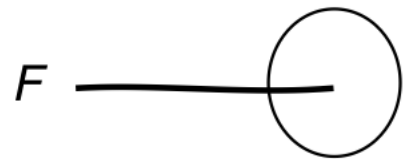
# Beta EGs: Lines of Identity

The interpretation "line of identity" in Beta EGs creates a lot of confusion



different meanings

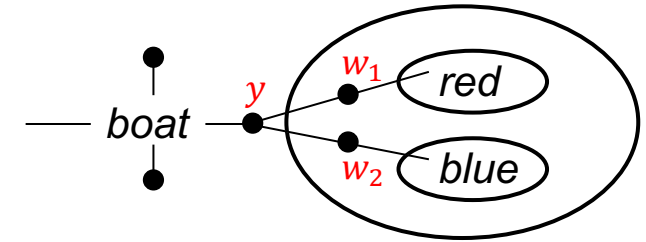
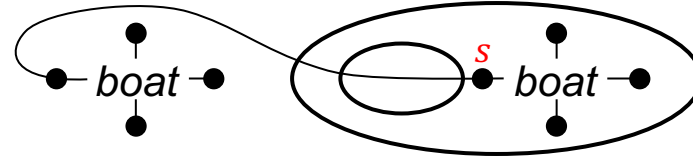
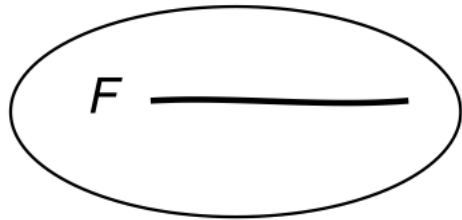
same meaning, but  
different interpretations





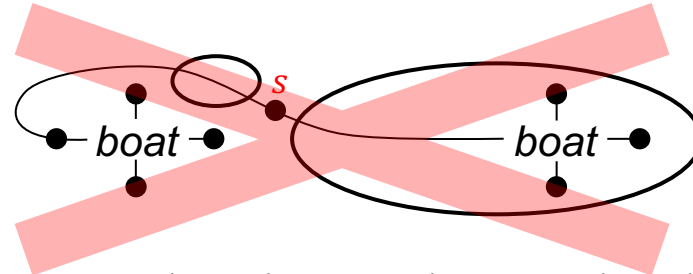
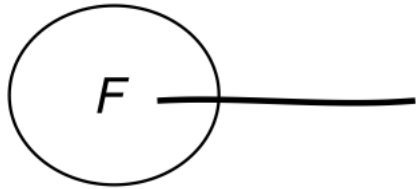
# Beta EGs: Lines of Identity

Quantification via a visual symbol \*different\* from the line could have avoided those difficulties

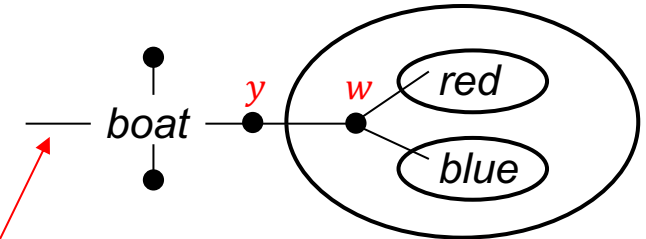


$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \neg(s,t,u,v [\text{Boat}(s,t,u,v) \wedge x \neq s])]$

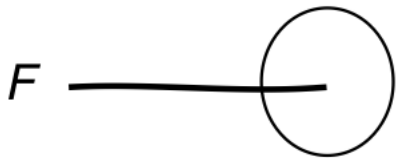
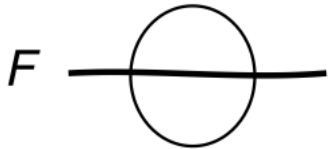
$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w_1,w_2 [w_1=y \wedge w_2=y \wedge \neg(w_1='red') \wedge \neg(w_2='blue')])]\}$



$\exists x,y,z,w,s [\text{Boat}(x,y,z,w) \wedge x \neq s \wedge \neg(\exists t,u,v [\text{Boat}(s,t,u,v)])]$

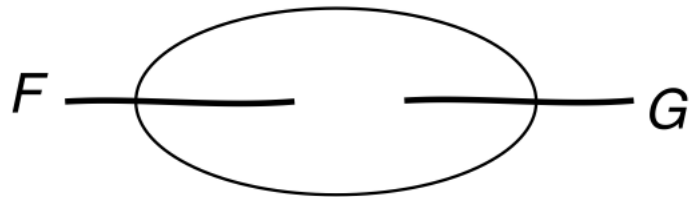


$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w [w=y \wedge \neg(w='red') \wedge \neg(w='blue')])]\}$



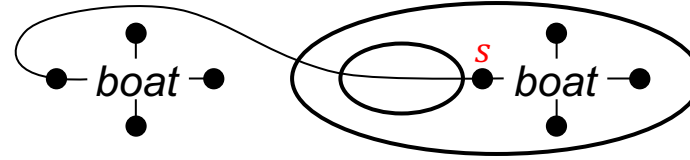
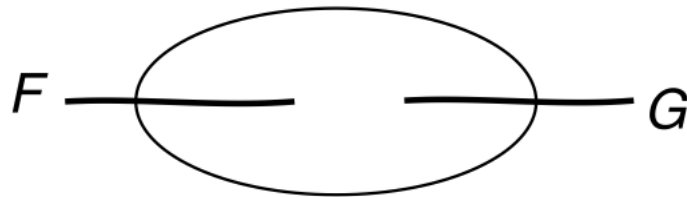
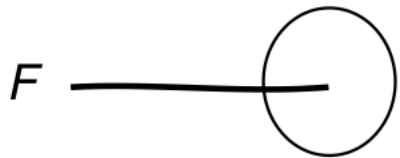
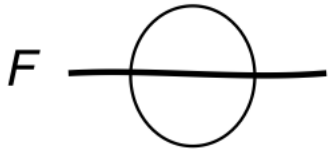
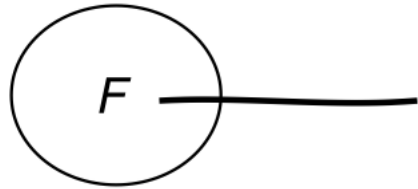
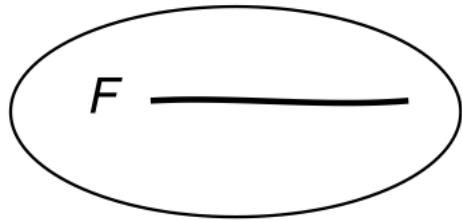
Here, the bullet (as in string diagrams, or a concept node as in conceptual graphs) is quantified.

- Free variables are possible
- the interpretation is easy

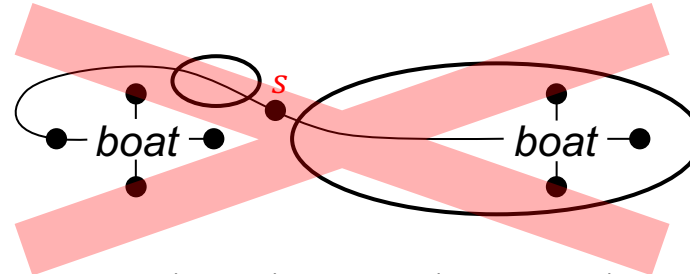


# Beta EGs: Lines of Identity

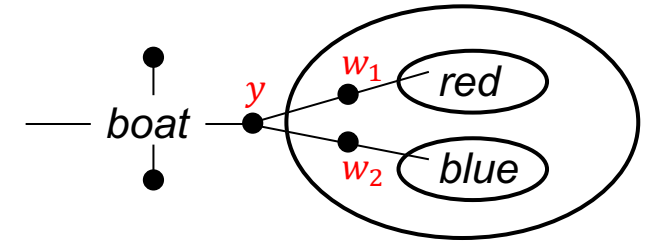
Quantification via a visual symbol \*different\* from the line could have avoided those difficulties



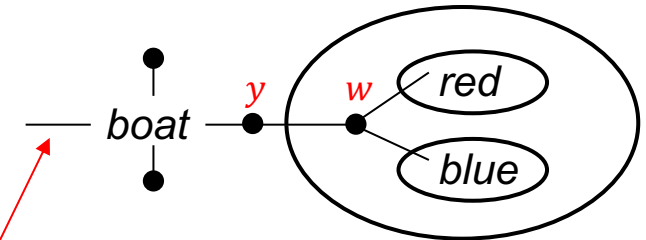
$$\exists x,y,z,w [\text{Boat}(x,y,z,w) \wedge \neg(s,t,u,v [\text{Boat}(s,t,u,v) \wedge x \neq s])]$$



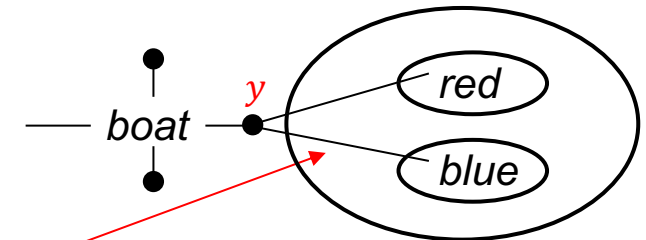
$$\exists x,y,z,w,s [\text{Boat}(x,y,z,w) \wedge x \neq s \wedge \neg(\exists t,u,v [\text{Boat}(s,t,u,v)])]$$



$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w_1,w_2 [w_1=y \wedge w_2=y \wedge \neg(w_1='red') \wedge \neg(w_2='blue')])]\}$$



$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\exists w [w=y \wedge \neg(w='red') \wedge \neg(w='blue')])]\}$$



$$\{(x) \mid \exists y,z,u [\text{Boat}(z,x,y,u) \wedge \neg(\neg(y='red') \wedge \neg(y='blue'))]\}$$

Here, the bullet (as in string diagrams, or a concept node as in conceptual graphs) is quantified.

- Free variables are possible
- the interpretation is easy
- a line can traverse a cut w/o quantification in that cut

# 1<sup>st</sup> abuse of lines and how to avoid it

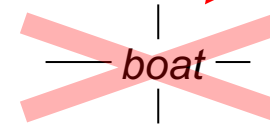
## RULE 1:

Lines should not be used for existential quantification.

Existential quantification of variables as in DRC is better done with a dedicated symbol (e.g. the bullet in string diagrams, or concept nodes in conceptual graphs)

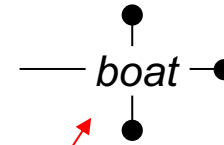
Lines of Identify (LIs) in Beta EGs have multiple meanings: existential quantification and identity = equality which leads to possible ambiguities.

## Domain RC



$\exists x,y,z,u[\text{Boat}(x,y,z,u)]$

Beta EGs



$\{(y) \mid \exists x,z,u[\text{Boat}(x,y,z,u)]\}$

Beta EGs,  
adapted with  
bullets from  
string diagrams

Using bullets (or concept nodes) for quantification, and lines as symbol for equality

# 1<sup>st</sup> abuse of lines and how to avoid it

## RULE 1:

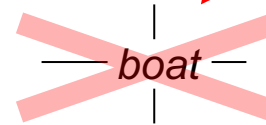
Lines should not be used for existential quantification.

Existential quantification of variables as in DRC is better done with a dedicated symbol (e.g. the bullet in string diagrams, or concept nodes in conceptual graphs)

Or, alternatively, existential quantification could be directly done with the actual relation symbols as in TRC (e.g. Relational Diagrams)

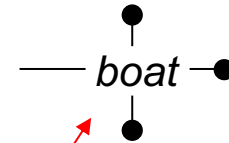
Lines of Identify (LIs) in Beta EGs have multiple meanings: existential quantification and identity = equality which leads to possible ambiguities.

## Domain RC



$\exists x,y,z,u[\text{Boat}(x,y,z,u)]$

Beta EGs



$\{(y) \mid \exists x,z,u[\text{Boat}(x,y,z,u)]\}$

Beta EGs,  
adapted with  
bullets from  
string diagrams

Using bullets (or concept nodes) for quantification, and lines as symbol for equality

## Tuple RC

boat

$\exists B \in \text{Boat}$

The relational predicate is existentially quantified, as in TRC and SQL

# 1<sup>st</sup> abuse of lines and how to avoid it

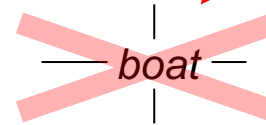
## RULE 1:

Lines should not be used for existential quantification.

Existential quantification of variables as in DRC is better done with a dedicated symbol (e.g. the bullet in string diagrams, or concept nodes in conceptual graphs)

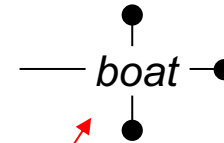
Or, alternatively, existential quantification could be directly done with the actual relation symbols as in TRC (e.g. Relational Diagrams)

## Domain RC



$\exists x,y,z,u[\text{Boat}(x,y,z,u)]$

Beta EGs



$\{(y) \mid \exists x,z,u[\text{Boat}(x,y,z,u)]\}$

Beta EGs,  
adapted with  
bullets from  
string diagrams

Using bullets (or concept nodes) for quantification, and lines as symbol for equality

## Tuple RC

boat

$\exists B \in \text{Boat}$

The relational predicate is existentially quantified, as in TRC and SQL

and then using a familiar UML notation

Boat

$\exists B \in \text{Boat}$

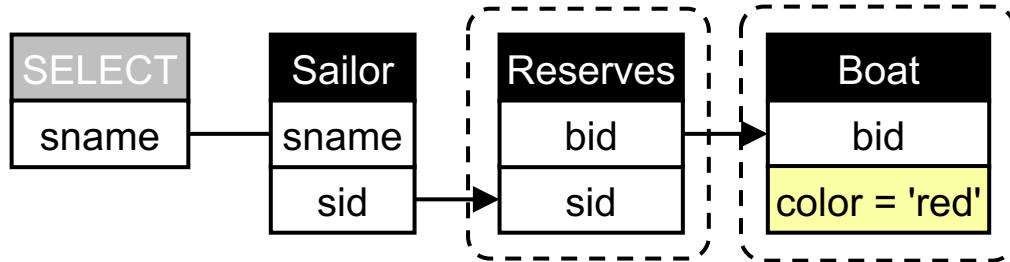
Relational  
Diagrams

Lines of Identify (LIs) in Beta EGs have multiple meanings: existential quantification and identity = equality which leads to possible ambiguities.

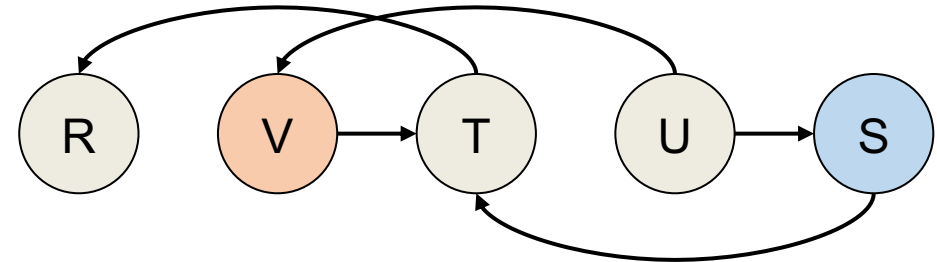
# How to visualize reading direction for negations

## QueryVis

Lines with arrowhead indicate the reading direction

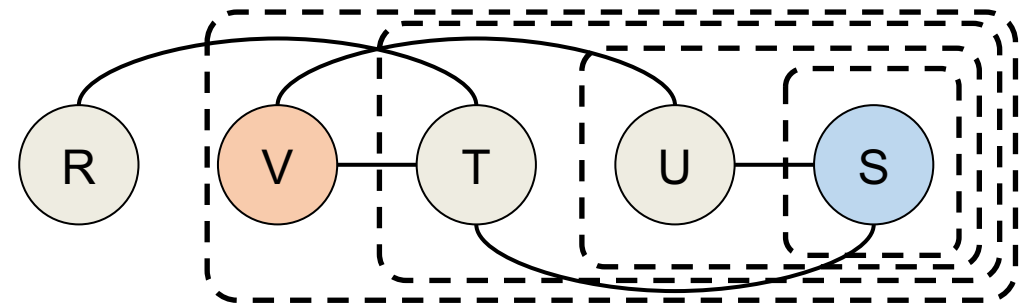
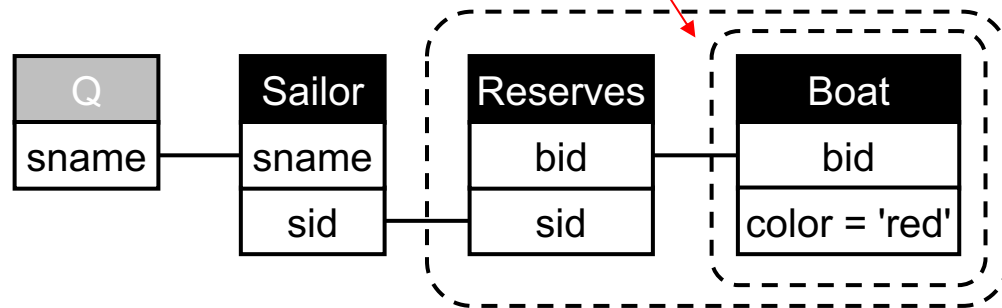


Arrows for making the reading order explicit may reduce the visual clutter



Reading order follows implicitly from the nesting hierarchy (outside in)

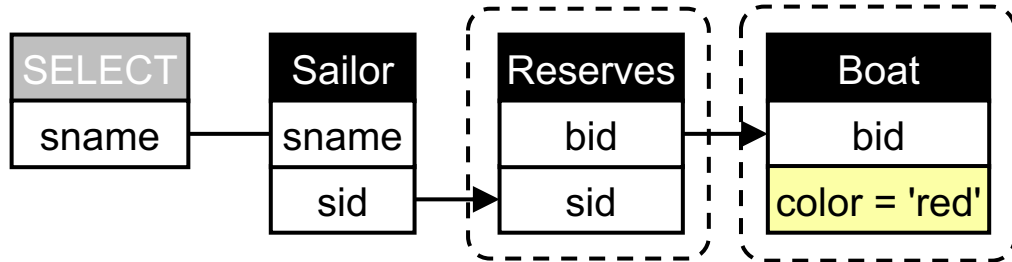
## Relational Diagrams



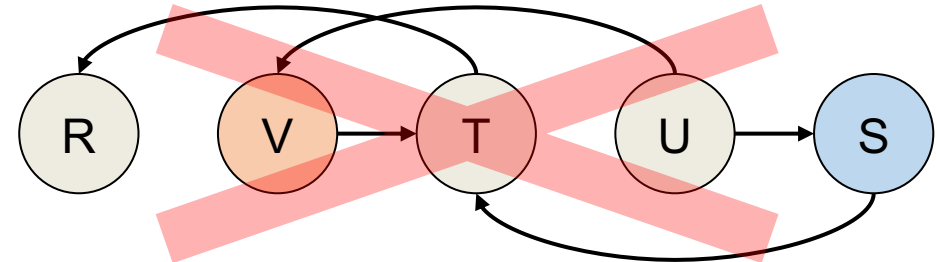
# How to visualize reading direction for negations

## QueryVis

Lines with arrowhead indicate the reading direction



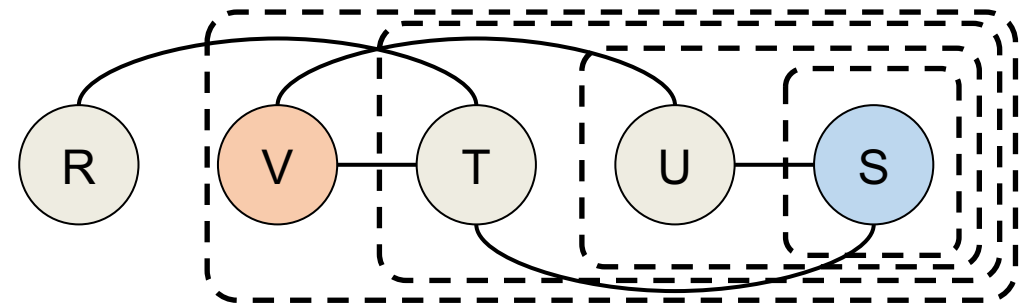
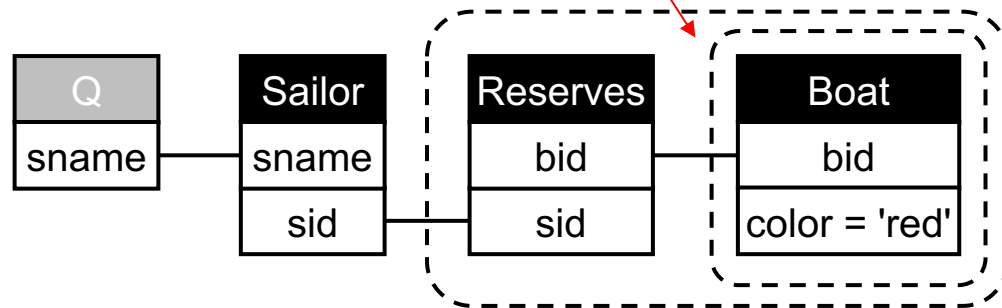
Arrows for making the reading order explicit may reduce the visual clutter



But, lines with arrowhead cannot represent all logical expressions, and can become ambiguous

## Relational Diagrams

Reading order follows implicitly from the nesting hierarchy (outside in)



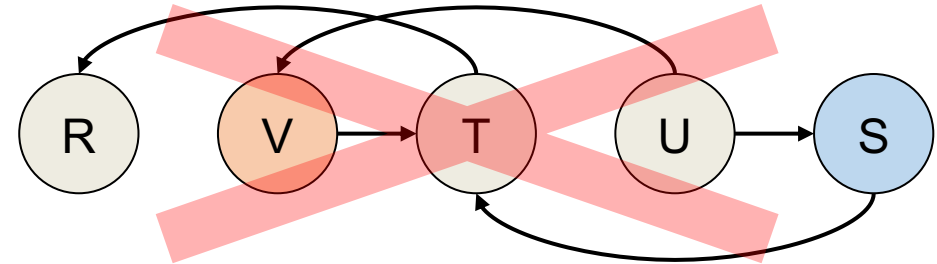
## 2<sup>nd</sup> abuse of lines and how to avoid it

### RULE 2:

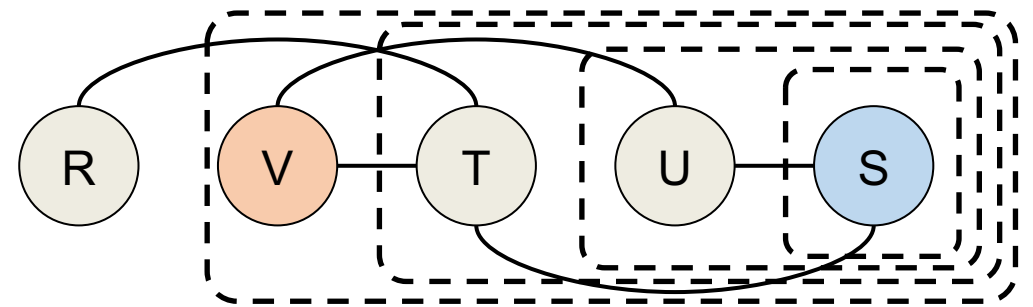
Lines should not be used as *\*only\** symbol for indicating quantifier scoping (i.e. the nested negation scopes, via a reading order).

Nesting hierarchy can be unambiguously represented by explicit nesting of the scopes

Arrows for making the reading order explicit may reduce the visual clutter



But, lines with arrowhead cannot represent all logical expressions, and can become ambiguous





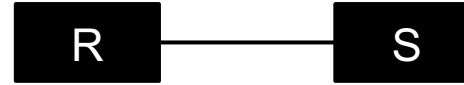
# How to visualize a natural join between two tables?

$R \bowtie S$

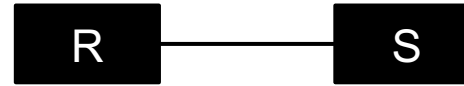


# How to visualize a natural join between two tables?

$R \bowtie S$



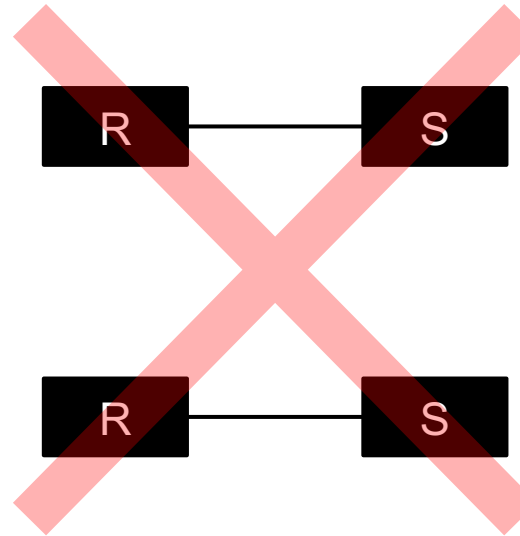
$R(A) \bowtie S(B)$



# How to visualize a natural join between two tables?

$R \bowtie S$

$R(A) \bowtie S(B)$



Lines representing joins  
(incl. Cartesian products)  
can lead to ambiguities  
(as in QBD) ☹

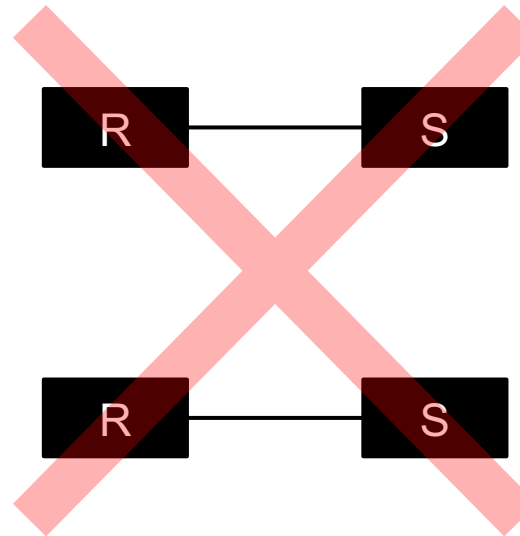
# How to visualize a natural join between two tables?

$$R \bowtie S$$

$$R(A) \bowtie S(B)$$

$$R(A) \bowtie S(B)$$

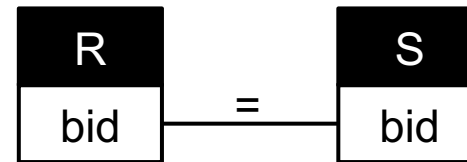
$$R(A) \bowtie S(\textcolor{red}{A}) \\ = R \bowtie_{\textcolor{red}{R.A=S.A}} S$$



Lines representing joins  
(incl. Cartesian products)  
can lead to ambiguities  
(as in QBD) ☹



$$\pi_{\emptyset}(R(A) \bowtie S(B)) \\ \exists r \in R \wedge \exists s \in S$$



Lines here represent the  
join condition b/w  
\*attributes\* not tables!

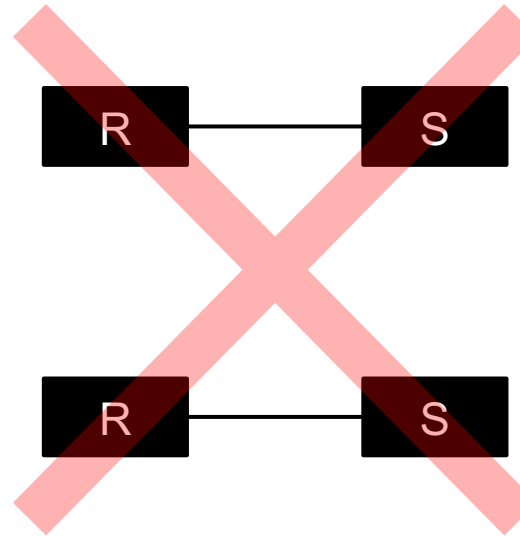
# 3<sup>rd</sup> abuse of lines and how to avoid it

## RULE 3:

Lines should not be used for (Cartesian) joins.

Cartesian joins can be better represented by just putting tables on the same Canvas partition.

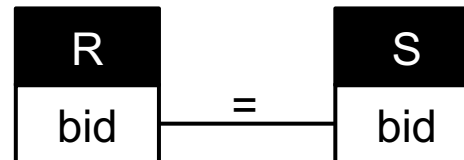
Lines are then representing the actual join condition between the respective attributes.



Lines representing joins (incl. Cartesian products) can lead to ambiguities (as in QBD) ☹



$$\pi_{\emptyset}(R(A) \bowtie S(B))$$
$$\exists r \in R \wedge \exists s \in S$$



Lines here represent the join condition b/w \*attributes\* not tables!

## 3 abuses of the line

**Lines** as visual symbol should only be used for **comparisons** (including equality, and with labels for disequality and inequality).

Lines should not be used for:

1. **existential quantification** (as in Peirce's Beta EGs)
2. **joins = cross products** (as in Query-By-Diagram)
3. for **nesting directions** with arrowheads (as in QueryVis)

# 3 abuses of the line

**Lines** as visual symbol should only be used for **comparisons** (including **equality**, and **with labels for disequality and inequality**).

Lines should not be used for:

1. **existential quantification** (as in Peirce's Beta EGs)

- instead, use dedicated symbols (e.g. bullets as in string diagrams for DRC)
- instead, use placement of relational symbols (Relational Diagrams for TRC)

2. **joins = cross products** (as in Query-By-Diagram)

- instead, use simple placement, and use lines as "join conditions"

3. for **nesting directions** with arrowheads (as in QueryVis)

- instead, use the topological nesting of scoping boxes (Relational Diagrams)

# Open issues



# 1: Showing Disjunctions diagrammatically is hard

Text:

Boat
bid
color = 'red' or 'blue'

Diagram:



# 1: Showing Disjunctions diagrammatically is hard

Text:

Boat
bid
color = 'red' or 'blue'

*But it can get far more complicated 😞*

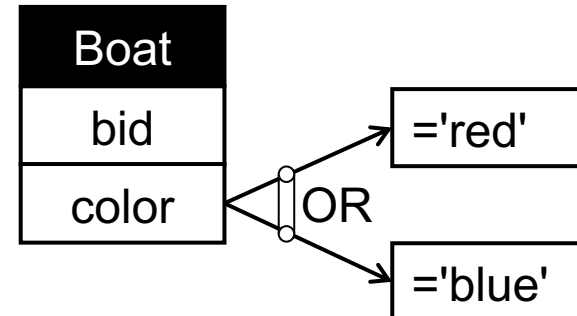
Diagram  
(or claimed  
"visual"):

Boat
color
red
blue

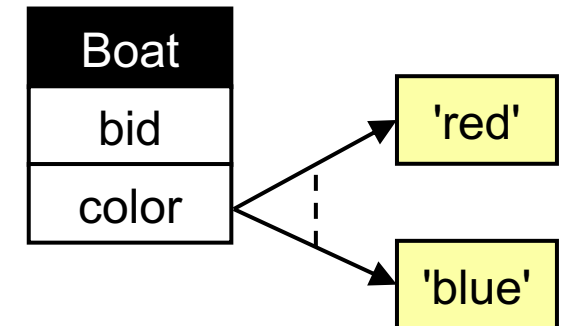
QBE (1977)

Boat	
bid	
color	red
	blue

TableTalk (1991)



Visual SQL (2003)



QueryVis (2011)

# 1: Showing Disjunctions diagrammatically is hard

R(A,B,C)  
S(A)

*How to visually represent arbitrary Boolean formulas?*

```
select exists
  (select *
   from R
   where (R.B = 0
         and exists
          (select *
           from S
           where R.A = S.A))
   or (R.B = 1
       and R.C = 2))
```



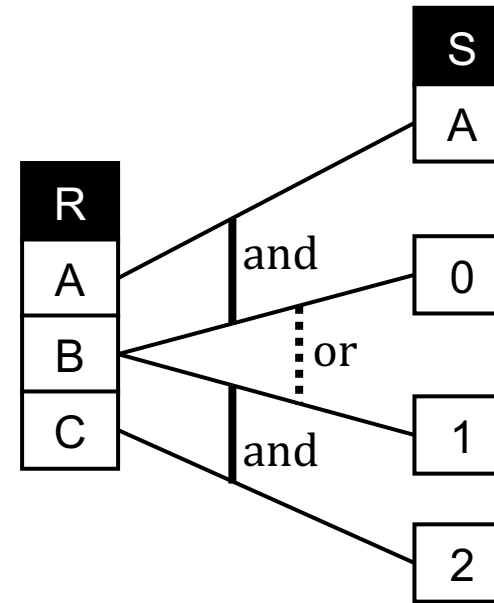
# 1: Showing Disjunctions diagrammatically is hard

$R(A,B,C)$   
 $S(A)$

*How to visually represent arbitrary Boolean formulas?*

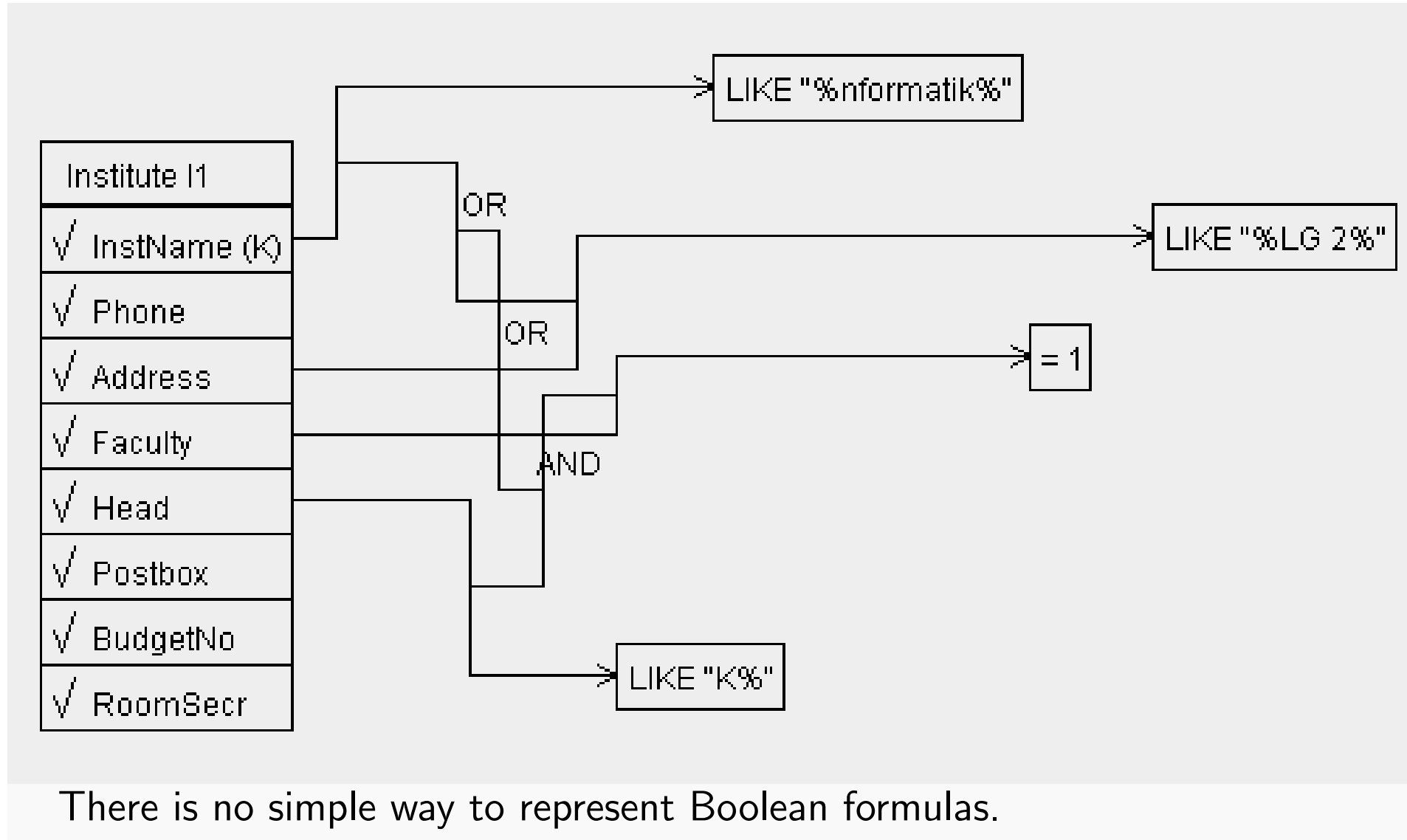
```
select exists
  (select *
   from R
   where (R.B = 0
         and exists
           (select *
            from S
            where R.A = S.A))
   or (R.B = 1
       and R.C = 2))
```

?



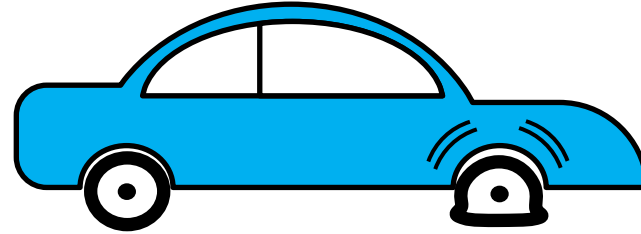
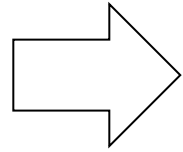
*quickly becomes ambiguous*

# 1: Showing Disjunctions diagrammatically is hard

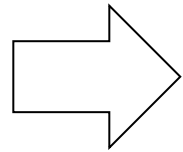


# 1: Why is visualizing disjunctive information harder?

I see a car that is blue  
**AND** that has a flat tire

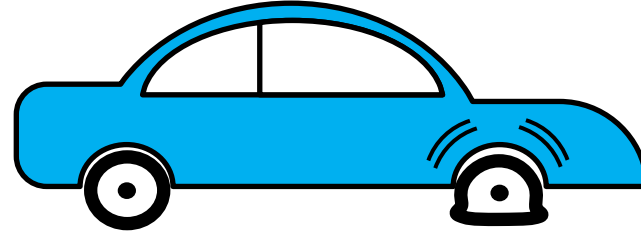
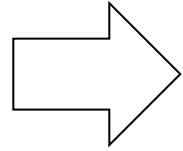


I see a car that is blue  
**OR** that has a flat tire

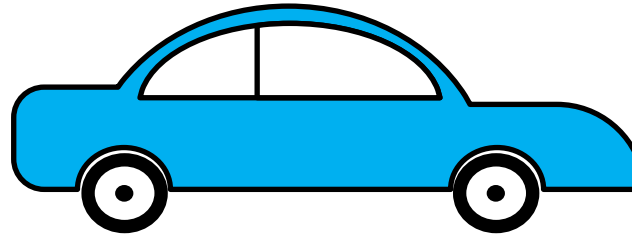
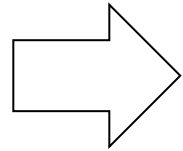


# 1: Why is visualizing disjunctive information harder?

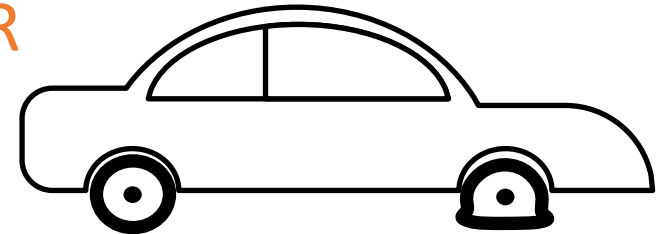
I see a car that is blue  
**AND** that has a flat tire



I see a car that is blue  
**OR** that has a flat tire

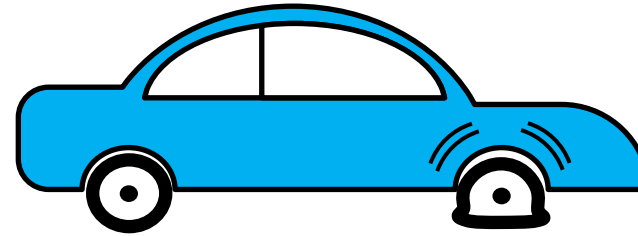
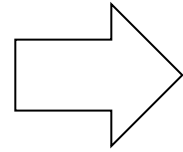


**OR**



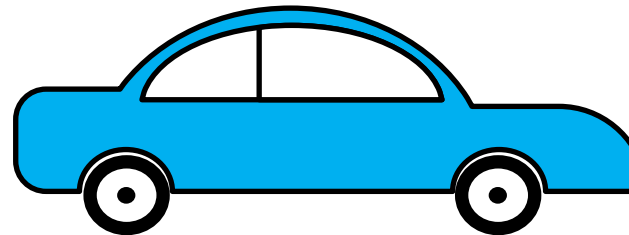
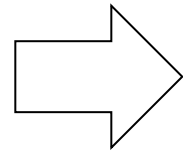
# 1: Why is visualizing disjunctive information harder?

I see a car that is blue  
**AND** that has a flat tire



color="blue"  
**AND** tire="flat"

I see a car that is blue  
**OR** that has a flat tire



**OR**



color="blue"

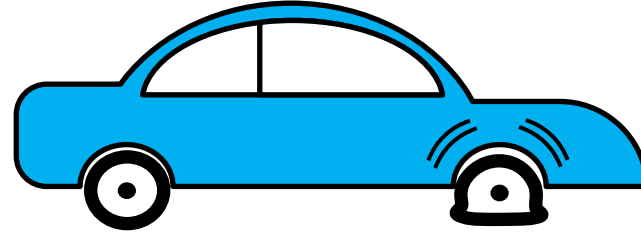
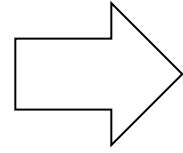
**OR**

tire="flat"



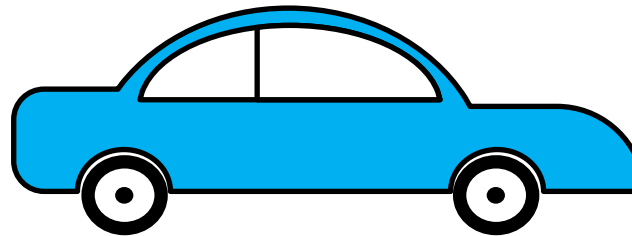
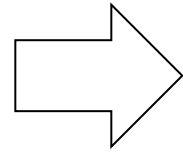
# 1: Why is visualizing disjunctive information harder?

I see a car that is blue  
**AND** that has a flat tire



$\sigma_{\text{color}=\text{"blue"} \text{ AND } \text{tire}=\text{"flat"} (\dots)}$

I see a car that is blue  
**OR** that has a flat tire



**OR**

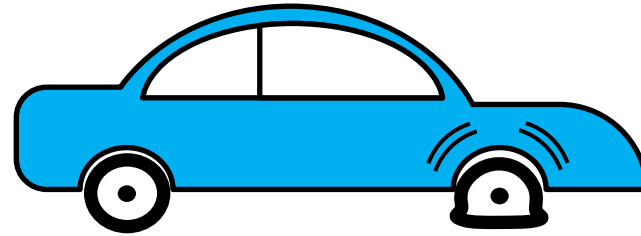
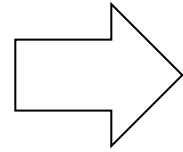


$\sigma_{\text{color}=\text{"blue"} \text{ OR } \text{tire}=\text{"flat"} (\dots)}$

# 1: Why is visualizing disjunctive information harder?

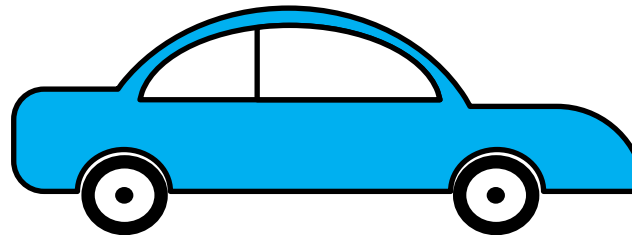
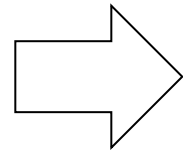
"A situation only displays conjunctive information."\*

I see a car that is blue  
**AND** that has a flat tire



$\sigma_{\text{color}=\text{"blue"}}(\sigma_{\text{tire}=\text{"flat"}}(\dots))$

I see a car that is blue  
**OR** that has a flat tire



**OR**



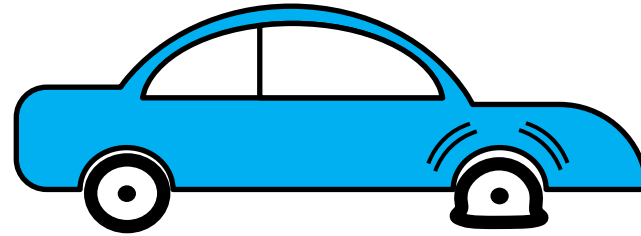
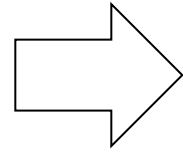
$\sigma_{\text{color}=\text{"blue"}} \text{ OR } \sigma_{\text{tire}=\text{"flat"}}(\dots)$

\* Sun-Joo Shin, "The logical status of diagrams", 1995. <https://doi.org/10.1017/CBO9780511574696>

# 1: Why is visualizing disjunctive information harder?

"A situation only displays conjunctive information."\*

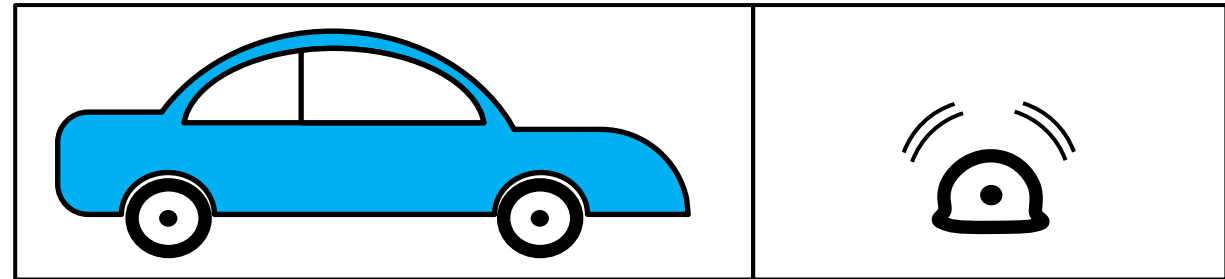
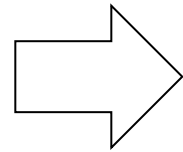
I see a car that is blue  
**AND** that has a flat tire



$\sigma_{\text{color}=\text{"blue"}}(\sigma_{\text{tire}=\text{"flat"}}(\dots))$

Peirce's "compartments" strategy (a syntactic device) for disjunctions:

I see a car that is blue  
**OR** that has a flat tire



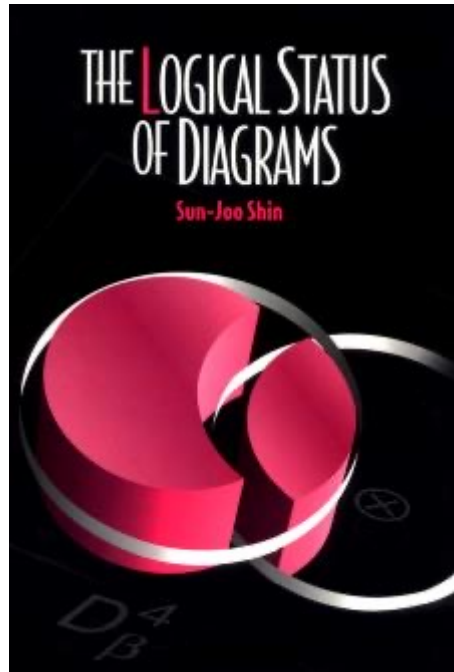
$\sigma_{\text{color}=\text{"blue"}} \text{ OR } \sigma_{\text{tire}=\text{"flat"}}(\dots)$

\* Sun-Joo Shin, "The logical status of diagrams", 1995. <https://doi.org/10.1017/CBO9780511574696>

Wolfgang Gatterbauer. A Comprehensive Tutorial on (...) Diagrammatic Representations (...), ICDE 2024. <https://northeastern-datalab.github.io/diagrammatic-representation-tutorial/>

# 1: Why is visualizing disjunctive information harder?

## Diagrammatic reasoning systems and their expressiveness



**Diagrams** are widely used in reasoning about problems in physics, mathematics, and logic, but have traditionally been considered to be only heuristic tools and not valid elements of mathematical proofs. This book challenges this prejudice against visualization in the history of logic and mathematics and provides a formal foundation for work on natural reasoning in a visual mode.

The author presents Venn diagrams as a formal system of representation equipped with its own syntax and semantics and specifies rules of transformation that make this system sound and complete. The system is then extended to the equivalent of a first-order monadic language. The soundness of these diagrammatic systems refutes the contention that graphical representation is misleading in reasoning. The validity of the transformation rules ensures that the correct application of the rules will not lead to fallacies. The book concludes with a discussion of some fundamental differences between graphical systems and linguistic systems.

This groundbreaking work will have important influence on research in logic, philosophy, and knowledge representation.

objects. **Conjunctive information** is more naturally represented by diagrams than by linguistic formulæ. For example, a single Venn diagram can

Still, not all relations can be viewed as membership or inclusion. Shin has been careful throughout her book to **restrict herself to monadic systems**. Relations per se (polyadic predicates) are not considered. And while it may be true that the formation of a system (such as Venn-II) that is provably both sound and complete would help mitigate the prejudice

perception. In her discussion of perception she shows that **disjunctive information is not representable in any system**. In doing so she relies on

## 2: A theory on visual minimality

How to measure "visual minimality"?

And what objective should we actually minimize?  
(alphabet size, time-to-learn a representation,  
time-to-solve a problem, "visual happiness", ...)

### 3. Other extensions beyond FOL

aggregates

```
select avg(price)
from Car
where maker='Toyota'
```

groupings

```
select product, sum(quantity)
from Purchase
where price > 1
group by product
```



# 3. Other extensions beyond FOL

aggregates

```
select avg(price)
from Car
where maker='Toyota'
```

QueryVis has actually been supporting simple groupings and aggregates (again, it can get quickly more complicated, think disjunctions but more complicated, a general solution still open,...)

groupings

```
select product, sum(quantity)
from Purchase
where price > 1
group by product
```

1. group by attributes are shaded

### Your Input

1. Specify a Schema

Purchase(product, quantity, price)

2. Specify or choose a Query [Supported grammar](#)

103 Bars: Persons who frequent some bar that serves some drink they like. ▾

```
select product, sum(quantity)
from Purchase
where price > 1
group by product
```

[Submit](#) [Reset](#) <http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

### QueryViz Result

```
graph LR
    subgraph SELECT
        direction TB
        S1[product]
        S2[SUM(quantity)]
    end
    subgraph Purchase
        direction TB
        P1[product]
        P2[SUM(quantity)]
        P3[price > 1]
    end
    S1 --> P1
    S2 --> P2
```

# 3. Other extensions beyond FOL

### SQL Query Visualization

**Your Input**

**1. Specify a Schema**

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

**2. Specify or choose a Query** [Supported grammar](#)

(clean)

select R.A, count(\*)  
from R, S  
where R.C = S.C  
group by R.A, R.B  
having avg(R.C)>10

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

**QueryViz Result**

QueryVis has actually been supporting simple groupings and aggregates (again, it can get quickly more complicated, think disjunctions but more complicated, a general solution still open,...)

2. having clause is treated like selections

3. count(\*) aggregates interpreted on the whole join via grouping boxes

4. Nested queries in having clause

### SQL Query Visualization

**Your Input**

**1. Specify a Schema**

R(A,B,C)  
S(A,B,C)  
T(A,B,C)  
U(A,B,C)

**2. Specify or choose a Query** [Supported grammar](#)

(clean)

select R.A, count(\*)  
from R, S  
where R.C = S.C  
group by R.A, R.B  
having max(R.C)>  
(select count(\*)  
from R,S  
where R.B=S.B  
group by R.B)

Submit Reset

<http://queryviz.com/> (Version: 2011.03.22)

Image loaded.

**QueryViz Result**



### 3. Other extensions beyond FOL

arithmetic predicates

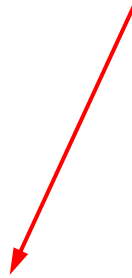
```
select sum(price * quantity)
from Purchase
```

- grouping & aggregates
- arithmetic predicates
- outer joins
- null values
- bag semantics
- recursion



## 4. We need a principled notion of relational patterns

What are "relational patterns"?



For first steps towards "relational patterns" see: "Gatterbauer, Dunne. On the Reasonable Effectiveness of Relational Diagrams: Explaining Relational Query Patterns and the Pattern Expressiveness of Relational Languages. SIGMOD 2024. <https://dl.acm.org/doi/pdf/10.1145/3639316>

# Relational patterns

$R(A,B), S(B)$

*Datalog*

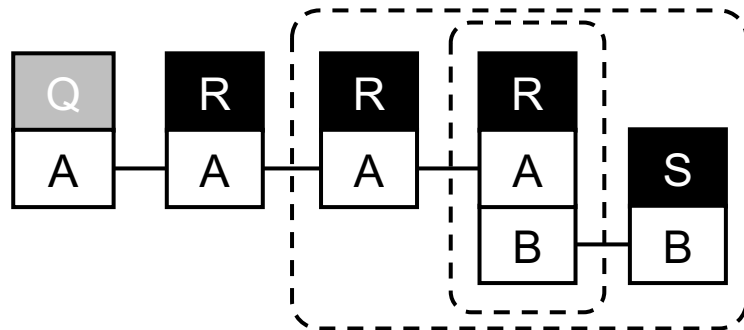
$I(x) :- R(x, \_), S(y), \neg R(x, y)$

$Q(x) :- R(x, \_), \neg I(x)$

*Relational Algebra:*

$\pi_A R - \pi_A ((\pi_A R \times S) - R)$

*Relational Diagram:*



Given 3 very different syntactic formulations of the same query (declarative, procedural, visual), what is a meaningful way to compare those different "query expressions"?

?

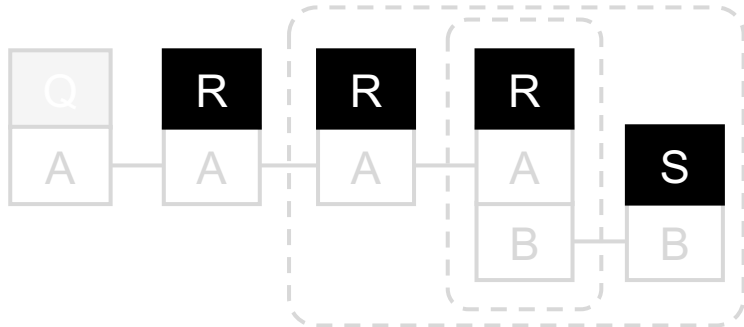
# Relational patterns

$R(A,B), S(B)$

## 1. Focus on relational atoms only

$I(x) :- R(x, \_), S(y), \neg R(x, y)$   
 $Q(x) :- R(x, \_), \neg I(x)$

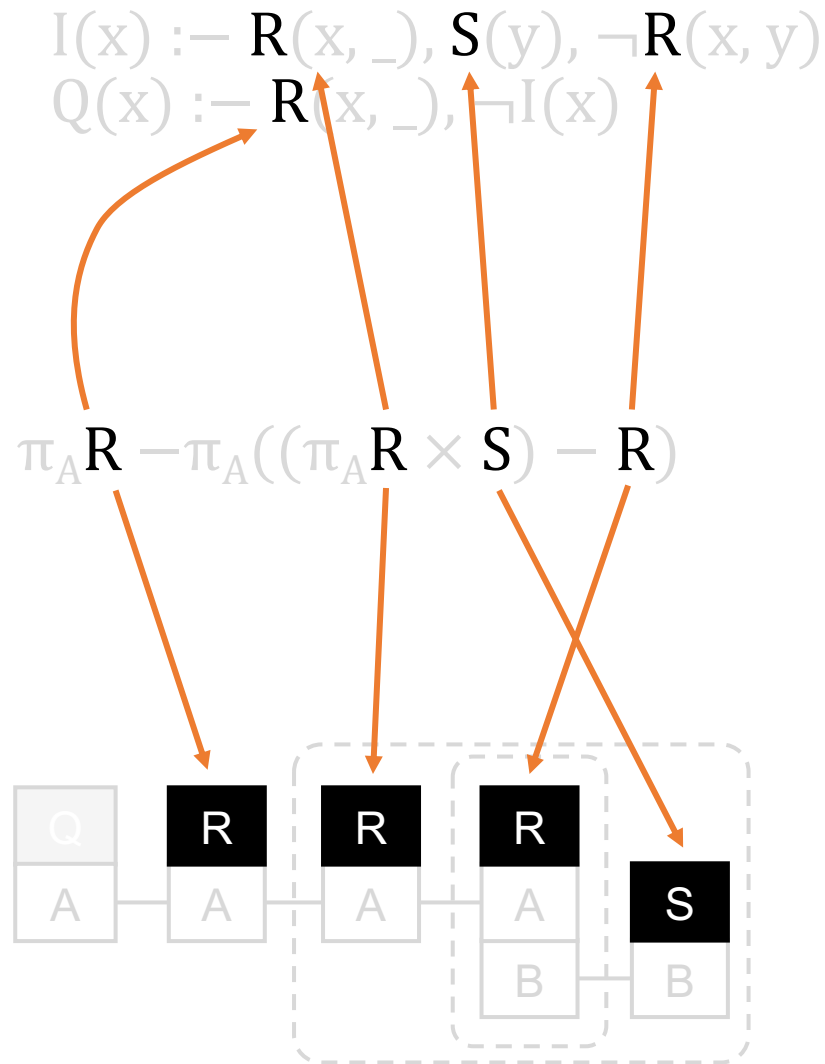
$\pi_A R - \pi_A ((\pi_A R \times S) - R)$



# Relational patterns

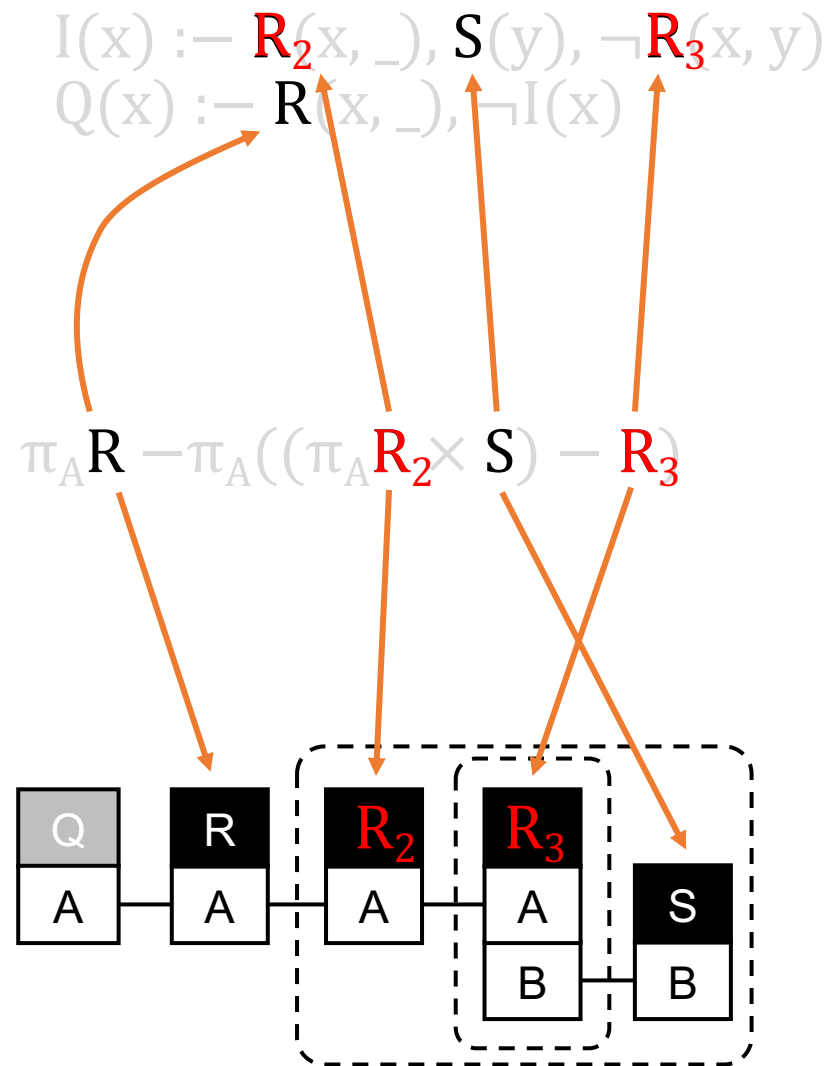
$R(A,B), S(B)$

1. Focus on relational atoms only
2. Find a table-preserving mapping between relational atoms



# Relational patterns

$R(A,B), S(B)$



1. Focus on relational atoms only
  2. Find a table-preserving mapping between relational atoms
  3. But for "dissociated queries" (treat each EDB as different)
- Are they still logically equivalent?

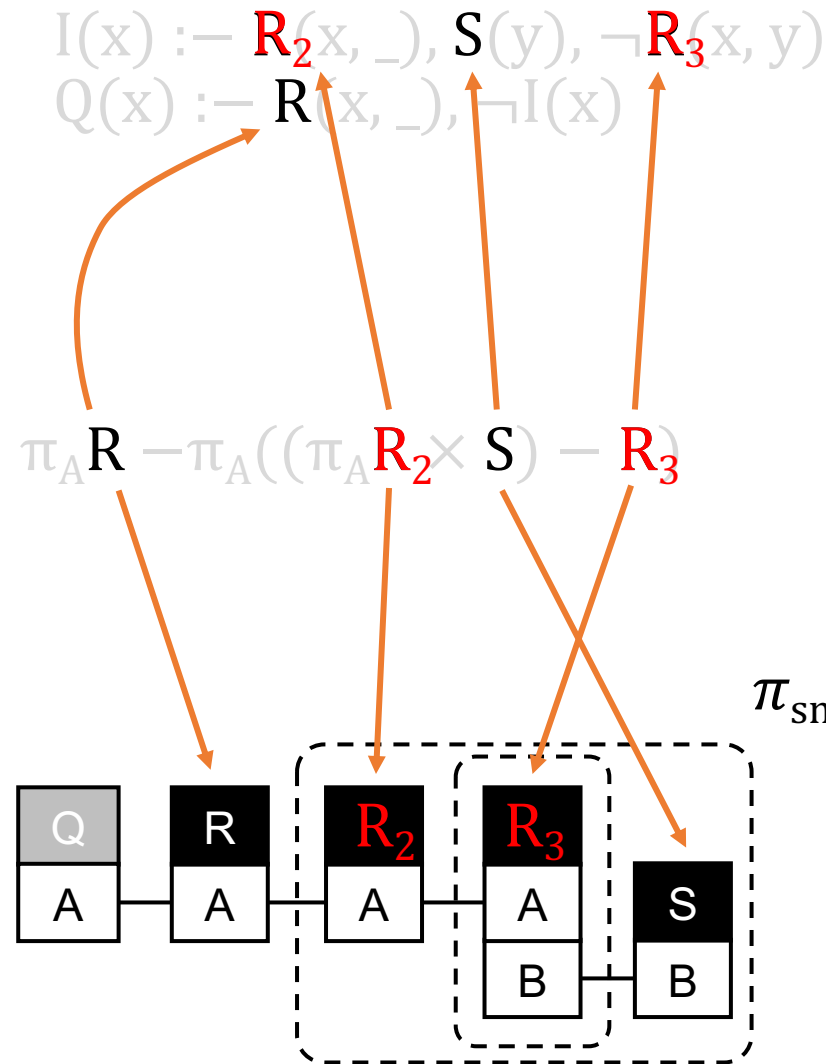
# Why patterns?

$R(A,B), S(B)$

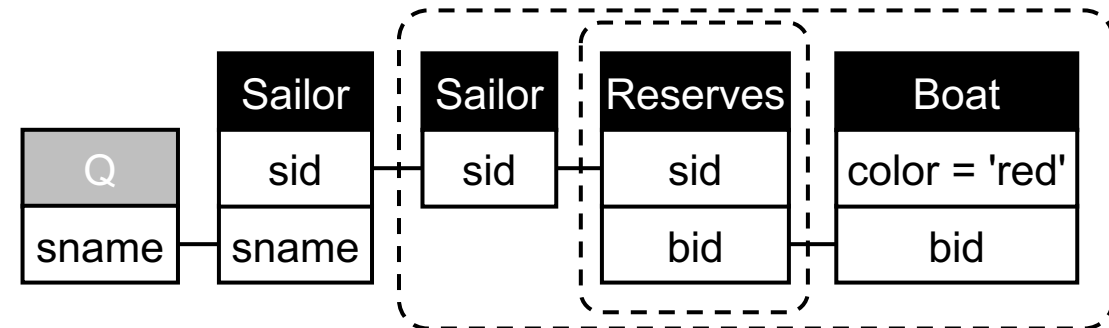
1. Focus on relational atoms only
2. Find a table-preserving mapping between relational atoms
3. But for "dissociated queries" (treat each EDB as different)

Are they still logically equivalent?

*Q: "Find sailors who have reserved all red boats"*



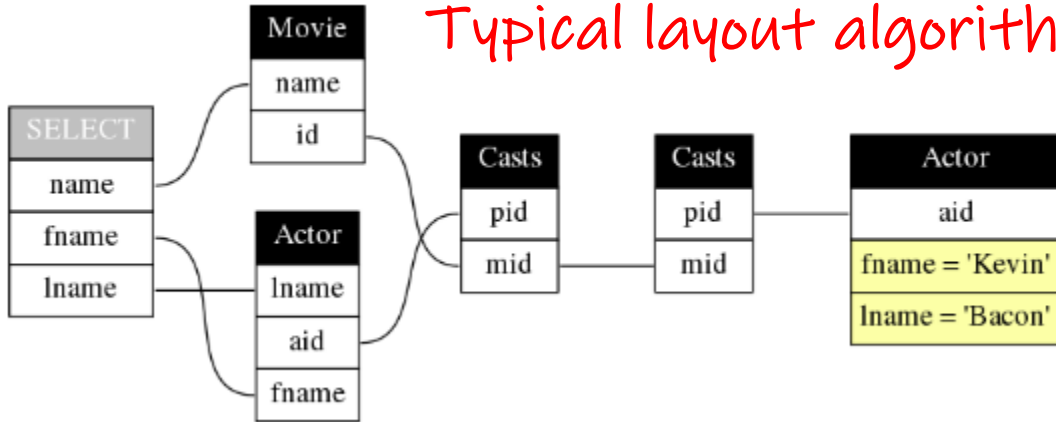
$\pi_{sname}(\text{Sailor} \triangleright_{sid} ((\text{Sailor} \times \rho_{color='red'} \text{Boat}) \triangleright_{sid, bid} \text{Reserves}))$



Notice the similarities, up to renaming of tables 😊

## 5. "Nice" layouts: Automatic layout algorithms

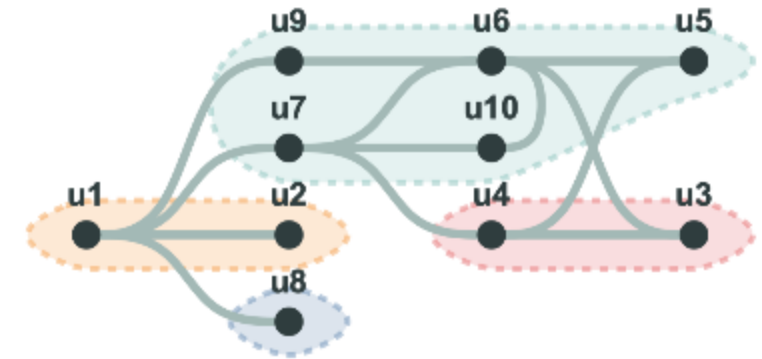
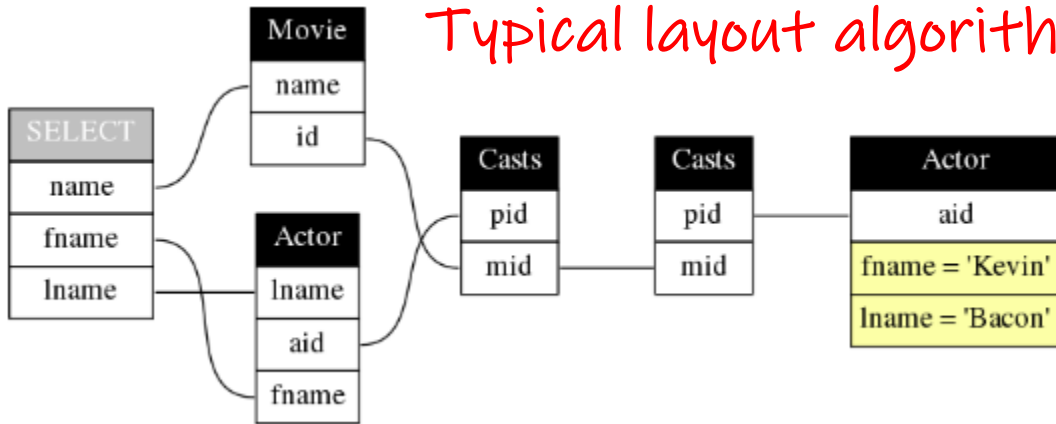
Typical layout algorithms cannot handle hierarchies well



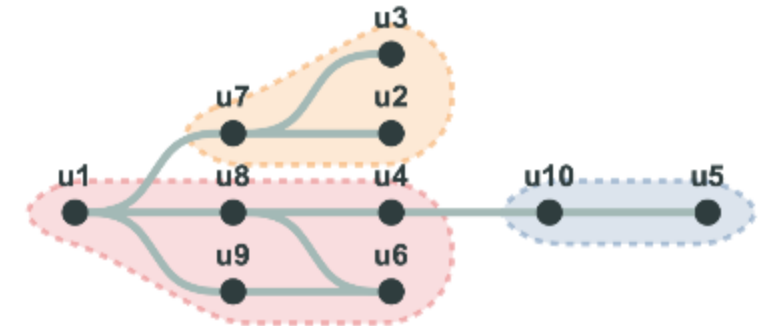
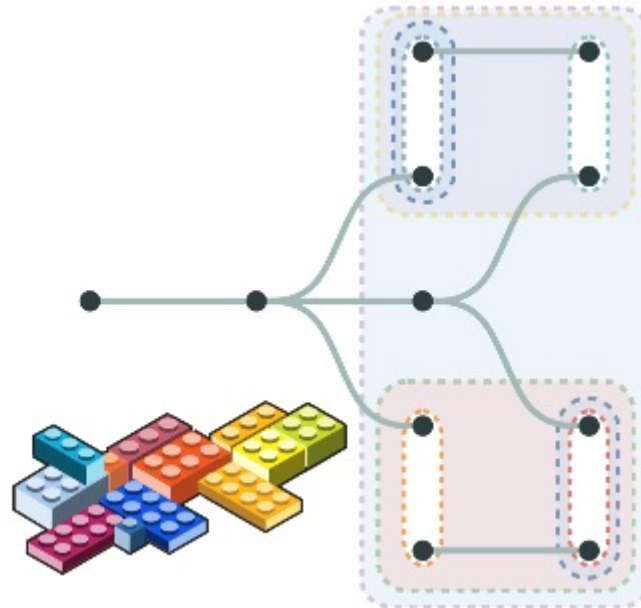
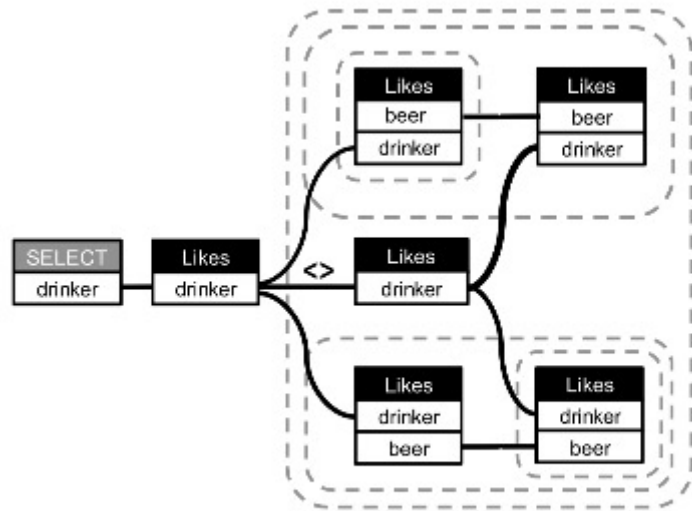
?



# 5. "Nice" layouts: Automatic layout algorithms

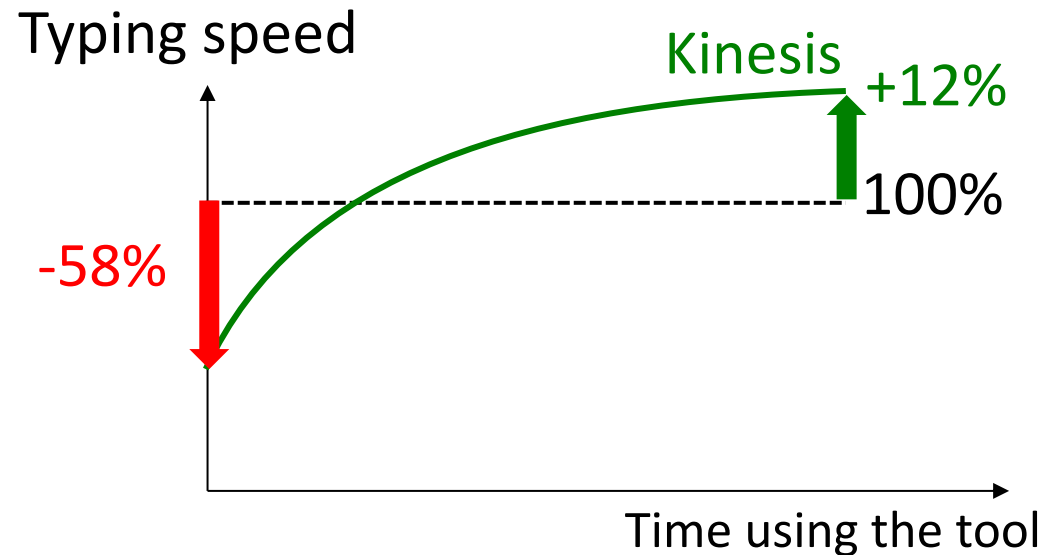


How do we design principled layered node-link visualizations?



## 6. Principled User Studies (preregistered, beyond students)

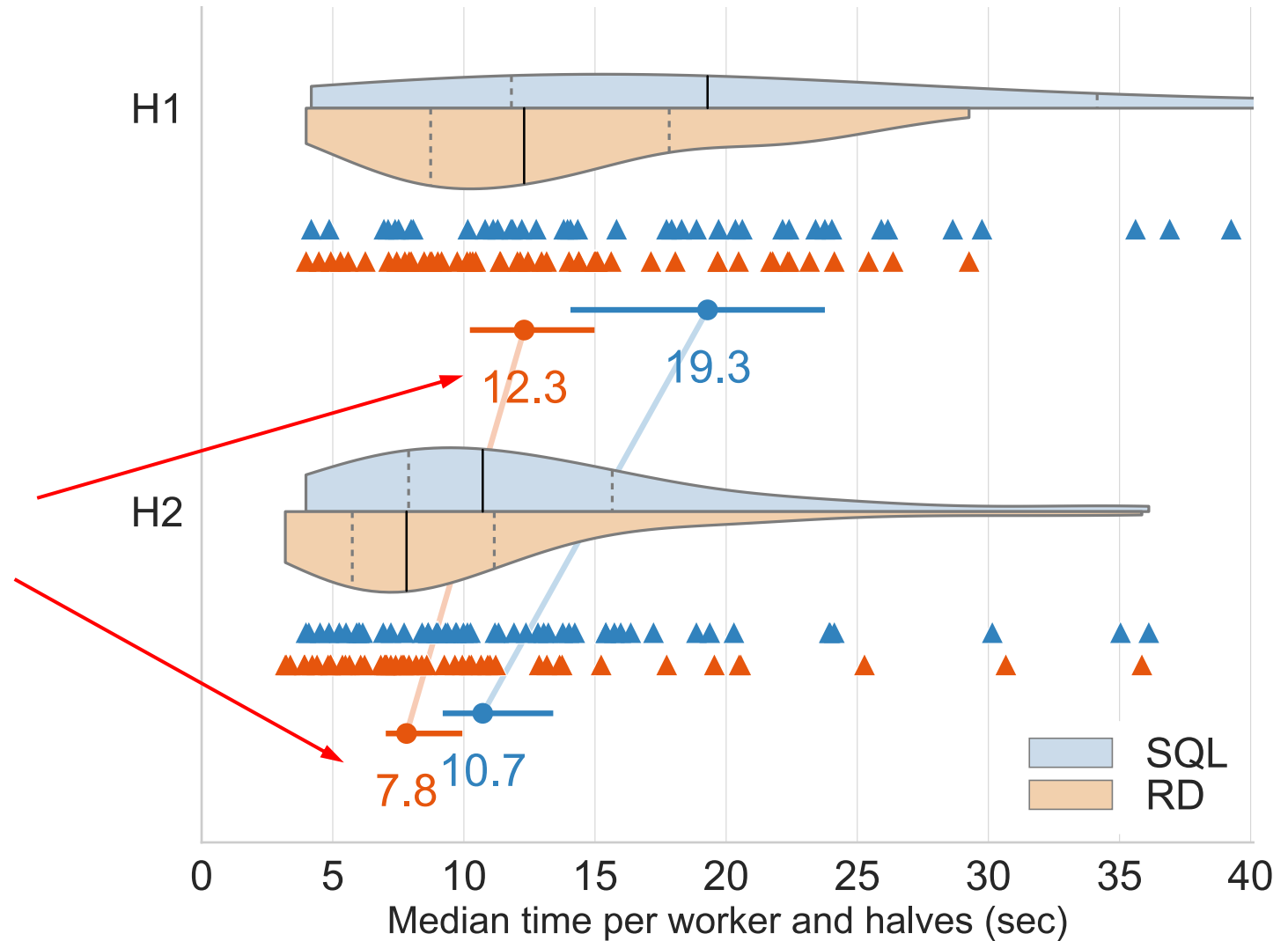
How to design principled, reproducible, longitudinal user studies?



# 6. Principled User Studies (preregistered, beyond students)

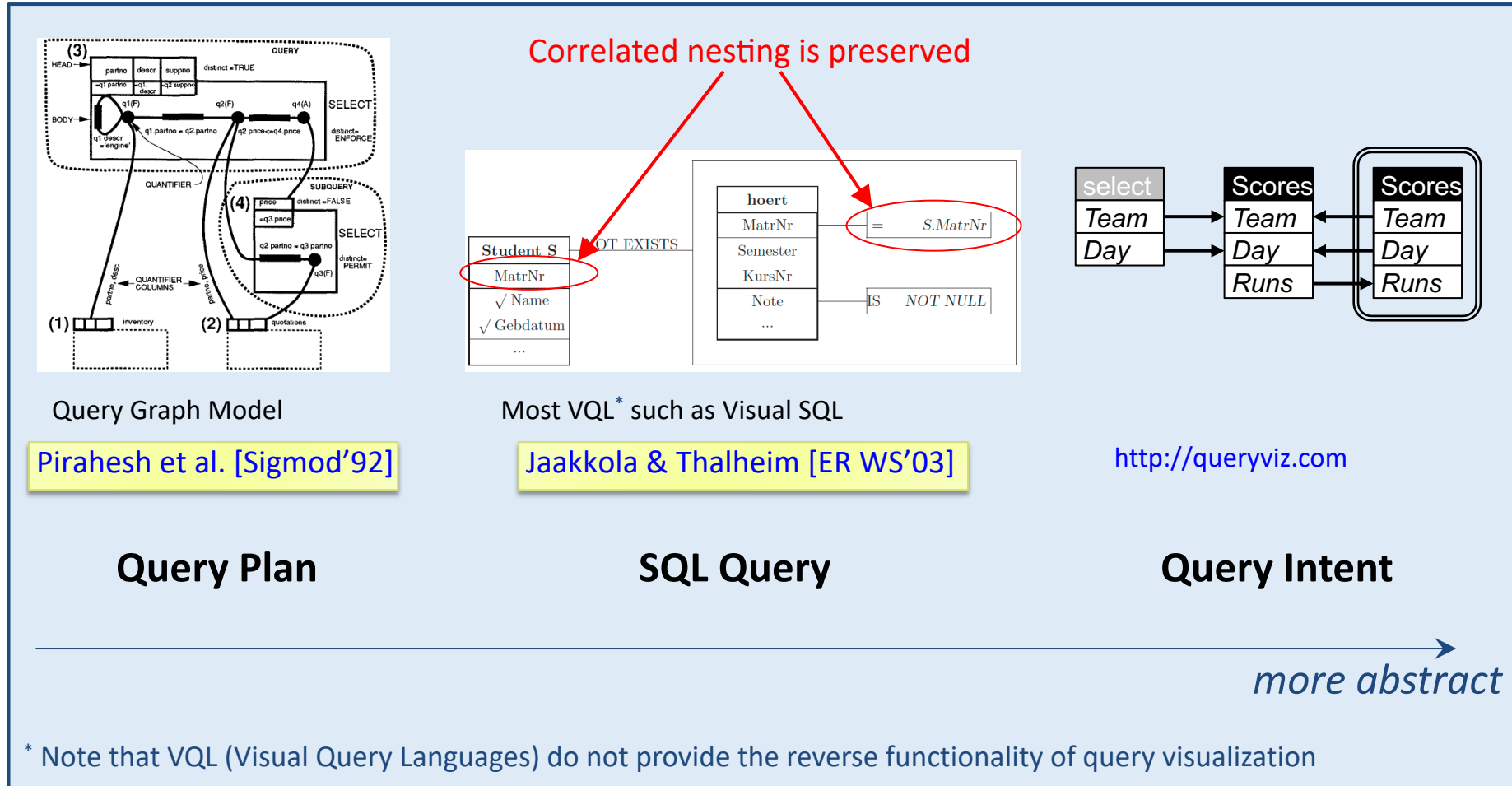
A recent user study that measured the learning by participants to interpret Relational Diagrams (counterbalanced within-subjects study with randomization)

Comparing the time to understand queries for the first half vs the second half of questions



# 7. Revisiting P7: syntactic invariance is maybe too strong

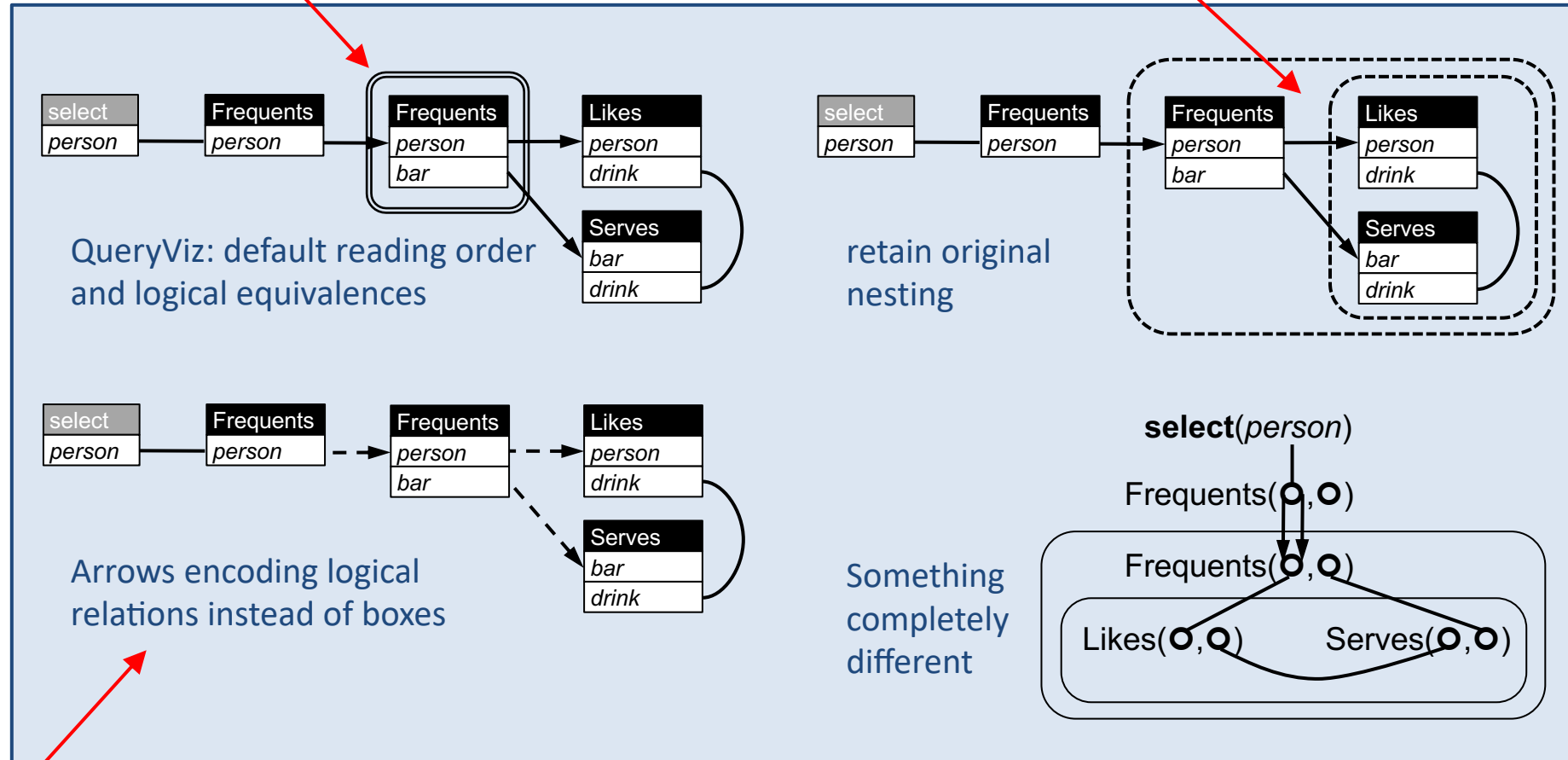
What is the appropriate level of abstraction? (intent vs. debugging)



# 8. What are other "better" visual metaphors?

Separate boxes was the choice of Queryvis

Nested boxes were considered but deemed visually too complex. Relational Diagrams made this choice.

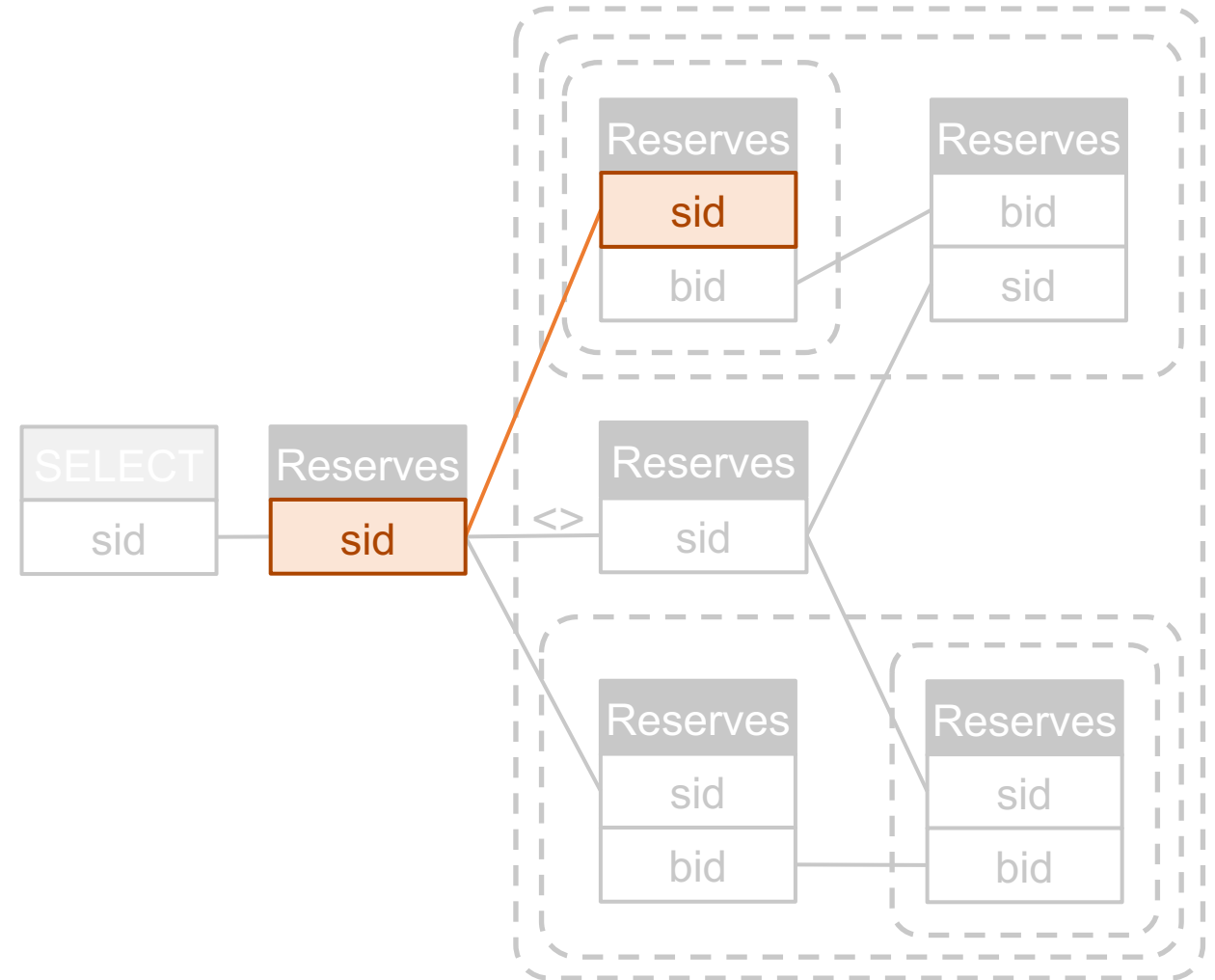


?

Likely not possible

## 9. What about interaction with diagrams?

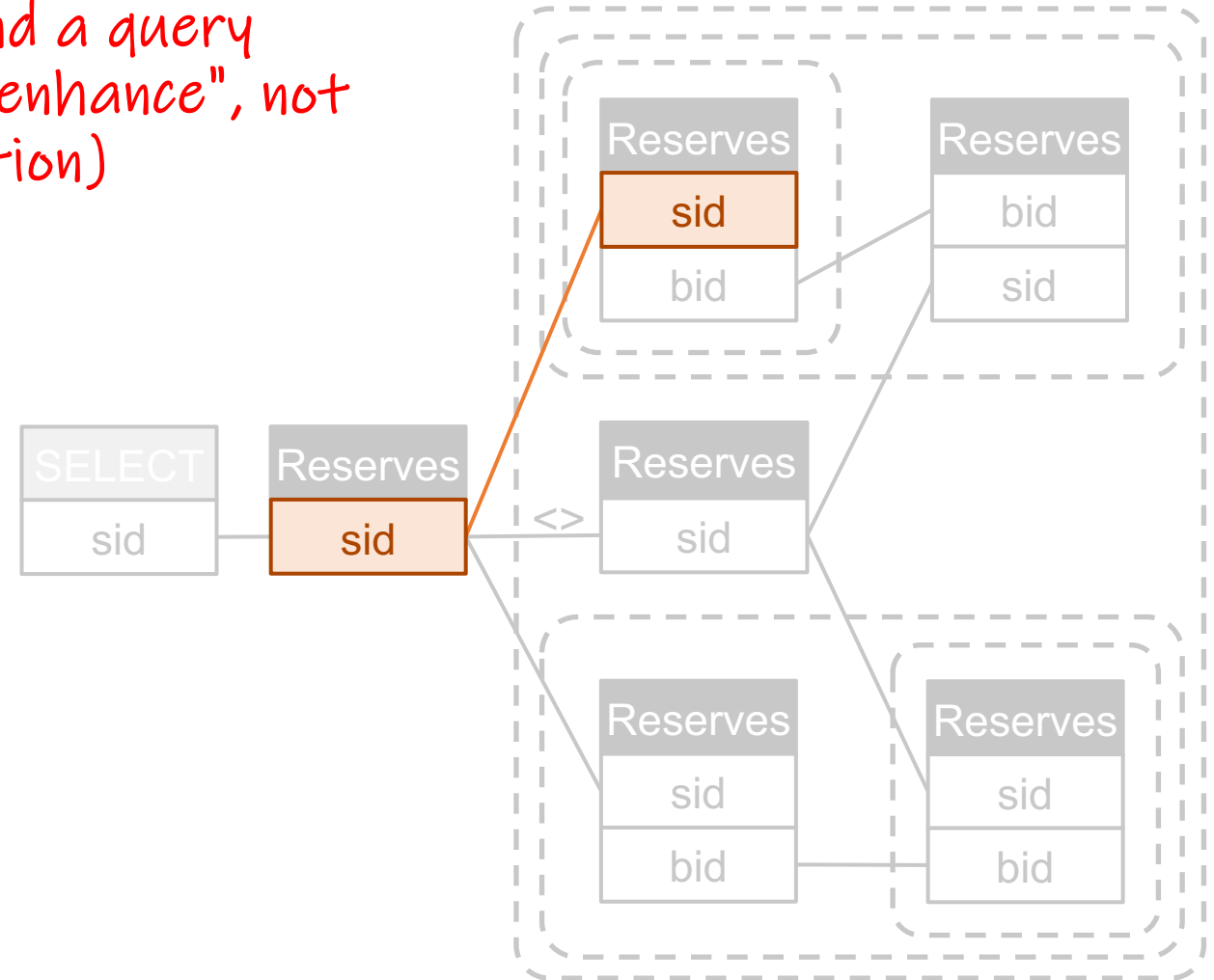
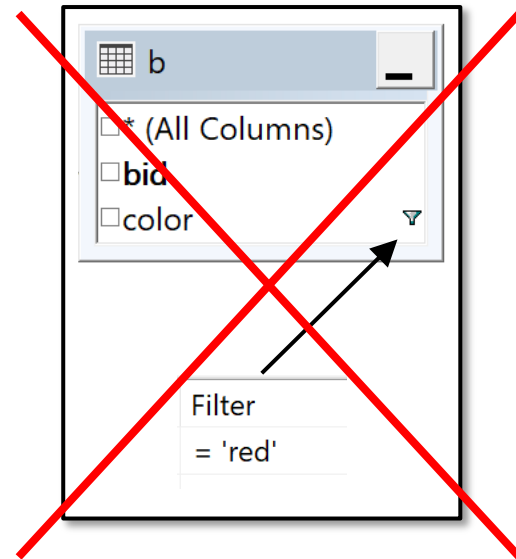
```
select distinct R1.sid
from Reserves R1
where not exists
(select *
from Reserves R2
where R1.sid <> R2.sid
and not exists
(select *
from Reserves R3
where R3.sid = R2.sid
and not exists
(select *
from Reserves R4
where R4.sid = R1.sid
and R4.bid = R3.bid)))
and not exists
(select *
from Reserves R5
where R5.sid = R1.sid
and not exists
(select *
from Reserves R6
where R6.sid = R2.sid
and R6.bid = R5.bid)))
```



# 9. What about interaction with diagrams?

```
select distinct R1.sid
from Reserves R1
where not exists
  (select *
   from Reserves R2
   where R1.sid <> R2.sid
   and not exists
     (select *
      from Reserves R3
      where R3.sid = R2.sid
      and not exists
        (select *
         from Reserves R4
         where R4.sid = R1.sid
         and R4.bid = R3.bid))
   and not exists
     (select *
      from Reserves R5
      where R5.sid = R1.sid
      and not exists
        (select *
         from Reserves R6
         where R6.sid = R2.sid
         and R6.bid = R5.bid)))
```

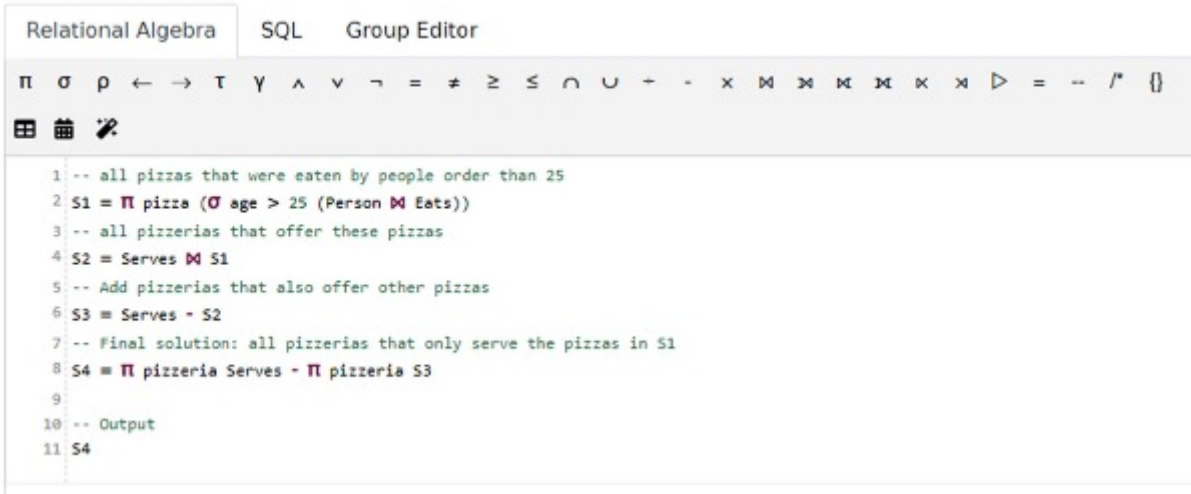
But recall: we don't want interaction required to understand a query (interactions should "enhance", not replace visual perception)





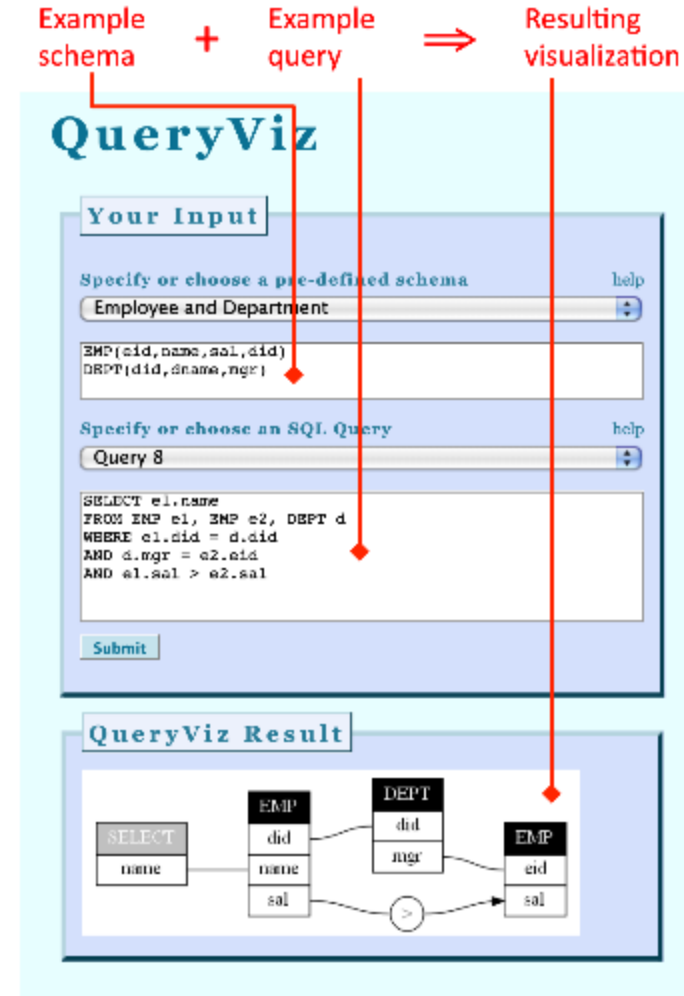
# 10. An ecosystem of tools that can translate between languages

Relax: relational algebra calculator (<https://dbis-uibk.github.io/relax/>):



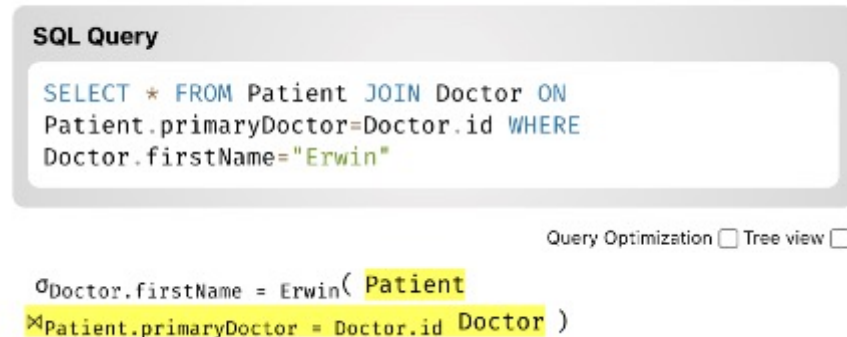
```
1 -- all pizzas that were eaten by people order than 25
2 S1 =  $\pi$  pizza ( $\sigma$  age > 25 (Person  $\bowtie$  Eats))
3 -- all pizzerias that offer these pizzas
4 S2 = Serves  $\bowtie$  S1
5 -- Add pizzerias that also offer other pizzas
6 S3 = Serves  $\cup$  S2
7 -- Final solution: all pizzerias that only serve the pizzas in S1
8 S4 =  $\pi$  pizzeria Serves  $\cap$   $\pi$  pizzeria S3
9
10 -- Output
11 S4
```

Online tools for translating b/w various query languages



Relational Playground by Michael Mior (<https://relationalplayground.com/>):

## Relational Playground



The screenshot shows the 'SQL Query' section with the following query:

```
SELECT * FROM Patient JOIN Doctor ON
Patient.primaryDoctor=Doctor.id WHERE
Doctor.firstName="Erwin"
```

Below the query, there are checkboxes for 'Query Optimization' and 'Tree view'. The 'Tree view' is selected, showing a diagrammatic representation of the query:

```
σDoctor.firstName = Erwin( Patient
⋈Patient.primaryDoctor = Doctor.id Doctor )
```

QueryVis:  
<http://demo.queryvis.com>



# Some take-aways from today

- Visualizations of Relational Expressions have been investigated for > 100 years
- The inverse functionality of query visualization ( $\neq$  VQLs from the 1990s) has not gotten much attention, yet new reasons to revisit
- Several (unresolved) issues lie in the actual details
- Solving those need rigorous and principled approaches

Thanks for your attention and please let me know about any mistakes you find. I must have missed some 😊

